# ITU-T 

Z. 100

TELECOMMUNICATION
Annex F3
STANDARDIZATION SECTOR
OF ITU

SERIES Z: LANGUAGES AND GENERAL SOFTWARE ASPECTS FOR TELECOMMUNICATION SYSTEMS
Formal description techniques (FDT) - Specification and Description Language (SDL)

Specification and Description Language - Overview of SDL-2010
Annex F3: SDL-2010 formal definition: Dynamic
semantics

Recommendation ITU-T Z. 100 - Annex F3

## ITU-T Z-SERIES RECOMMENDATIONS

## LANGUAGES AND GENERAL SOFTWARE ASPECTS FOR TELECOMMUNICATION SYSTEMS

| FORMAL DESCRIPTION TECHNIQUES (FDT) |
| :--- |
| Specification and Description Language (SDL) |
| Application of formal description techniques |
| Message Sequence Chart (MSC) |
| User Requirements Notation (URN) |
| Testing and Test Control Notation (TTCN) |
| PROGRAMMING LANGUAGES |
| CHILL: The ITU-T high level language |
| MAN-MACHINE LANGUAGE |
| General principles |
| Basic syntax and dialogue procedures |
| Extended MML for visual display terminals |
| Specification of the man-machine interface |
| Data-oriented human-machine interfaces |
| Human-machine interfaces for the management of telecommunications networks |
| QUALITY |
| Quality of telecommunication software |
| Quality aspects of protocol-related Recommendations |
| METHODS |
| Methods for validation and testing |
| MIDDLEWARE |
| Processing environment architectures |
| Z |

For further details, please refer to the list of ITU-T Recommendations.

## Recommendation ITU-T Z. 100

## Specification and Description Language - Overview of SDL-2010

## Annex F3 <br> SDL-2010 formal definition: Dynamic semantics

## Summary

This annex defines the SDL-2010 dynamic semantics.

History

| Edition | Recommendation | Approval | Study Group | Unique ID* |
| :---: | :---: | :---: | :---: | :---: |
| 1.0 | ITU-T Z.100 | $1984-10-19$ |  | $\underline{11.1002 / 1000 / 2222}$ |
| 1.1 | ITU-T Z.100 Annex A | $1984-10-19$ |  | $\underline{11.1002 / 1000 / 6664}$ |
| 1.2 | ITU-T Z.100 Annex B | $1984-10-19$ |  | $\underline{\underline{11.1002 / 1000 / 6665}}$ |
| 1.3 | ITU-T Z.100 Annex C1 | $1984-10-19$ |  | $\underline{11.1002 / 1000 / 6666}$ |
| 1.4 | ITU-T Z.100 Annex C2 | $1984-10-19$ |  | $\underline{11.1002 / 1000 / 6667}$ |
| 1.5 | ITU-T Z.100 Annex D | $1984-10-19$ |  | $\underline{\underline{11.1002 / 1000 / 6668}}$ |
| 2.0 | ITU-T Z.100 | $1987-09-30$ | X | $\underline{11.1002 / 1000 / 10954}$ |
| 2.1 | ITU-T Z.100 Annex A | $1988-11-25$ |  | $\underline{11.1002 / 1000 / 6669}$ |
| 2.2 | ITU-T Z.100 Annex B | $1988-11-25$ |  | $\underline{\underline{11.1002 / 1000 / 6670}}$ |
| 2.3 | ITU-T Z.100 Annex C1 | $1988-11-25$ |  | $\underline{11.1002 / 1000 / 6671}$ |
| 2.4 | ITU-T Z.100 Annex C2 | $1988-11-25$ |  | $\underline{11.1002 / 1000 / 6672}$ |
| 2.5 | ITU-T Z.100 Annex D | $1988-11-25$ | $X$ | $\underline{11.1002 / 1000 / 3646}$ |
| 2.6 | ITU-T Z.100 Annex E | $1988-11-25$ |  | $\underline{11.1002 / 1000 / 6673}$ |
| 2.7 | ITU-T Z.100 Annex F1 | $1988-11-25$ | $X$ | $\underline{11.1002 / 1000 / 3647}$ |
| 2.8 | ITU-T Z.100 Annex F2 | $1988-11-25$ | $X$ | $\underline{11.1002 / 1000 / 3648}$ |
| 2.9 | ITU-T Z.100 Annex F3 | $1988-11-25$ | $X$ | $\underline{11.1002 / 1000 / 3649}$ |
| 3.0 | ITU-T Z.100 | $1988-11-25$ |  | $\underline{11.1002 / 1000 / 3153}$ |
| 3.1 | ITU-T Z.100 Annex C | $1993-03-12$ | $X$ | $\underline{11.1002 / 1000 / 3155}$ |
| 3.2 | ITU-T Z.100 Annex D | $1993-03-12$ | $X$ | $\underline{11.1002 / 1000 / 3156}$ |
| 3.3 | ITU-T Z.100 Annex F1 | $1993-03-12$ | X | $\underline{11.1002 / 1000 / 3157}$ |

[^0]| 3.4 | ITU-T Z.100 Annex F2 | $1993-03-12$ | X | $\underline{\underline{11.1002 / 1000 / 3158}}$ |
| :--- | :---: | :---: | :---: | :---: |
| 3.5 | ITU-T Z.100 Annex F3 | $1993-03-12$ | X | $\underline{11.1002 / 1000 / 3159}$ |
| 3.6 | ITU-T Z.100 App. I | $1993-03-12$ | X | $\underline{11.1002 / 1000 / 3160}$ |
| 3.7 | ITU-T Z.100 App. II | $1993-03-12$ | X | $\underline{11.1002 / 1000 / 3161}$ |
| 4.0 | ITU-T Z.100 | $1993-03-12$ | X | $\underline{\underline{11.1002 / 1000 / 3154 ~}}$ |
| 4.1 | ITU-T Z.100 (1993) Add. 1 | $1996-10-18$ | 10 | $\underline{11.1002 / 1000 / 3917}$ |
| 5.0 | ITU-T Z.100 | $1999-11-19$ | 10 | $\underline{11.1002 / 1000 / 4764}$ |
| 5.1 | ITU-T Z.100 (1999) Cor. 1 | $2001-10-29$ | 17 | $\underline{11.1002 / 1000 / 5567}$ |
| 6.0 | ITU-T Z.100 | $2002-08-06$ | 17 | $\underline{11.1002 / 1000 / 6029}$ |
| 6.1 | ITU-T Z.100 (2002) Amd. 1 | $2003-10-29$ | 17 | $\underline{11.1002 / 1000 / 7091}$ |
| 6.2 | ITU-T Z.100 (2002) Cor. 1 | $2004-08-29$ | 17 | $\underline{11.1002 / 1000 / 356}$ |
| 7.0 | ITU-T Z.100 | $2007-11-13$ | 17 | $\underline{11.1002 / 1000 / 9262}$ |
| 8.0 | ITU-T Z.100 | $2011-12-22$ | 17 | $\underline{11.1002 / 1000 / 11387}$ |
| 8.1 | ITU-T Z.100 Annex F1 | $2000-11-24$ | 10 | $\underline{11.1002 / 1000 / 5239}$ |
| 8.2 | ITU-T Z.100 Annex F2 | $2000-11-24$ | 10 | $\underline{11.1002 / 1000 / 5576}$ |
| 8.3 | ITU-T Z.100 Annex F3 | $2000-11-24$ | 10 | $\underline{11.1002 / 1000 / 5577}$ |
| 8.4 | ITU-T Z.100 Annex F1 | $2015-01-13$ | 17 | $\underline{11.1002 / 1000 / 12354}$ |
| 8.5 | ITU-T Z.100 Annex F2 | $2015-01-13$ | 17 | $\underline{11.1002 / 1000 / 12355}$ |
| 8.6 | ITU-T Z.100 Annex F3 | $2015-01-13$ | 17 | $\underline{11.1002 / 1000 / 12356}$ |
| 9.0 | ITU-T Z.100 | $2016-04-29$ | 17 | $\underline{11.1002 / 1000 / 12846}$ |
| 9.1 | ITU-T Z.100 Annex F1 | $2016-10-29$ | 17 | $\underline{11.1002 / 1000 / 13040}$ |
| 9.2 | ITU-T Z.100 Annex F2 | $2016-10-29$ | 17 | $\underline{11.1002 / 1000 / 13041}$ |
| 9.3 | ITU-T Z.100 Annex F3 | $2016-10-29$ | 17 | $\underline{11.1002 / 1000 / 13042}$ |

## Keywords

Specification and Description Language, SDL-2010, formal definition, Dynamic semantics, Behaviour semantics, SDL-2010 abstract machine, SAM, Compilation function, SAM programs, Data semantics.

## FOREWORD

The International Telecommunication Union (ITU) is the United Nations specialized agency in the field of telecommunications, information and communication technologies (ICTs). The ITU Telecommunication Standardization Sector (ITU-T) is a permanent organ of ITU. ITU-T is responsible for studying technical, operating and tariff questions and issuing Recommendations on them with a view to standardizing telecommunications on a worldwide basis.

The World Telecommunication Standardization Assembly (WTSA), which meets every four years, establishes the topics for study by the ITU-T study groups which, in turn, produce Recommendations on these topics.
The approval of ITU-T Recommendations is covered by the procedure laid down in WTSA Resolution 1.
In some areas of information technology which fall within ITU-T's purview, the necessary standards are prepared on a collaborative basis with ISO and IEC.

## NOTE

In this Recommendation, the expression "Administration" is used for conciseness to indicate both a telecommunication administration and a recognized operating agency.

Compliance with this Recommendation is voluntary. However, the Recommendation may contain certain mandatory provisions (to ensure, e.g., interoperability or applicability) and compliance with the Recommendation is achieved when all of these mandatory provisions are met. The words "shall" or some other obligatory language such as "must" and the negative equivalents are used to express requirements. The use of such words does not suggest that compliance with the Recommendation is required of any party.

## INTELLECTUAL PROPERTY RIGHTS

ITU draws attention to the possibility that the practice or implementation of this Recommendation may involve the use of a claimed Intellectual Property Right. ITU takes no position concerning the evidence, validity or applicability of claimed Intellectual Property Rights, whether asserted by ITU members or others outside of the Recommendation development process.

As of the date of approval of this Recommendation, ITU had not received notice of intellectual property, protected by patents, which may be required to implement this Recommendation. However, implementers are cautioned that this may not represent the latest information and are therefore strongly urged to consult the TSB patent database at http://www.itu.int/ITU-T/ipr/.

All rights reserved. No part of this publication may be reproduced, by any means whatsoever, without the prior written permission of ITU.

## Table of Contents

Page
Annex F3 - SDL-2010 formal definition: Dynamic semantics ..... 1
F3.1 General information ..... 1
F3.2 Behaviour semantics ..... 2
F3.3 Data semantics ..... 76
Appendix I to Annex F3 - List of abstract syntax grammar rules used. ..... 95

## Recommendation ITU-T Z. 100

## Specification and Description Language - Overview of SDL-2010

## Annex F3

## SDL-2010 formal definition: Dynamic semantics

## F3.1 General information

An overview of the formal semantics is described in clause F1.2 (Annex F1).

## F3.1.1 Definitions from Annex F1

The following definitions for the syntax and semantics of ASMs are used within Annex F3. The domains and functions are defined in Annex F1 and listed here for cross-referencing reasons.

The keywords case, choose, constraint, controlled, derived, do, domain, else, elseif, endcase, endchoose, enddo, endextend, endif, endlet, endwhere, extend, forall, if, initially, let, monitored, of, shared, static, then, where, with.

The domains Time, AGENT, X, Boolean, NAT, REAL, TOKEN, DEFINITIONASI.
The functions take, program, Self, undefined, true, false, empty, head, tail, last, length, toSet, parentAS1, parentASlofKind, rootNodeAS1.

The operation symbols $*,+,-\mathbf{s e t},-\mathbf{s e q},=, \neq \wedge, \vee, \Rightarrow, \Leftrightarrow, \neg, \exists, \forall,>, \geq,<, \leq,+,-, *, /, \mathbf{i n}, \times, \frown, \cup, \cap, \backslash, \in, \notin$, $\subseteq, \subset, \|, \cup, \varnothing, \mathbf{m k}-, \mathbf{s}^{-}$, s2-.
For more information about the ASM syntax, see Annex F1.

## F3.1.2 Definitions from Annex F2

EntityDefinitions: the union of all the entity definitions in AS1. It is therefore a subset of DEFINITIONAS1.

EntityDEFInItIon $_{l}=$ def Agent-definition
$\checkmark$ Agent-type-definition
$\cup$ Channel-definition
$\cup$ Composite-state-type-definition
$\cup$ Data-type-definition
$\cup$ Gate-definition
$\cup$ Literal-signature
$\cup$ Operation-signature
$\cup$ Package-definition
$\cup$ Procedure-definition
$\cup$ Signal-definition
$\cup$ State-node
$\cup$ Syntype-definition
$\cup$ Timer-definition
$\cup$ Variable-definition
ENTITYKIND1: the set of all the entity kinds in AS1.
ENTITYKIND $1=_{\text {def }}$ \{agent, agent type, package, state, state type, procedure, variable,
signal, timer, channel, gate, sort, exception, literal, operation\}

Given an Identifier, the corresponding EntityDEfinition 1 is retrieved using the function idToNodeAS1:
idToNodeASl(id: Identifier): $\left[\right.$ ENTITYDEFINITION $\left._{l}\right]={ }_{\text {def }}$ getEntityDefinition ${ }_{l}\left(i d\right.$, idKind $_{l}(i d)$ )
where:
function getEntityDefinition ${ }_{I}$ from Annex F2 gets the entity definition for an identifier:
getEntityDefinition $n_{1}$ : Identifier, ENTITYKIND ${ }_{l} \rightarrow$ EntityDEFInITION $_{l}$
and function idKind $_{1}$ from Annex F2 is used determine the kind of the entity from the identifier: idKind $_{1}:$ Identifier $\rightarrow$ EntityKind $_{I}$

Given an EntityDEfinition ${ }_{l}$, the corresponding Identifier is retrieved using the function identifier $_{l}$ from Annex F2:

```
identifier l: ENTITYDEFINITION
```

Given two definitions, whether one is a supertype of the other is determined using the function isSuperType from F2:
isSuperType: EntityDEFINITION $\times$ ENTITYDEFINITION $_{l} \rightarrow$ Boolean $^{2}$

## F3.1.3 Status of Annex F3 (this annex)

The ASM in the previous $(01 / 2015)$ edition had been updated to correct errors in the earlier $(01 / 2000)$ edition and to reflect the features of SDL-2010 compared with SDL-2000. The ASM was not complete in the $(01 / 2000)$ edition. For example, the $(01 / 2000)$ edition mentions the function objectsAssign and the macro SetObjects, but the definitions of these items were not included. While the $(01 / 2015)$ edition was an improvement on the previous edition, some items still needed further work, in particular adding the treatment of an Aggregation-kind of REF (see [ITU-T Z.107]) that replaces object data types.
As noted in clause F1.2.4 (d) (Annex F1), the data semantics is separated from the rest of the dynamic semantics, which allows the data model to be changed. The current document is based on the previous edition ( $01 / 2000$ ) that described the object data types of SDL-2000. The document has been considerably reduced by the removal of object data types, user exception definitions, user exception raising and exception handling.
The ( $01 / 2000$ ) edition included a clause " 4 Example", where an example specification and its expansion into an abstract syntax tree were given, but the results of initialization and compilation of the example had "TBD" sentences, meaning work was still to be done. In this state the example is not useful for the illustrating application of the dynamic semantics, and it has been removed from this edition.

## F3.2 Behaviour semantics

This clause defines the following parts of the dynamic semantics:

- the SAM (SDL-2010 Abstract Machine): clause F3.2.1;
- the compilation function: clause F3.2.2; and
- SAM programs: clause F3.2.3.

An overview of the dynamic semantics is given in clause F1.2.4 (Annex F1).

## F3.2.1 SDL-2010 abstract machine definition (SAM)

The SAM constitutes a generic behaviour model for SDL-2010 specifications. According to an abstract operational view, the possible computations of a given SDL-2010 specification are defined in terms of ASM runs. The underlying semantic model of distributed real-time ASMs is explained in Annex F1. The SAM definition consists of the following four main building blocks:

- signal flow related definitions: clause F3.2.1.1;
- SDL-2010 agent-related definitions: clause F3.2.1.2;
- the interface to the data semantics: clause F3.2.1.3; and
- behaviour primitives: clause F3.2.1.4.

These definitions, in particular, also state explicitly the various constraints on initial SAM states complementing the behaviour model.

## F3.2.1.1 Signal flow model

This clause introduces the signal flow model as part of the SAM. The main focus here is on a uniform treatment of signal flow aspects, in particular, on defining how agents communicate through signals via gates. Also, timers (clause F3.2.1.1.5), which are modelled as special kinds of signals, are treated here.

## F3.2.1.1.1 Signals

PLainSignal represents the set of signal types as declared by an SDL-2010 specification.

$$
\text { PLAINSIGNAL }=_{\text {def }} \text { Identifier } \cup \text { NONE }
$$

In an SDL-2010 specification, also timers (clause F3.2.1.1.5) are considered as signals; they are contained in a common domain SIGNAL

$$
\text { SIGNAL }^{\operatorname{def}} \text { PLAINSIGNAL } \cup \text { TIMER }
$$

Dynamically created plain signal instances (plain signals for short) are elements of a dynamic domain PLAINSIGNALINST. Since plain signals can also be created and sent by the environment, this domain is shared. The function plainSignalType gives the signal type for a given plain signal instance.

```
shared domain PlainSIGNALInSt
initially PLAINSIGNALINST = \varnothing
shared plainSignalType: PLAInSIGNALINST }->\mathrm{ PLAINSIGNAL
```

The domain SIGNALINST contains all kinds of signal instances (signals for short). Each element of SIGNALINST is uniquely related to an element of SIGNAL, as defined by the derived function signalType.

```
SIGNALINST = def PLAINSIGNALINST }\cup\mathrm{ TIMERINST
signalType(si:SIGNALINST): SIGNAL = =def
    if si\inPLAINSIGNALINST then si.plainSignalType
    elseif si \in TimerInst then si.s-TimER
    endif
```

The functions plainSignalSender (giving the sender process) and signalSender (giving the sender of the signal or the agent for the timer) are defined:

```
shared plainSignalSender: PLAINSIGNALINST }->\mathrm{ PID
signalSender(si:SIGNALINST): PID = def
    if si \in PlainSIGNALINST then si.plainSignalSender
    elseif si G TIMERINST then si.s-PID
```

endif
With each signal a (possibly empty) list of signal values is associated. Because the type information and concrete value for signal values is immaterial to the dynamic aspects considered here, values are abstractly represented in a uniform way as elements of the static domain VALUE (see clause F3.2.1.3):

```
shared plainSignalValues: PLAINSIGNALInST }->\mathrm{ VALUE*
```

SDL-2010 provides for two forms of indicating the receiver of a message, where the receiver may also remain unspecified.

```
VIAARG = def Identifier-set
TOARG = def PID }\cup\mathrm{ Identifier
```

Additional functions on plain signals are toArg (giving the destination) and viaArg (giving optional constraints on admissible communication paths).

Signals received at an input gate of an agent set are appended to the input port of an agent instance depending on the value of toArg. Signals are discarded whenever no matching receiver instance exists.

The value of type PID is evaluated dynamically and associated with the label.

```
shared toArg: PLAINSIGNALINST }->\mathrm{ [TOARG]
shared viaArg: PLAINSIGNALInST }->\mathrm{ VIAARG
```


## F3.2.1.1.2 Gates

Exchange of signals between SDL-2010 agents (such as processes, blocks or a system) and the environment is modelled by means of gates from a controlled domain GATE.

```
controlled domain GATE
    initially GATE = \varnothing
```

A gate forms an interface for serial and unidirectional communication between two or more agents. Accordingly, gates are either classified as input gates or output gates (see clause F3.2.1.2.4).

```
DIRECTION \(=_{\text {def }}\{\) inDir, outDir \(\}\)
controlled direction: GATE \(\rightarrow\) DIRECTION
controlled myAgent: GATE \(\rightarrow\) AGENT
```


## Global system time

In SDL-2010, the global system time is represented by the expression now assuming that values of now increase monotonically over system runs. In particular, SDL-2010 allows having the same value of now in two or more consecutive system states. Building on the concept of distributed real-time ASM, this behaviour is modelled using a nullary, dynamic, monitored function now. Intuitively, now refers to internally observable values of the global system time.

```
monitored now: }->\mathrm{ TIME
```

There are two integrity constraints on the behaviour of now:

1. now values change monotonically, increasing over ASM runs;
2. now values do not increase as long as a signal is in transit on a non-delaying channel.

## Discrete delay model

Signals need not reach their destination instantaneously, but may be subject to delays, which means, it is possible to send signals to arrive in the future. Although those signals are not available at their destination before their arrival time has come, they are to be associated with their destination gates. A gate has to be capable of holding signals that are in transit (not yet arrived). Hence, to each gate a possibly empty signal queue is assigned, as detailed below.
To model signal arrivals at specified destination gates, each signal instance $s i$ has an individual arrival time (siarrival) determining the time at which $s$ eventually reaches a certain gate.
shared arrival: SIGNALINST $\rightarrow$ TIME
The relation between signals and gates in a given SAM state is represented by means of a dynamic function schedule defined on gates:

```
shared schedule: Gate }->\mathrm{ SIGNALInsT*
```

where schedule specifies, for each gate $g$ in GATE, the corresponding signal arrivals at $g$.
An integrity constraint on g.schedule is that signals in g.schedule are linearly ordered by their arrival times. That is, if g.schedule contains signals si, si', and si.arrival < si'.arrival, then $s i<s i '$ in the order as imposed by g.schedule. This condition is assured by the insert function below.

## Waiting signals

A signal instance si in g.schedule does not arrive "physically" at gate $g$ before now $\geq$ si.arrival. Intuitively, that means that $s$ remains "invisible" at $g$ as long as it is in transit. Thus, in every given SAM state, the visible part of $g$.schedule forms a possibly empty signal queue $g . q u e u e$, where $g . q u e u e$ represents those signal instances si in g.schedule that have already arrived at $g$ but are still waiting to be removed from g.schedule. The visible part of $g$ is denoted as g.queue and formally defined as follows.

```
queue(g:GATE): SIGNALINST* }=\mathrm{ def < si in g.schedule: (now }\geq\mathrm{ si.arrival) >
```

See also Figure F3-1 below for an overview of the functions on schedules.


Figure F3-1 - Signal instances at a gate

## Operations on schedules

To ensure that the order on signals is preserved when new signals are added to the schedule of a gate, there is a special insertion function insert on schedules.

```
insert(si:SIGNALInST, \(t:\) Time, siSeq:SIGNALINST*): SIGNALINST* \(=_{\mathrm{def}}\)
    if siSeq = empty then
        \(\left\langle s i>{ }^{\text {siSeq }}\right.\)
    elseif \(t<\) siSeq.head.arrival
    then \(\langle s i\rangle\) siSeq
    else < siSeq.head> \(\operatorname{insert(si,t,\text {siSeq.tail)})~(1)}\)
```

endif
The function insert defines the result of inserting some signal instance si with the intended arrival time $t$ into a finite signal instance list siSeq, representing (for example) the schedule of a gate. Analogously, a function delete is used to remove a signal from a finite signal instance list siSeq.

```
delete(si:SIGNALInST, siSeq:SIGNALINST*): SIGNALINST* = def
    if siSeq = empty then empty
    elseif siSeq.head = si then siSeq.tail
    else < siSeq.head > delete(si, siSeq.tail)
    endif
```

The macros InSERT and DELETE update the schedule of a gate $g$ by assigning some new signal list to g.schedule.

```
INSERT(si:SIGNALINST, t:TIME, g:GATE) \equiv
    g.schedule := insert(si,t,g.schedule)
    si.arrival := t+si.delay
DELETE(si:SIGNALINST, g:GATE) \equiv
    g.schedule := delete(si,g.schedule)
```

The function nextSignal yields, for a sequence of signal instances and a signal instance, the next signal instance of the sequence, or the value undefined, if the next signal instance is not determined.

```
nextSignal(si: SIGNALINST, siSeq:SIGNALINST*): [SIGNALINST] = def
    if siSeq = empty then undefined
    elseif siSeq.head =si then
        if siSeq.tail = empty then undefined
        else siSeq.tail.head
        endif
    else nextSignal(si, siSeq.tail)
    endif
```

The function selectContinuousSignal yields, for a set of continuous signal transitions and a set of natural numbers, an element of the transition set with a priority not contained in the set of natural numbers, such that this priority is the maximum priority of all transitions not having priorities in this set of natural numbers.

```
selectContinuousSignal(tSet: SEMTRANSITION-set, nSet: NAT-set): [SEMTRANSITION] = def
    if }\foralltl\intSet: t1.s-NAT \in nSet then undefined
    else take({t t tSet:t.s-NAT & nSet ^\foralltl \intSet: (tl.s-NAT & nSet =>t.s-NAT\leqtl.s-NAT)})
    endif
```


## F3.2.1.1.3 Channels

Channels, as declared in a given SDL-2010 specification, consist of either one or two unidirectional channel paths. In the SAM model, each channel path is identified with an object of a derived domain LINK. The elements of LINK are SAM agents, such that their behaviour is defined through LinkProgram.

$$
\text { LINK }=\operatorname{def} A G E N T
$$

$$
\text { LINKSEQ }=_{\operatorname{def}} \operatorname{LINK} *
$$

Intuitively, elements of LINK are considered as point-to-point connection primitives for the transport of signals. More specifically, each $l$ of LINK is able to convey certain signal types, as specified by $l$.with, from an originating gate $l$.from to a destination gate $l$.to, and $l . n o d e l a y$ indicating if $l$ is nondelaying.

```
controlled with: LINK }->\mathrm{ SIGNAL-set
```

controlled from: LINK $\rightarrow$ [ GATE ] // need to have optional result here, because function is also called within allConnections with general AGENT
controlled to: LINK $\rightarrow$ GATE
controlled noDelay: LINK $\rightarrow$ [NODELAY]

## Signal delays

SDL-2010 considers channels as reliable and order-preserving communication links. A channel is able to delay the transport of a signal for an indeterminate and non-constant time interval. Although the exact delaying behaviour is not further specified, the fact that channels are reliable implies that all delays are finite.

Signal delays are modelled through a monitored function delay stating the dependency on external conditions and events. In a given SAM state, delay associates finite time intervals from a domain DURATION to the elements of LINK, where the duration of a particular signal delay appears to be chosen non-deterministically.

```
DURATION = def REAL
monitored delay: LINK }->\mathrm{ DURATION
```


## Integrity constraints

There are two important integrity constraints on the function delay:

1. Taking into account that there are also non-delaying channels, the only admissible value for non-delaying channel paths is 0 .
2. For every link agent $l$, the value of (now $+l$.delay) increases monotonically (with respect to now).

The second integrity constraint is needed in order to ensure that channel paths are order-preserving: that is, signals transported via the same channel path (and therefore are inserted into the same destination schedule) cannot overtake each other.

## Channel behaviour

A link agent $l$ performs a single operation: signals received at gate $l$.from are forwarded to gate l.to. That means, $l$ permanently watches $l$.from waiting for the next deliverable signal in l.from.queue. Whenever $l$ is applicable to a waiting signal si (as identified by the $l$.from.queue.head), it attempts to remove si from l.from.queue in order to insert it into l.to.schedule. This attempt need not necessarily be successful as, in general, there may be several link agents competing for the same signal si.

But, how does a link agent $l$ know whether it is applicable to a signal si? Now, this decision does of course depend on the values of si.toArg, si.viaArg, si.signalType and $l$.with. In other words, $l$ is a legal choice for the transportation of si only, if the following two conditions hold: (1) si.signalType $\in$ l.with and (2) there exists an applicable path connecting l.to to some final destination that matches with the address information and the path constraints of si. Abstractly, this decision can be expressed using a predicate applicable, defined in clause F3.2.1.1.4. The domain ToARG is defined in clause F3.2.1.1.1.

## F3.2.1.1.4 Reachability

When signals are sent, it has to be determined whether there currently is an applicable communication path: a path consisting of a sequence of links that can transfer the signal, and that satisfies further constraints as specified by the optional to- and via-arguments. The predicate applicable formally states all conditions that must be satisfied.

```
applicable(s: SIGNAL, toArg: [ ToARG ], viaArg: VIAARG, \(g:\) GATE, \(l:\left[\right.\) LINK ]): BOOLEAN \(=_{\text {def }}\)
    \(\exists\) commPath \(\in\) allConnections \((g)\) :
            \((\forall l l \in\) commPath \(: s \in l l . w i t h \wedge l l . o w n e r ~ \neq\) undefined \() \wedge\)
            if commPath = empty then
                \(l=\) undefined \(\wedge((\) g.direction \(=\) outDir \() \Rightarrow\)
```

```
                (toArg = undefined }\wedges\ing.gateAS1.s-Out-signal-identifier-set)) ^
            ((g.direction = inDir ) = (validDestinationGate (g,toArg) ^ // to self
                s}\ing.gateAS1.s-In-signal-identifier-set)) ^ viaArg = \varnothing
            else
                if l\not= undefined then commPath.head =l else true endif ^
                \neg \exists l l \in L I N K : ( l l . f r o m ~ = ~ c o m m P a t h . l a s t . t o ~ \wedge ~ s \in l l . w i t h ) ~ \wedge ~ / / ~ t h e ~ p a t h ~ i s ~ c o m p l e t e
                viaArg \subseteqcommPath.commPathIds ^ validDestinationGate(commPath.last.to,toArg)
            endif
validDestinationGate(g: GATE,toArg: [ ToARG ]): BOOLEAN =def
        if toArg \in Agent-identifier then
            g.myAgent.agentAS1.identifier }\mp@subsup{}{1}{}=\mathrm{ toArg else true endif ^
        if toArg \in PID ^ toArg # nullPid then
            \existssa AGENT: (sa.owner = g.myAgent }\wedge\mathrm{ sa.selfPid = toArg) else true
        endif
allConnections(g:GATE): LINKSEQ-set = def
    U({{<l\rangle\frown list |list \in allConnections(l.to) } |l\inLINK: l.from =g }) \cup
    { empty }
commPathIds(lSeq: LINK*): Identifier-set = def
    { g.gateASl.identifier }|\mp@code{g}\in\mathrm{ GATE: }\existsl\inl\mathrm{ Seq: (g=l.from }\veeg=l.to) }
    { l.agentAS1.identifier }|l\in\mp@subsup{\mathrm{ LINK: }}{l}{}(l\inl\mathrm{ lSeq) }
```


## F3.2.1.1.5 Timers

A particular concise way of modelling timers is by identifying timer objects with respective timer signals. More precisely, each active timer is represented by a corresponding timer signal in the schedule associated with the input port of the related process instance.

```
TIMER = def Identifier
TIMERINST = def PID }\times\mathrm{ TIMER }\times\mathrm{ VALUE*
```

The information associated with timers is accessed using the functions defined on SIGNAL.

## Active timers

To indicate whether a timer instance $t m i$ is active or not, there is a corresponding derived predicate active:
active(tmi:TIMERINST): BOOLEAN $=_{\text {def }}$ tmi $\in$ Self.inport.schedule

## Timer operations

The macros below model the SDL-2010 actions Set-node and Reset-node on timers as executed by a corresponding SDL-2010 agent. A static function (duration) is used to represent default duration values as defined by an SDL-2010 specification under consideration.

```
static duration: TIMER }->\mathrm{ DURATION
SetTimer(tm:Timer,vSeq :VALUE*,t:[TIME]) \equiv
    let tmi=mk-TIMERINST(Self.selfPid,tm,vSeq ) in
        if }t=\mathrm{ undefined then
            Self.inport.schedule := insert(tmi, now + tm.duration,delete(tmi, Self.inport.schedule))
            tmi.arrival := now + tm.duration
        else
            Self.inport.schedule := insert(tmi, t, delete(tmi, Self.inport.schedule))
            tmi.arrival := t
        endif
    endlet
```

```
RESETTIMER(tm:TIMER, vSeq :VALUE*) \equiv
    let tmi=mk-TIMERInST(Self.selfPid,tm,vSeq ) in
        if active(tmi) then
            DELETE(tmi, Self.inport)
        endif
    endlet
```


## F3.2.1.1.6 Exceptions

Exceptions are identified dynamic conditions. How the system behaves when an exception occurs, is not defined by SDL-2010. Each kind of exception has an identity that can be used in the implementation to report or to handle the exception. The raise function (see clause F3.3.1.1) is called for the dynamic conditions under which an exception occurs with the exception as a parameter. As the further behaviour is undefined when an exception occurs, it is preferable if the SDL-2010 is written to prevent the dynamic conditions arising (for example, checking on indexing bounds).

```
ExCEPTION = def Exception-identifier
```


## F3.2.1.2 SDL-2010 agents

In this clause, the domain AGENT is further refined to consist of three basically different types of agents, namely: link agent instances (modelled by the domain LINK, see clause F3.2.1.1.3), SDL-2010 agent instances, and SDL-2010 agent set instances (modelled by the derived domains SDLAGENT and SDLAGENTSET, respectively).

```
SDLAGENT = def AGENT
SDLAGENTSET = def AGENT
```

Initially, there is only a single agent system denoting a distinguished SDL-2010 agent set instance of the domain SdLAGENTSET.

```
static system: }->\mathrm{ SDLAGENTSET
    initially AGENT = { system }
```


## F3.2.1.2.1 State machine

The structure of the agent's state machine is directly modelled, and built up during the agent initialization. To represent the structure formally, several domains and functions are used. The state machine structure is exploited in the execution phase, when transitions are selected, and states entered and left.

```
controlled domain STATENODE
    initially \(\operatorname{STATENODE}=\varnothing\)
```

The StateNode domain is modified in clause F3.2.3.1 to contain entries for each basic node or composite state type in the system.

```
STATENODEKIND = def { stateNode, statePartition, procedureNode}
STATENODEREFINEMENTKIND = def { compositeStateGraph, stateAggregationNode}
STATEENTRyPoINT = def [ State-entry-point-name ]
STATEEXITPOINT = def State-exit-point-name }\cup\mathrm{ DEFAULT
StateNodEWITHENTRyPoInT = def STATENODE }\times(\mathrm{ STATEENTRyPoINT }\cup\mathrm{ HISTORY)
StateNodeWithExitPoint = def StateNode \times StateExitPoint
STATENODEWITHCONNECTOR = def STATENODE }\times\mathrm{ Connector-name
```

The first group of declarations and definitions introduces a controlled domain STATENODE, and a number of derived domains.

[^1]```
controlled stateName: STATENODE -> State-name
controlled stateId: STATENODE }->\mathrm{ STATEID
controlled inheritedStateNode: STATENode }->\mathrm{ [STATENODE]
controlled parentStateNode: STATENODE -> [STATENODE]
controlled stateTransitions: STATENODE }->\mathrm{ SEMTRANSITION-set
controlled startTransitions: STATENODE -> STARTTRANSITION-set
controlled freeActions: STATENODE -> FREEACTION-set
controlled statePartitionSet: STATENODE }->\mathrm{ STATENODE-set
```

The stateNodeRefinement of a StateNode for a basic state is undefined.
The parentStateNode of a StateNode is either undefined for a basic state, or the StateNode for the composite state type of a composite state node, or undefined or the super type for a composite state type.

The inheritedStateNode of a STATENODE is either undefined for a basic state or an unspecialized composite state, or one of the specializations a composite state type.

The second group of declarations introduces controlled functions defined on the domain STATENODE, they can be understood as a state node control block and are used to model the state machine by a hierarchical inheritance state graph.
controlled currentSubStates: StateNode $\rightarrow$ StateNode-set
controlled previousSubStates: StateNode $\rightarrow$ StateNode-set
The currentSubStates function defines, for each state node, the current substates. If the state node is refined into a composite state graph, this is at most one substate. In case of a state aggregation node, this is a subset of the state partition set.

The previousSubStates function gives the set of state nodes to use when a composite state with HISTORY is re-entered.

```
collectCurrentSubStates(sn: STATENODE): STATENODE-set \(=_{\text {def }}\)
    \(\{s n\} \cup \mathbf{U}(\{\) collectCurrentSubStates \((x) \mid x \in\) sn.currentSubStates \(\cup\) sn.inheritedStateNodes \(\})\)
```

The collectCurrentSubStates function collects, for a given state node, all current substates.
controlled currentExitPoints: STATENODE $\rightarrow$ STATEEXITPOINT-set
The currentExitPoints function defines, for each state aggregation node, the current exit points: the exit points activated by exiting state partitions. The state aggregation is exited only if all state partitions have exited.

```
inheritsFrom(sn1: STATENODE, sn2: STATENODE): BOOLEAN = def
    if sn2.parentStateNode = undefined then false
        elseif snl.parentStateNode = undefined then false
        else
        sn2.parentStateNode \in sn1.parentStateNode.inheritedStateNodes ^
        sn1.stateName = sn2.stateName
        endif
```

The inheritsFrom predicate determines whether the composite state type of one state node (sn2) inherits the composite state type of another state node (snl).

```
directlyInheritsFrom(sn1: STATENODE, sn2: STATENODE): BOOLEAN = def
    inheritsFrom(sn1, sn2) ^
        ( }\neg\exists\mathrm{ snx }\in\mathrm{ STATENODE:
            inheritsFrom(sn1, snx)^ inheritsFrom(snx, sn2))
```

The directlyInheritsFrom predicate determines whether the composite state type of one state node (sn2) directly inherits (in one step) the composite state type of another state node (sn1).

```
directlyRefinedBy(sn1: STATENODE, sn2: STATENODE): BOOLEAN =def
    sn2.parentStateNode = sn1
```

The directlyRefinedBy predicate determines whether a state node is refined by another state node by a single refinement step.

```
directlyInheritsFromOrRefinedBy(sn1: STATENODE, sn2: STATENODE): BOOLEAN = def
    directlyRefinedBy(sn1, sn2) v directlyInheritsFrom(sn1, sn2)
```

The directlyInheritsFromOrRefinedBy predicate determines whether two state nodes are related by a sequence of refinement or inheritance steps.

```
inheritsFromOrRefinedBy(sn1: STATENODE, sn2: STATENODE): BOOLEAN =def
    directlyInheritsFromOrRefinedBy(sn1, sn2) \vee
            (\exists sn3 \in { sn \in STATENODE: directlyInheritsFromOrRefinedBy (snl, sn) }:
                (inheritsFromOrRefinedBy(sn3, sn2)))
```

The inheritsFromOrRefinedBy predicate determines whether snl inherits from or is refined by $s n 2$, taking transitivity of this relationship into account.

```
selectNextStateNode(snSet: STATENODE-set): [STATENODE] = def
    let sn = take({sn1 \in snSet: (\neg\existssn2 \in snSet: inheritsFromOrRefinedBy(sn1, sn2))}) in
        if }sn=\mathrm{ undefined then undefined
        elseif }\existssn1\insnSet:directlyInheritsFrom(sn1,sn)\veesn=sn1.inheritedStateNode then
            selectNextStateNode(snSet \{sn})
        else sn
        endif
    endlet
```

The selectNextStateNode function returns a state node that may be checked next, provided snSet is a valid set of current state nodes reduced by state nodes that have already been selected with this function.

```
inheritedStateNodes(sn: STATENODE): STATENODE-set =def
    if sn.inheritedStateNode = undefined then \varnothing
    else {sn.inheritedStateNode} \cup sn.inheritedStateNode.inheritedStateNodes
    endif
```

The inheritedStateNodes function defines, for a given state node, the set of inherited state nodes.

```
parentStateNodes(sn: STATENODE): STATENODE-set = def
    if sn.parentStateNode = undefined then }
    else {sn.parentStateNode} \cup sn.parentStateNode.parentStateNodes
    endif
```

The parentStateNodes function defines, for a given state node, the set of parent state nodes.

```
mostSpecialisedStateNode(sn:StateNODE): STATENODE = def
    let sn1 = take({sn2 \in STATENODE: inheritsFrom(sn2, sn)}) in
        if snl = undefined then sn else sn1.mostSpecialisedStateNode endif
    endlet
```

The mostSpecialisedStateNode function returns, for a given state node, the most specialized state node applied during the selection of transitions in order to obtain the correct sequence of state node checks.

```
selectInheritedStateNode(sn: STATENODE, snSet: STATENODE-set): [STATENODE ]= \({ }_{\text {def }}\)
    take (\{snl \(\in\) snSet: directlyInheritsFrom(sn,snl) \})
```

The selectInheritedStateNode function yields a state node that may be left next, provided snSet is a valid set of state nodes to be left.

```
getPreviousStatePartition(sn: STATENODE): STATENODE \(=_{\text {def }}\)
    if sn.stateNodeKind \(=\) statePartition \(\wedge\)
        \(\neg \exists\) sn1 \(\in\) sn.parentStateNodes: sn1.stateNodeKind \(=\) procedureNode
        then sn.mostSpecialisedStateNode
        else getPreviousStatePartition(sn.parentStateNode)
        endif
```

The getPreviousStatePartition function determines, for a given state node, the innermost state partition not belonging to a procedure.

```
controlled resultLabel: STATENODE -> LABEL
```

The resultLabel function refers to the location of the return value, if the state node is a procedure state node, i.e., a state node owning the procedure graph.
controlled callingProcedureNode: $($ AGENT $\cup$ STATENODE $) \rightarrow[$ STATENODE $]$
The callingProcedureNode function refers to the root node of the calling procedure, if any, and is associated with the state node owning the procedure graph. Thus, nested procedure calls are modelled.

```
controlled entryConnection: STATEENTRYPOINT × STATENODE }->\mathrm{ [STATEENTRYPoINT]
controlled exitConnection: StateExitPoinT × STATENODE }->\mathrm{ StateExitPoint
```

Finally, the entryConnection and exitConnection functions model the entry and exit connections of state nodes.

## F3.2.1.2.2 Agent modes

To model the dynamic semantics of agents, several activity phases are distinguished. These phases are modelled by a hierarchy of agent modes. At this point, the agent modes are formally introduced; their usage is explained in clause F3.2.3.

```
AGENTMODE = def {
    initialisation, // agent mode 1
    execution, // agent mode 1
    selectingTransition, // agent mode 2
    firingTransition, // agent mode 2
    stopping, // agent mode 2
    initialising1, // agent mode 2, 4
    initialising2, // agent mode 2
    initialisingStateMachine, // agent mode 2
    initialisingProcedureGraph, // agent mode 4
    initialisationFinished, // agent mode 2, 4
    startSelection, // agent mode 3
    selectFreeAction, // agent mode 3
    selectExitTransition, // agent mode 3
    selectStartTransition, // agent mode 3
    selectPriorityInput, // agent mode 3
    selectInput, // agent mode 3
    selectContinuous, // agent mode 3
    startPhase, // agent mode 2, 4
    selectionPhase, // agent mode 4,5
    evaluationPhase, // agent mode 4,5
    selectSpontaneous, // agent mode 4
    leavingStateNode, // agent mode 3
    firingAction, // agent mode 3, 4
    enteringStateNode, // agent mode 3
    exitingCompositeState,// agent mode 3
```

| initialisingProcedure, | // agent mode 3 |
| :--- | :--- |
| enterPhase, | // agent mode 4 |
| enteringFinished, | // agent mode 4 |
| leavePhase, | // agent mode 4 |
| leavingFinished $\}$ | // agent mode 4 |

The agent modes are grouped according to their usage and the level of the agent mode hierarchy where they are relevant. In cases no conflict arises, agent modes may be applied on more than one level of this hierarchy.

## F3.2.1.2.3 Agent control block

The state information of an SDL-2010 agent instance is collected in an agent control block. The agent control block is partially initialized when an SDL-2010 agent (set) instance is created, and completed/modified during its initialization and execution. Since part of the state information is valid only during certain activity phases, the agent control block is structured accordingly. Following is the state information needed in all phases. Further control blocks that form part of the agent control block, but are relevant during certain activity phases only, are defined subsequently.

```
controlled owner: AGENT \cupSTATENODE \cup LINK }->\mathrm{ [AGENT]
```

Hierarchical system structure is modelled by means of a function owner defined on agents, and on state nodes (see clause F3.2.1.2.1), expressing structural relations between them and their constituent components. More specifically, an agent set instance is considered as owner of all those agent instances currently contained in the set; an agent instance owns its substructure, consisting of agent set instances. Similarly, a composite state node owns the state nodes or state partitions forming the refinement.

```
controlled agentAS1: AGENT }->\mathrm{ Agent-definition
controlled channelAS1: AGENT }->\mathrm{ [Channel-definition]
controlled gateAS1: GATE }->\mathrm{ [Gate-definition]
controlled stateAS1: STATENODE }->\mathrm{ State-node
controlled procedureAS1: STATENODE }->\mathrm{ Procedure-definition
controlled stateDefinitionAS1: STATENODE }->\mathrm{ Composite-state-type-definition
controlled partitionAS1: STATENODE }->\mathrm{ [State-partition]
```

A series of unary functions (agentAS1 to partitionAS1, see above, defined on agents, gates and state nodes) identify the corresponding AST definition. These definitions are needed during the initialization phase and also during dynamic creation of agents.

```
isAgentSet(ag:AGENT): BOOLEAN = def ag.program = AGENT-SET-PROGRAM
```

To distinguish SDL-2010 agent sets from other agents, the predicate isAgentSet is defined.

```
controlled selfPid: SDLAGENT -> PID
controlled sender: SDLAGENT }->\mathrm{ PID
controlled parent: SDLAGENT -> [PID ]
controlled offspring: SDLAGENT }->\mathrm{ PID
```

The above functions model the corresponding Pid expressions introduced in ITU-T Z.101.
controlled state: SDLAGENT $\rightarrow$ STATE
The values of the variables of an agent are collected in a state associated with some agent, modelled by the function state. This function is changed dynamically whenever the variable values of an agent or a procedure change. The data semantics provides the initial value for this function via initAgentState and initProcedureState.
controlled stateAgent: SDLAGENT $\rightarrow$ SDLAGENT

The values of the variables of an SDL-2010 agent are normally associated with the agent. However, in case of nested process agents (i.e. process agents contained within a process agent), they are associated with the outermost process agent. The function stateAgent yields, for a given SDL-2010 agent, the SDL-2010 agent to which the variable values are associated.

```
controlled topStateId: SDLAGENT }->\mathrm{ STATEID
```

The topStateId function associates the outermost scope with an agent. In case of nested process agents, it is only defined for the outermost process agent.

```
controlled isActive: SDLAGENT }->\mathrm{ [SDLAGENT]
```

Nested process agents are to be executed in an interleaving manner. To model the required synchronization, the function isActive of the outermost process agent is used.

```
monitored spontaneous: AGENT \(\rightarrow\) BOOLEAN
```

The SDL-2010 concept of spontaneous transition is abstractly modelled by means of a monitored predicate spontaneous associated with a particular SDL-2010 agent instance, which serves for triggering spontaneous transition events. It is assumed that spontaneous transitions occur from time to time without being aware of any causal dependence on external conditions and events. This view reflects the indeterminate nature behind the concept of spontaneous transition.

```
controlled inport: SDLAGENT \(\rightarrow\) GATE
```

Each SDL-2010 agent instance has its local input port at which arriving signals are stored until these signals either are actively received, or until they are discarded. Input ports are modelled as a gate, containing a finite sequence of signals.

```
controlled currentSignalInst: SDLAGENT }->\mathrm{ [SIGNALINST]
```

During the firing of input transitions, the signal instance removed from the input port is available through the function currentSignalInst.
controlled topStateNode: SDLAGENT $\rightarrow$ STATENODE
The state nodes of an agent are rooted at a top state node modelling the state machine of the agent instance.
controlled currentStartNodes: SDLAGENT $\rightarrow$ STATENODEWITHENTRYPoINT-set
Start transitions take precedence over regular transitions; they are identified by tuples consisting of a state node and an entry point.
controlled currentExitStateNodes: SDLAGENT $\rightarrow$ STATENODEWITHExitPoint-set
Exit transitions take precedence over regular transitions; they are identified by tuples consisting of a state node and an exit point.
controlled currentConnector: SDLAGENT $\rightarrow$ [STATENODEWITHCONNECTOR]
Free actions take precedence over regular transitions; they are identified by tuples consisting of a state node and a connector name.

```
controlled scopeName: SDLAGENT \(\times\) STATEID \(\rightarrow\) Connector-name
controlled scopeContinueLabel: SDLAGENT \(\times\) STATEID \(\rightarrow\) ContinuELABEL
controlled scopeStepLabel: SDLAGENT \(\times\) STATEID \(\rightarrow\) STEPLABEL
```

The functions scopeName, scopeContinueLabel and scopeStepLabel are used for Compound-node interpretation (see Z.102).

## InitStateMachine/InitProcedureGraph control block

When the state machine of an agent is initialized, a hierarchical inheritance state graph is created. Because this normally takes several steps, the intermediate status of the creation is kept in an InitStateMachine/InitProcedureGraph control block. Based on this information, it is, for instance, possible to control the order of node creation as far as necessary. This control block is used during the initialization of the agent instance, and also dynamically when a procedure call occurs.

```
controlled stateNodesToBeCreated: SDLAGENT }->\mathrm{ State-node-set
controlled statePartitionsToBeCreated: SDLAGENT }->\mathrm{ State-partition-set
controlled stateNodesToBeRefined: SDLAGENT -> STATENODE-set
controlled stateNodesToBeSpecialised: SDLAGENT }->\mathrm{ STATENODE-set
```

In order to keep track of the state machine creation, a distinction is made between the state nodes and the state partitions to be created. Also, the refinement and specialization of state nodes is taken into account.

## Selection control block

During the selection of a transition, additional information is needed to keep track of the selection status. For instance, when the selection starts, the input port is "frozen", meaning that its state at the beginning of the selection is the basis for this selection cycle. This does not prevent signal instances arriving while the selection is active, but these signals are not considered before the next selection cycle.

```
controlled inputPortChecked: SDLAGENT \(\rightarrow\) SIGNALINST*
controlled stateNodesToBeChecked: SDLAGENT \(\rightarrow\) STATENODE-set
controlled stateNodeChecked: SDLAGENT \(\rightarrow\) [STATENODE]
controlled startNodeChecked: SdLAGENT \(\rightarrow\) STATENODEWITHENTRYPOINT
controlled exitNodeChecked: SDLAGENT \(\rightarrow\) StateNodeWithExitPoint
controlled transitionsToBeChecked: SDLAGENT \(\rightarrow\) SEMTRANSITION-set
controlled transitionChecked: SDLAGENT \(\rightarrow\) SEMTRANSITION
controlled signalChecked: SDLAGENT \(\rightarrow\) SIGNALINST
controlled SignalSaved: SDLAGENT \(\rightarrow\) BOOLEAN
controlled continuousPriorities: SDLAGENT \(\rightarrow\) NAT-set
```


## Enter/Leave/ExitStateNode control block

In general, to enter, leave or exit a state node requires a sequence of steps. In hierarchical state graphs, entering a state node means to enter contained states, and to execute start transitions and entry procedures. Likewise, leaving a state node means to leave the contained states and to execute exit procedures. Exiting a composite state in addition means to fire an exit transition. During these activity phases, the status information is maintained in the enter/leave/exitStateNode control block.

```
controlled stateNodesToBeEntered: SDLAGENT \(\rightarrow\) STATENODEWITHENTRYPoINT-set
controlled stateNodesToBeLeft: SDLAGENT \(\rightarrow\) STATENODE-set
controlled stateNodeToBeExited: SDLAGENT \(\rightarrow\) [STATENODEWITHExitPoint]
```


## Procedure control block

The procedure control block comprises the part of the agent control block that has to be stacked when a procedure call occurs. This includes the agent modes, the current action label, and the state identification. Once the procedure terminates, this state information has to be restored. The stacked information is associated with the state node containing the procedure graph. Such a state node is created dynamically for each procedure call.
During the execution of a procedure, other control blocks may be required, for instance, the InitStatemachine control block or the selection control block. However, the corresponding phases
do not lead to the execution of further procedures, and are not interrupted by other phases. Therefore, it is not necessary to stack these parts of the agent control block.

```
controlled agentModel: AGENT \cupSTATENODE }->\mathrm{ AGENTMODE
controlled agentMode2: AGENT \cupSTATENODE }->\mathrm{ AGENTMODE
controlled agentMode3: AGENT \cupSTATENODE }->\mathrm{ AGENTMODE
controlled agentMode4: AGENT \cupSTATENODE }->\mathrm{ AGENTMODE
controlled agentMode5: AGENT }\cup\mathrm{ STATENODE }->\mathrm{ AGENTMODE
```

To control the execution of agents, a control hierarchy is formed, which consists of up to five levels, depending on the current execution phase. For each of these levels, a specific function agentMode is defined.
controlled currentStateId: SdLAGENT $\cup$ StateNode $\rightarrow$ STATEID
In order to handle nested process agents and procedure calls, a state may contain substates. Every substate is given an identification at the time of its creation; for example, when a procedure is called or when a nested process agent is started. These identifications are taken from the domain STATEID. A STATE contains associations between a number of STATEID values, a number of variable identifiers, and their respective values.
controlled currentLabel: SDLAGENT $\cup$ STATENODE $\rightarrow$ [LABEL]
The currentLabel function, which identifies the action currently executed or to be executed next, controls the firing of transitions and the evaluation of expressions. When a sequence of steps is completed, currentLabel is set to undefined.
controlled continueLabel: SDLAGENT $\cup$ STATENODE $\rightarrow$ [CONTINUELABEL]
The continueLabel function is needed while a state node is left, which forms part of the firing of a transition and may lead to the execution of further action sequences. When the state node is left, firing of the transition is resumed. In particular, this value is needed when procedures are executed. Also, this function records the label where execution is continued after a procedure call.
controlled currentParentStateNode: SDLAGENT $\cup$ STATENODE $\rightarrow$ STATENODE
The currentParentStateNode function defines the correct ownership between state nodes, and identifies states to be left and to be entered.
controlled previousStateNode: SDLAGENT $\cup$ STATENODE $\rightarrow$ STATENODE
When a transition is fired, the previousStateNode function refers to the state node where the transition started.
controlled currentProcedureStateNode: SDLAGENT $\cup$ StateNode $\rightarrow$ StateNode
The currentProcedureStateNode function refers to the current procedure state node.

## F3.2.1.2.4 Agent connections

SDL-2010 agents are organized in agent sets. All members of an agent set have the same sets of input gates and output gates as defined for the agent set.

```
gateUnconnected(g:GATE):BOOLEAN = def
    let myDef: Agent-type-definition = g.myAgent.agentAS1.s-Agent-type-identifier.idToNodeAS1 in
        \forallcd \inmyDef.s-Channel-definition-set: }\forallcp\incd.s-Channel-path-set
            (g.gateASl # cp.s-Originating-gate.idToNodeAS1 ^
                g.gateASl # cp.s-Destination-gate.idToNodeAS1)
    endlet
```

The gateUnconnected is true if the gate is not linked to an inner gate by a channel path:

```
ingates(a: AGENT): GATE-set \(=_{\text {def }}\)
    if a.isAgentSet then
            \(\{g \in\) GATE: \(g\). myAgent \(=a \wedge\) g.direction \(=\) inDir \(\wedge\) g.gateUnconnected \(\}\)
        else
            a.owner.ingates
        endif
outgates(a:AGENT): GATE-set \(=_{\text {def }}\)
    if a.isAgentSet then
        \(\{g \in\) GATE: g.myAgent \(=a \wedge\) g.direction \(=\) outDir \(\wedge\) g.gateUnconnected \(\}\)
    else
        a.owner.outgates
    endif
```

The derived function ingates and outgates collect all input gates and all output gates of an agent. Input gates (output gates) are gates of an agent set or agent with direction inDir (outDir) that are not connected to inner gates by a channel path.

## F3.2.1.2.5 Agent behaviour

For the transitions of agents, a tuple domain is introduced, consisting of the signal type, the start label for any firing conditions, a priority value, and the start label of the transition actions. Additionally, state exit points may be given. Depending on the kind of transition, some of these components may be unspecified. For instance, in case of an input transition, there is no firing transition and no priority.

```
SEMTRANSITION= = def SIGNAL }\times[LABEL]\times[NAT]\timesLABEL ×[STATEEXITPOINT 
STARTTRANSITION = def LABEL }\times\mathrm{ STATEENTRYPOINT
FREEACTION = = def Connector-name }\times\mathrm{ LABEL
```

Given a set of transitions, several derived functions are defined to select particular subsets:

```
priorityInputTransitions(tSet:SEMTRANSITION-set): SEMTRANSITION-set = def
    {t\intSet: t.\mathbf{S}-SIGNAL}\not=\mathbf{NONE}\wedget.\mathbf{s}-LABEL= undefined \wedget.\mathbf{S}-NAT\not= undefined 
inputTransitions(tSet:SEMTRANSITION-set): SEMTRANSITION-set =def
    {t\intSet:t.s-SIGNAL # NONE ^t.s-NAT = undefined }
continuousSignalTransitions(tSet:SEMTRANSITION-set): SEMTRANSITION-set = def
    {t\intSet: t.S-SIGNAL = NONE ^t.s-LABEL }\not=\mathrm{ undefined }\wedget.\mathbf{s}-NAT\not= undefined 
spontaneousTransitions(tSet:SEMTRANSITION-set): SEMTRANSITION-set =def
    {t\intSet: t.s-SIGNAL = NONE ^t.s-NAT = undefined }\wedget.s-STATEExITPOINT = undefined 
exitTransitions(tSet:SEMTRANSITION-set): SEMTRANSITION-set = def
    {t\intSet:t.s-STATEEXITPOINT # undefined }
```


## F3.2.1.3 Interface to the data type part

The semantics of the data type part of SDL-2010 is handled separately from the concurrency related aspects of the language. To make this splitting possible, an interface for the semantics definition is defined.
NOTE - The data type part does not include the REF Aggregation-kind for reference variables defined in SDL-2010, and therefore is inconsistent with SDL-2010. Further work needs to be done to update the data part for reference variables defined in SDL-2010.

## F3.2.1.3.1 Functions provided by the data type part

The data interface is grouped around a derived domain State. This domain is abstract from the concurrency side, and concrete from the data type side. It represents the values of the variables of an
agent, which are collected in the outermost process agent. This is achieved by a dynamic, controlled function state defined on process instances (see clause F3.2.1.2.3).
derived domain STATE
The function state is changed dynamically whenever the state of a process or a procedure changes. It is solely used within the concurrency semantics part. The data type semantics part provides the initial value for the state function via the functions initAgentState and initProcedureState. In order to handle recursion, a state might contain substates. Every substate is given an identification at the time of its creation; for example, when a procedure is called or when a nested process agent is started. These identifications are in the domain StateId. A State contains associations between a number of STATEID values, a number of variable identifiers, and their respective values.
The parameters of initAgentState are:

- State of the outermost process agent (undefined if the outermost process agent is being created)
- $\quad$ State ID of the new state
- State ID of the super state of the new state (undefined for the outermost agent)
- Declarations of the agent

The additional parameter for initProcedureState is

- List of parameter values and variable names
controlled domain STATEID
DECLARATION $=_{\text {def }}$ Procedure-formal-parameter $\cup$ Variable-definition
initAgentState: $[$ STATE $] \times$ StateID $\times[$ STATEID $] \times$ DECLARATION-set $\rightarrow$ State
initProcedureState: State $\times$ StateId $\times$ StateId $\times$ DEClaration-set $\times$ DECLARATION* $^{*} \times$ VALUE $^{*} \times$ Variableidentifier $^{*} \rightarrow$ STATE

The domain Declaration is used to create lists of variables for a state. Positional parameters are guaranteed to come first in this list.
There is also a domain for values, called VALUE.

$$
\begin{aligned}
V A L U E= & \text { def } \\
S D L I N T E G E R \cup S D L B O O L E A N & \cup S D L R E A L \cup S D L C H A R A C T E R \cup S D L S T R I N G \\
& \cup P I D \cup S D L L I T E R A L S \cup S D L S T R U C T U R E \cup S D L A R R A Y \cup S D L P O W E R S E T \\
& \cup S D L B A G \cup S D L T I M E \cup S D L D U R A T I O N
\end{aligned}
$$

Some operations invoked in the data part may raise an exception. In SDL-2010 there is no definition of the handling of exceptions, so that if one occurs the further behaviour of the system is not defined. Therefore, if an exception occurs in the operation the termination is not defined, so the formal semantics is only given for the case of termination without an exception. The possibility of the operation raising an exception is shown by the return being in one of the following domains:

```
STATEOREXCEPTION = def STATE \cup EXCEPTION
VALUEOREXCEPTION = def VALUE \cup EXCEPTION
```

The data type part has to provide functions that model how assignments are performed, namely

[^2]The function eval (see below) retrieves the value associated with a variable for a given state and state id. The function assign associates a new value with a given variable. There is an ASSIGN rule macro using this function, which is doing the real assignment.

> ASSIGN(variableName: Variable-identifier, value: VALUE, state: STATE, id: STATEID) $\equiv$
> Self.stateAgent.state:= assign(variableName, value, state, id)

Assignments are the only way to change the state.
In order to get the current value of a variable, the data part provides the function eval to get it. It returns undefined if the variable is not set.

```
eval:Variable-identifier }\times\mathrm{ STATE }\times\mathrm{ STATEID }->\mathrm{ VALUE
```

The semantics of these functions is given by the data semantics part.
In order to handle expressions, the concurrent semantics provides a domain for procedure bodies, which is also used for method and operator bodies. The data part, in return, provides a static domain PROCEDURE for procedures (definitions) and a function dispatch for procedure instances.

PROCEDURE $=_{\text {def }}$ Static-operation-signature $\cup$ Literal-signature
For modelling the dynamic dispatch, a dispatch function is provided by the data part.

```
dispatch: PROCEDURE }\times\mathrm{ VALUE* }->\mathrm{ Identifier
```

Finally, there are two functions to model the predefined functions that do not have a procedure body because they are part of the predefined data. There is one function to check if the procedure is functional (predefined), and one function to compute the result in this case.
functional: PROCEDURE $\times$ VALUE* $\rightarrow$ BOOLEAN
compute: PROCEDURE $\times$ VALUE* $\rightarrow$ VALUEOREXCEPTION
Moreover, the following domains and functions referring to the Predefined data are used.
derived domain SDLBOOLEAN
derived domain SDLINTEGER
derived semvalueBool: SDLBOOLEAN $\rightarrow$ BOOLEAN
derived semvalueInt: SDLINTEGER $\rightarrow$ NAT
derived semvalueRealNum: SDLREAL $\rightarrow$ NAT
derived semvalueRealDen: SDLREAL $\rightarrow$ NAT
derived semvalueReal: SDLREAL $\rightarrow$ REAL

## F3.2.1.3.2 Functions used by the data type part

The following special points are worth noting:

- If two processes have part of their state in common (which could be possible due to the reference nature of the new data type part), there are no semantic problems in the concurrency part, as all state changes are automatically synchronized by the underlying ASM semantics.
- The values for the predefined variables of a process such as SENDER, PARENT, OFFSPRING, SELF, as well as the value of NOW are provided by the concurrency part.


## F3.2.1.4 Behaviour primitives

This clause describes the SAM behaviour primitives and how these primitives are evaluated. It describes how actions are evaluated, and gives for each primitive a short explanation of its intended meaning. Together with the domains, functions and macros that are used to define the behaviour of a primitive, an informal description of the intended meaning is provided as well. Additional reference clauses for further explanations complement the description of behaviour primitives.

The result of the compilation is accessible through the function behaviour. This function is static to reflect the fact that SAM code cannot be modified during execution.

```
STARTLABEL = def LABEL
BEHAVIOUR = def PRIMITIVE-set
PRIMITIVE = def LABEL }\times\mathrm{ ACTION
```

The behaviour consists of a start label and label-action pairs. The label is used to uniquely identify the action and to represent the current state of the interpretation.

## F3.2.1.4.1 Action evaluation

## Explanation

Action evaluation is used within the execution phase of agents. Primitives are attached to labels. The function currentLabel determines for each agent an action to be evaluated next. Actions have different types. For example, there exists, beside others, a primitive for the evaluation of variables and one for procedure calls. The evaluation of an action first determines the type of an action and then, depending of this type, fires an appropriate rule.

## Representation

The domain ACTION is defined as disjoint union of derived domains, which are explained in the subsequent clauses. For example, there exists a domain VAR that contains actions for the evaluation of variables.

```
ACTION = def VAR \cup OPERATIONAPPLICATION }\cup\mathrm{ CALL }\cup\mathrm{ RETURN }\cupTASK \cup ASSIGNPARAMETERS \cup EQUALITY \cup
```



```
SETRANGECHECKVALUE }\cupSCOPE \cupSKIP\cupBREAK \cupCONTINUE \cup ENTERSTATENODE \cup LEAVESTATENODE
```


## Domains

During the execution phase and the evaluation of actions we use labels basically in two ways: as jumps (continue labels) for modelling the corresponding control flow and as stores (value labels) for intermediate results. For example, intermediate results arise during the evaluation of expressions. A domain Continuelabel represents labels where an agent continues execution after completing an action. A domain VALUELABEL represents labels at which an agent can write or read values.

```
CONTINUELABEL = def LABEL
VALUELABEL = def LABEL
```


## Functions

Values stored at value labels can be accessed by a dynamic controlled function value and a dynamic derived function values.

```
controlled value: VALUELABEL }\times\mathrm{ SDLAGENT }->\mathrm{ VALUE
values(lSeq:VALUELABEL*, sa: SDLAGENT):VALUE* = def
    if lSeq = empty then empty
    else <value(lSeq.head,sa)> `values(lSeq.tail,sa)
    endif
```



Figure F3-2 - Agents, labels and values
In Figure 3-2 there are two agents, $a$ and $b$. The label of agent $a$, which determines the next action to be evaluated within the execution phase, is $k$. Agent $a$ has stored value 4 at label $m$, whereas Agent $b$ has a stored value 2 at the same label. In this way, different agents can write different values to the same label.

## Behaviour

The evaluation of an action is defined by macro Eval. Macro Eval takes as argument an action and depending on the type of this action a specific macro is called. These macros are explained in the subsequent clauses. The subdomains of ACTION are pairwise disjoint.

```
EVAL(a:ACTION) \equiv
    if }a\in\operatorname{VAR}\mathrm{ then EVALVAR(a)
    elseif }a\in\mathrm{ OPERATIONAPPLICATION then EvALOPERATIONAPPLICATION(a)
    elseif a\inCALL then EvalCALL(a)
    elseif }a\in\mathrm{ RETURN then EvalREtURN(a)
    elseif }a\in\mathrm{ TASK then EvalTASK(a)
    elseif a ASSIGNPARAMETERS then EvALASSIGNPARAMETERS(a)
    elseif }a\in\mathrm{ EQuality then EvalEQuality(a)
    elseif }a\in\mathrm{ DECISION then EvALDECISION(a)
    elseif }a\in\mathrm{ OUTPUt then EvalOUTPut(a)
    elseif a\inCreate then EvalCreate(a)
    elseif }a\inSET\mathrm{ then EvalSet(a)
    elseif a\inRESET then EvalReset(a)
    elseif }a\in\mathrm{ TimERActivE then EvalTimerActive(a)
    elseif }a\inSTOP then EVALSTOP(a
    elseif }a\in\mathrm{ SystemValue then EvalSystemValue(a)
    elseif }a\in\mathrm{ ANYVALUE then EvalANYVAlUE(a)
    elseif }a\in\mathrm{ SEtRANGECHECKVALUE then EvalSETRANGECHECKVALUE(a)
    elseif }a\inSCOPE then EvalSCOPE(a
    elseif }a\in\mp@subsup{S}{KIP}{\prime}\mathrm{ then EvalSKIP(a)
    elseif a\inBREAK then EvalBreak(a)
    elseif }a\in\mathrm{ Continue then EvalContinue(a)
    elseif }a\in\mathrm{ EnterStateNode then EvalEnterStateNode(a)
    elseif a\inLEAveStateNode then EvalLeaveStateNode(a)
    endif
```


## F3.2.1.4.2 Primitive Var

## Explanation

The Var primitive models the evaluation of a variable. It is used within the evaluation of expressions. An action of type $V A R$ is a tuple consisting of a variable name and a so-called continue label. The macro EvalVar evaluates the given variable within the state of the executing agent and writes this value at the current label of this agent. In this way the result of the evaluation can be used in consecutive execution steps of this agent.

## Representation

The domain VAR is defined as a Cartesian product of the domain Variable-identifier of variable names and domain ContinueLabel of labels.

```
VAR \(=_{\text {def }}\) Variable-identifier \(\times\) CONTINUELABEL
```


## Behaviour

If the value of a variable in the current state of the executing agent is undefined, the UndefinedVariable exception is raised. Otherwise the value of a variable in the current state of the executing agent is determined by function eval and is written at Self.currentLabel. In order to avoid conflicts with other agents, the function value takes a further argument of type AGENT, which identifies the owner of the value. Additionally, the label which determines the next rule to be fired is set to the given continue label.

```
EVALVAR (a:VAR) \equiv
    if eval(a.s-Variable-identifier,Self.stateAgent.state,Self.currentStateId) = undefined then
        raise(UndefinedVariable)
    else
        value(Self.currentLabel, Self) := eval(a.s-Variable-identifier,
            Self.stateAgent.state, Self.currentStateId)
        Self.currentLabel := a.s-CONTINUELABEL
    endif
```


## Reference sections

For the definition of function value refer to clause F3.2.1.4.1. The definition of function eval can be found in clause F3.2.1.3.1. Function currentLabel is defined in clause F3.2.1.2.3.

## F3.2.1.4.3 Primitive OperationApplication

## Explanation

The OperationApplication primitive models the application of operators. Procedures without procedure body are called functional or predefined procedures. In this sense, all built-in operators such as,+- on the set of integers are predefined procedures. A predefined procedure is executed by function compute: a non-functional operation, which is handled with function dispatch that determines (depending on the current values) the correct procedure identifier.

## Representation

OPERATIONAPPLICATION $=$ def PROCEDURE $\times$ VALUELABEL $* \times$ CONTINUELABEL

## Behaviour

EvalOPerationApplication (a:OPERATIONAPPLICATION) $\equiv$
if functional(a.s-PROCEDURE, values(a.s-VALUELABEL-seq, Self)) then value(Self.currentLabel, Self):= compute(a.s-PROCEDURE, values(a.s-VALUELABEL-seq, Self)) Self.currentLabel:=a.s-CONTINUELABEL
else

```
    let pd: Procedure-definition = idToNodeASl(
        dispatch(a.s-PROCEDURE, values(a.s-VALUELABEL-seq, Self))) in
        CreateProcedure(pd, Self.currentLabel, a.s-ContinueLabel)
    endlet
endif
```


## Reference sections

For the definition of function value refer to clause F3.2.1.4.1. The definition of predicate functional and the definition of function compute can be found in clause F3.2.1.3.1.

## F3.2.1.4.4 Primitive Call

## Explanation

The call primitive models procedure calls, or method invocations. It is used within the evaluation of expressions and actions. An action of type CALL is defined as a tuple consisting of an identifier of the called procedure, a sequence of value labels and variable identifiers, and a continue label. Inparameters are represented by value labels, in/out-parameters by variable identifiers. The macro EvalCall creates a new context (e.g., new local scope for variables, for names of its states and connectors) and saves the old context, which in turn is restored by the corresponding return.

## Representation

An action of type CALL is defined as a tuple consisting of an identifier of the called procedure, a sequence of value labels and variable identifiers, and a continue label. In-parameters are represented by value labels, in/out-parameters by variable identifiers.

$$
\text { CALLPARAM }=_{\text {def }} \text { VALUELABEL } \cup \text { Variable-identifier }
$$

$$
\text { CALL }=_{\text {def }} \text { Procedure-identifier } \times \text { CALLPARAM } \times \text { VALUELABEL } \times \text { CONTINUELABEL }
$$

## Behaviour

```
EVALCALL}(a:CALL)
    let pd: Procedure-definition = a.s-Procedure-identifier.idToNodeASl in
        CreateProcedure(pd, a.s-VALUELABEL, a.s-CoNTINUELABEL)
    endlet
```

A procedure call is evaluated with macro CREATEPROCEDURE, which basically performs a procedure initialization and additionally creates a procedure state node.

```
SAvEProcedureControlBLOCK(sn:STATENODE, cl:CONTINUELABEL) \equiv
    sn.agentMode1 := Self.agentModel
    sn.agentMode2 := Self.agentMode2
    sn.agentMode3 := Self.agentMode3
    sn.agentMode4 := Self.agentMode4
    sn.agentMode5 := Self.agentMode5
    sn.currentStateId := Self.currentStateId
    sn.currentLabel := Self.currentLabel
    sn.continueLabel:= cl
    sn.currentParentStateNode := Self.currentParentStateNode
    sn.previousStateNode := Self.previousStateNode
    sn.callingProcedureNode := Self.callingProcedureNode
```

The parameter passing mechanism is realized by function initProcedureState. This function returns a state, which contains Self.state as a substate. Furthermore, for all local and in-parameters initProcedureState "creates" new locations. In-parameters are initialized with values stored in resultLabel. Formal inout-parameters are unified with the corresponding actual inout-parameters.

## Reference sections

For the definition of macro CreateProcedure refer to clause F3.2.3.1.4. Information on procedure control blocks is given in clause F3.2.1.2.3.

## F3.2.1.4.5 Primitive Return

## Explanation

The Return primitive is used to model a procedure, method or operator return, or the exit of a composite state. In case of a procedure, method or operator return, it basically restores the old context (e.g., local scope for names of its states and connectors) of the corresponding call. Since procedures can return values, an action of type RETURN is modelled by a value label. The return value of the procedure is stored at this label. In case of an exit, the state exit point name is given.

## Representation

$$
\text { RETURN }=_{\text {def }}() \times(\text { VALUELABEL } \cup \text { STATEEXITPoINT })
$$

## Behaviour

```
EvALRETURN(a: RETURN) \equiv
    if a.s-implicit \in VALUELABEL then
            EVALEXITPROCEDURE(a.s-implicit )
        else
            EvaLEXITCOMPOSITESTATE(a.s-implicit)
        endif
EVALEXITPROCEDURE(vl: VALUELABEL) \equiv
    value(Self.callingProcedureNode.resultLabel, Self) := value(vl, Self)
    RESTOREPROCEDURECONTROLBLOCK(Self.callingProcedureNode)
EvalExitCompositeState(sep: STATEExitPoint) \equiv
    Self.stateNodeToBeExited :=
        mk-STATENODEWITHEXITPoinT(Self.currentParentStateNode, sep)
    Self.agentMode3 := exitingCompositeState
RESTOREPROCEDURECONTROLBLOCK(sn:STATENODE) \equiv
    Self.agentModel := sn.agentMode1
    Self.agentMode2 := sn.agentMode2
    Self.agentMode3 := sn.agentMode3
    Self.agentMode4 := sn.agentMode4
    Self.agentMode5 := sn.agentMode5
    Self.currentStateId := sn.currentStateId
    Self.currentLabel := sn.continueLabel
    Self.continueLabel := sn.continueLabel
    Self.currentParentStateNode := sn.currentParentStateNode
    Self.previousStateNode := sn.previousStateNode
    Self.callingProcedureNode := sn.callingProcedureNode
```


## Reference sections

Information on procedure control blocks is given in clause F3.2.1.2.3.

## F3.2.1.4.6 Primitive Task

## Explanation

The Task primitive is used for the evaluation of assignments. An action of type TASK is defined as a tuple consisting of a variable name, a value label and a continue label. The variable name becomes as value within the state of the executing agent the value stored at value label.

## Representation

An action of type TASK is defined as a tuple consisting of a variable name, a value label and a continue label.

$$
\text { TASK }^{\operatorname{def}} \text { Variable-identifier } \times \text { VALUELABEL } \times \text { BOOLEAN } \times \text { CONTINUELABEL }
$$

## Behaviour

The assignment is mainly realized by means of macro ASSIGN. Within the state of the executing agent the corresponding variable is set to the value stored at value label.

## $\operatorname{EVALTASK}(a: T A S K) \equiv$

Assign(a.s-Variable-identifier, value(a.s-VALUELABEL, Self), Self.stateAgent.state, Self.currentStateId)
Self.currentLabel :=a.s-ContinuELABEL

## Reference Sections

The definition of macro ASSIGN can be found in clause F3.2.1.3.1.

## F3.2.1.4.7 Primitive AssignParameters

## Explanation

The AssignParameters primitive is used for the assignments of parameters. An action of type ASSIGNPARAMETERS is defined as a tuple consisting of a variable identifier, a natural number, and a continue label.

## Representation

An action of type ASSIGNPARAMETERS is defined as a tuple consisting of a variable identifier, a natural number, and a continue label.

$$
\text { ASSIGNPARAMETERS }=_{\text {def }} \text { Variable-identifier } \times \text { NAT } \times \text { CONTINUELABEL }
$$

## Behaviour

```
EvALASSIGNPARAMETERS(a:ASSIGNPARAMETERS) \equiv
    let v=Self.currentSignalInst.plainSignalValues[a.s-NAT] in
        ASSIGN(a.s-Variable-identifier,v, Self.stateAgent.state, Self.currentStateId)
    endlet
    Self.currentLabel := a.s-CoNTINUELABEL
```


## Reference sections

The definition of macro ASSIGN can be found in clause F3.2.1.3.1.

## F3.2.1.4.8 Primitive Equality

## Explanation

The Equality primitive is used for the evaluation of equality tests. An action of type EQUALITY is defined as a tuple consisting of two value labels and a continue label. The values associated with these labels are compared. The result is stored at continue label.

## Representation

$E Q U A L I T Y={ }_{\text {def }}$ VALUELABEL $\times$ VALUELABEL $\times$ CONTINUELABEL

## Behaviour

```
    value(a.s-ConTINUELABEL,Self) := mk-SDLBoolEAN(true, BooleanType)
else
    value(a.s-ConTINUELABEL,Self) := mk-SDLBooLEAN(false, BooleanType)
endif
Self.currentLabel := a.s-CoNTINUELABEL
```


## Reference sections

No references.

## F3.2.1.4.9 Primitive Decision

## Explanation

The Decision primitive is used for the evaluation of decisions. A decision in DECISION consists of a value label and a set of answer. An answer in ANSWER is a tuple consisting of a value label and a continue label. The action itself chooses an answer such that the decision-value given by the corresponding value label coincides with the answer-value.

## Representation

A decision in DECISION consists of a value label and a set of answer. An answer in ANSWER is a tuple consisting of a value label and a continue label.

```
DECISION = def VALUELABEL }\times\mathrm{ ANSWER-set }\times[\mathrm{ [CONTINUELABEL]
ANSWER = def VALUELABEL }\times\mathrm{ CONTINUELABEL
```


## Behaviour

Macro EvalDecision chooses an answer such that the decision-value given by the corresponding value label coincides with the answer-value.

```
EvALDECISION(d:DECISION) \equiv
    if value(d.s-VALUELABEL,Self) }\in{\mathrm{ value(an.s-VALUELABEL,Self) |an |d.s-ANSWER-set } then
        choose an: an \ind.s-ANSWER-set ^
            value(d.s-VALUELABEL,Self) = value(an.s-VALUELABEL,Self)
        Self.currentLabel := an.s-CoNTINUELABEL
        endchoose
    elseif d.s-CONTINUELABEL }=\mathrm{ undefined then
        Self.currentLabel := d.s-CONTINUELABEL
    else raise(NoMatchingAnswer)
    endif
```


## Reference sections

For the definition of function value refer to clause F3.2.1.4.1.

## F3.2.1.4.10 Primitive Output

## Explanation

The Output primitive is used for expressing a signal output. An action of type OUTPUT consists of a signal, a sequence of value labels, an argument specifying the destination, an argument specifying a path, and a continue label.

## Representation

An action of type OUTPUT consists of a signal type, a sequence of value labels, an argument specifying the destination, an argument specifying a path, and a continue label.

```
OUTPUT = def SIGNAL }\times\mp@subsup{V}{\mathrm{ VALUELABEL* }}{}\times[VALUELABEL] ` VIAARG × CONTINUELABEL
```


## Behaviour

Macro EvalOutput defines signal output by macro SignalOutput, which takes the signal, a value sequence, the destination and the path as arguments.

```
EVALOUTPUT(a:OUTPUT) \equiv
    SignalOutput(a.s-SIGNAL, values(a.s-VALUELABEL-seq, Self),
            if a.s-VALUELABEL = undefined then undefined else value(a.s-VALUELABEL,Self) endif,
        a.s-VIAARG)
    Self.currentLabel := a.s-CoNTINUELABEL
```

A signal output operation causes the creation of a new signal instance. The process instance initiating the output operation identifies itself as sender of the signal instance by setting a corresponding function signalSender defined on signals. In general, there may be none, one or more output gates of a process to which a signal can be delivered depending on the specified constraints on

- possible destinations,
- potential receivers and
- admissible paths,
as stated by the values of TOARG and $\operatorname{VIAARG}$, which are obtained as parameters of an output operation and are assigned to a signal by setting corresponding functions defined on signals. Possible ambiguities are resolved by a non-deterministic choice for a gate that is connected to a path being compatible with ToArg, ViaArg. In the rule below, this choice is stated in abstract terms using the predicate applicable (cf. clause F3.2.1.1.4). If the constraints cannot be met, the signal instance is discarded.

```
SignalOutput(s:Signal, vSeq:VALUE*, delay:Duration, priority:NAT,
    toArg:[TOARG], viaArg:VIAARG) \(\equiv\)
    let invReference \(=\quad(\) if toArg \(\in\) PID then
                                    s.idToNodeASl \(\notin\) toArg.s-Interface-definition.s-Signal-definition-set
                                    else false endif)
    in
    if invReference then
        raise(InvalidReference)
    else
        choose \(g: g \in(\) Self.outgates \(\cup\) Self.ingates \() \wedge\) applicable \((s\), toArg, viaArg, \(g\), undefined \()\)
            extend PlainSignalinst with si
            si.plainSignalType:=s
            si.plainSignalValues \(:=v S e q\)
            si. delay \(=\) delay
            si.priority \(=\) priority
            si.toArg := toArg
            si.viaArg \(:=\) viaArg
            si.plainSignalSender \(:=\) Self.selfPid
            InSERT(si, now, g)
        endextend
        endchoose
    endif
    endlet
```


## Reference sections

Definitions of functions associated with signals can be found in clause F3.2.1.1.1.

## F3.2.1.4.11 Primitive Create

## Explanation

The Create primitive specifies the creation of an SDL-2010 agent. An action of type CREATE is defined by a tuple consisting of an agent-definition, a sequence of value labels, and a continue label.

## Representation

An action of type CREATE is defined as tuple consisting of an agent-definition, a sequence of value labels, and a continue label.

```
CREATE = def Agent-identifier }\times\mathrm{ VALUELABEL* }\times\mathrm{ CONTINUELABEL
```


## Behaviour

```
EvALCREATE(a:CREATE) \equiv
    let sas = take({sas \in SDLAGENTSET: sas.agentAS1 = a.s-Agent-identifier.idToNodeAS1 }) in
        if sas.agentAS1.s-Number-of-instances.s-Maximum-number }=\mathrm{ undefined then
            let n=|{ sa\inSDLAGENT: sa.owner = sas }| in
                if n< sas.agentASl.s-Number-of-instances.s-Maximum-number then
                    CreateAgent(sas, Self, sas.agentASl)
                    else
                    Self.offspring := nullPid
            endif
            endlet
        else
            CrEATEAGENT(sas, Self, sas.agentAS1)
        endif
    endlet
    Self.currentLabel := a.s-CONTINUELABEL
```


## Reference sections

For the definition of the macro CreateAgent see clause F3.2.3.1.3.

## F3.2.1.4.12 Primitive Set

## Explanation

The Set primitive is used for expressing a timer set. An action of type SET is defined as tuple consisting of a time label, a timer, a sequence of value labels, and a continue label. The action itself is mainly defined by macro SetTimer.

## Representation

An action of type $\operatorname{SET}$ is defined as tuple consisting of a time label, a timer, a sequence of value labels, and a continue label.

```
SET = def TIMELABEL \times TIMER }\times VALUELABEL* × CONTINUELABEL
```


## Domains

TIMELABEL $=_{\text {def }}$ VALUELABEL

## Behaviour

Macro EvalSet defines the setting of a timer by macro SetTimer.

## $\operatorname{EvaLSet}(a: S E T) \equiv$

SETTimer(a.s-Timer, values(a.s-VALUELABEL-seq, Self), semvalueReal(value(a.s-TimELABEL,Self))) Self.currentLabel $:=a . s-C O N T I N U E L A B E L$

## Reference sections

The definition of macro SeTTimer can be found in clause F3.2.1.1.5.

## F3.2.1.4.13 Primitive Reset

## Explanation

The Reset primitive is used for expressing a timer reset. An action of type reset is defined as tuple consisting of a timer, a sequence of value labels, and a continue label. The primitive specifies a reset of a timer with macro ResetTimer.

## Representation

An action of type reset is defined as tuple consisting of a timer, a sequence of value labels, and a continue label.

```
RESET = def TIMER }\times VALUELABEL* × CONTINUELABEL
```


## Behaviour

Macro EvalReset specifies a reset of a timer with macro ResetTimer.

```
EvALRESET(a:RESET) \equiv
    RESETTIMER(a.s-TIMER, values( a.s-VALUELABEL-seq, Self))
    Self.currentLabel:= a.s-CoNTINUELABEL
```


## Reference sections

The definition of macro ReSETTIMER can be found in clause F3.2.1.1.5.

## F3.2.1.4.14 Primitive TimerActive

## Explanation

The TimerActive primitive is used for expressing a timer active expression. The primitive specifies the timer active check using the function active.

## Representation

An action of type TimerActive is defined as tuple consisting of a timer, a sequence of value labels, and a continue label.

```
TIMERACTIVE \(=_{\text {def }}\) TIMER \(\times\) VALUELABEL \(^{*} \times\) CONTINUELABEL
```


## Behaviour

Macro EvalTimerActive specifies the evaluation of a timer active expression.

```
EvALTimERACTIVE(t:TIMERACTIVE) \equiv
    let tmi=mk-TimERINST(Self.selfPid, t.s-TIMER, values( t.s-VALUELABEL-seq, Self) ) in
        value(Self.currentLabel, Self):= mk-SDLBooLEAN(active(tmi),BooleanType)
        Self.currentLabel := t.s-CoNTINUELABEL
    endlet
```


## Reference sections

The definition of function active can be found in clause F3.2.1.1.5.

## F3.2.1.4.15 Primitive Raise (SDL-2000 feature)

## Explanation

In SDL-2000 the Raise primitive is used for expressing the raising of exceptions. In SDL-2010, exceptions cannot be explicitly raised, so there is no need for the RAISE primitive, the EvalRaISE or RAISEEXCEPTION macros that were defined in the formal dynamic semantics for SDL-2000. Predefined exceptions still occur for certain well-defined runs as indicated by the use of the raise
function with the exception identifier as a parameter. When this occurs the further behaviour of the system is not defined by SDL-2010.

## Reference sections

The ExCEPTION domain is defined in clause F3.2.1.1.6. The raise function is defined in clause F3.3.1.1.

## F3.2.1.4.16 Primitive Stop

## Explanation

The Stop primitive is used for initiating the stopping of an agent, which takes place in two phases. In the first phase, the state machine of the agent goes into a stopping state, meaning that it no longer selects and fires any transitions. The agent ceases to exist as soon as all contained agents have been removed.

The Stop primitive is used for expressing the evaluation of stop conditions.

## Representation

$$
S T O P=\operatorname{def}()
$$

## Behaviour

Macro EvalStop specifies all actions to be taken when an agent performs a stop.

```
EVALSTOP(a:STOP) \equiv
    Self.agentMode2 := stopping
```


## Reference sections

Clause F3.2.3.2.18.

## F3.2.1.4.17 Primitive SystemValue

## Explanation

The SystemValue primitive computes the values of the predefined imperative operators.

## Representation

SYSTEMVALUE $=_{\text {def }}$ VALUEKIND $\times$ CONTINUELABEL
VALUEKIND $=_{\operatorname{def}}\{$ kNow, kSelf, kParent, kOffspring, kSender,kActiveAgents $\}$

## Behaviour

EvalSystemValue $(a:$ SystemValue $) \equiv$
value(Self.currentLabel, Self) := case a.s-VALUEKIND of | kNow => mk-SDLTimE(now, TimeType) | kSelf=> Self.selfPid | kParent=> Self.parent | kOffspring=> Self.offspring |kSender=> Self.sender | kActiveAgents=> mk-SDLINTEGER(|\{ sa $\in$ SDLAGENT: sa.parent = Self \}|, IntegerType) endcase
Self.currentLabel :=a.s-CONTINUELABEL

## F3.2.1.4.18 Primitive AnyValue

## Explanation

The AnyValue primitive computes the any expression.

## Representation

ANYVALUE $=_{\text {def }}$ Sort-identifier $\times$ CONTINUELABEL

## Behaviour

$\operatorname{EVALANYVALUE}(a: \operatorname{ANYVALUE}) \equiv$
value(Self.currentLabel, Self) := selectAnyValue( a.s-Sort-identifier)
Self.currentLabel :=a.s-CONTINUELABEL
The selectAnyValue function returns the nullPid for a pid sort, a random value of the sort for other sorts and undefined if the sort has no values.

```
selectAnyValue(id: Sort-identifier): VALUE = def
    if id.idToNodeAS1 \in Interface-definition then nullPid
    else take( {v|v\inVALUE ^v.sort =id })
    endif
```


## F3.2.1.4.19 Primitive SetRangeCheckLabel

## Explanation

The SetRangeCheckValue primitive is used to set the value to be used in a range check.

## Representation

SETRANGECheckVaLue $=_{\text {def }}$ VALUELABEL $\times$ ContinueLabeL
static rangeCheckValue: $\rightarrow$ LABEL
The static function rangeCheckValue denotes a special label, which is different from all other labels in the system. It is used to store the value to be used in the subsequent range check via the function value.

## Behaviour

EvalSetRangeCheckValue( $a$ : SetRangeCheckValue) $\equiv$
value(rangeCheckValue, Self) := value(a.s-VALUELABEL, Self)
Self.currentLabel :=a.s-CONTINUELABEL

## F3.2.1.4.20 Primitive Scope

## Explanation

The Scope primitive creates a new scope for use in a compound node.

## Representation

SCOPE $=_{\text {def }}$ Connector-name $\times$ Variable-definition-set $\times$ STARTLABEL $\times$ STEPLABEL $\times$ CONTINUELABEL STEPLABEL def $_{\text {def }}$ LABEL

## Behaviour

$\operatorname{EVALSCOPE}(a: S C O P E) \equiv$
CreatecompoundNodeV ariables(Self, a) Self.currentLabel :=a.s-STARTLABEL

## Reference sections

See also clause F3.2.3.1.8.

## F3.2.1.4.21 Primitive Skip

## Explanation

This is basically a no-op. It is used, for instance, to model joins.

## Representation

```
SKIP = def () }\times(\mathrm{ Connector-name }\cup\mathrm{ CONTINUELABEL }
```


## Behaviour

```
EVALSKIP(a:SKIP) \equiv
    if a.s-implicit \inConnector-name then
        Self.stateNodeChecked := Self.currentParentStateNode
        Self.currentConnector := mk-STATENODEWITHCONNECTOR(Self.currentParentStateNode, a.s-implicit)
        Self.agentMode2 := selectingTransition
        Self.agentMode3 := startSelection
    else
        Self.currentLabel := a.s-implicit
    endif
```


## Reference sections

Clause F3.2.3.2.8.

## F3.2.1.4.22 Primitive Break

## Explanation

The Break primitive models the break operation, i.e., it leaves the current scope until the named scope is found.

## Representation

$$
\text { BREAK }=\operatorname{def}() \times(\text { Connector-name })
$$

## Behaviour

```
EvalBreak(a:BREAK) \equiv
    if scopeName(Self,Self.currentStateId) = a.s-Connector-name then
        Self.currentLabel := scopeContinueLabel(Self, Self.currentStateId)
    endif
    Self.currentStateId := caller(Self.stateAgent.state, Self.currentStateId)
```


## F3.2.1.4.23 Primitive Continue

## Explanation

The Continue primitive is used for modelling the loop continue operation.

## Representation

Continue $=_{\text {def }}() \times($ Connector-name $)$

## Behaviour

EvalContinue $(a:$ Continue $) \equiv$
if scopeName(Self, Self.currentStateId) $=$ a.s-Connector-name then
Self.currentLabel $:=$ scopeStepLabel(Self, Self.currentStateId)
else
Self.currentStateId := caller(Self.stateAgent.state, Self.currentStateId)
endif

## F3.2.1.4.24 Primitive EnterStateNode

## Explanation

State nodes are entered when an SDL-2010 agent has been created, and at the end of each transition. Also, state nodes are entered when a procedure is invoked. The evaluation of the primitive starts the sequence of steps needed to enter a given state node, which may include the entering of composite states and the execution of start transitions and entry procedures.

## Representation

```
ENTERSTATENODE = def (State-name \cup HISTORY ) }\times\mathrm{ STATEENTRYPOINT }\times\mp@subsup{V}{\mathrm{ VALUELABEL*}}{
```


## Behaviour

```
EvalEntERStatENodE(a:ENTERSTATENODE) \equiv
    let enterName:(State-name \cup HISTORY) =a.s-implicit in
        if enterName = HISTORY then
            Self.stateNodesToBeEntered :=
                {mk-STATENODEWITHENTRYPOINT(Self.previousStateNode, HISTORY)}
        else
            choose sn: sn E STATENODE ^ sn.stateName = enterName ^
                sn.stateNodeKind = stateNode ^ sn.parentStateNode = Self.currentParentStateNode
                Self.stateNodesToBeEntered :=
                            {\mathbf{mk}-STATENODEWITHENTRYPoint(sn, a.s-STATEENTRYPoint)}
            endchoose
        endif
        Self.agentMode3 := enteringStateNode
        Self.agentMode4 := startPhase
        Self.currentLabel:= undefined
        Self.continueLabel := undefined
    endlet
```

Given the State-name and the currentParentStateNode, the state node to be entered is determined. This has to be done at execution time, as the state node instance is not known during compilation. Agent modes are set such that the sequence of steps needed to enter the state node is performed.

## Reference sections

See also clause F3.2.3.2.15.

## F3.2.1.4.25 Primitive LeaveStateNode

## Explanation

State nodes are left at the start of transitions.

## Representation

LeavestateNode $=_{\text {def }}$ State-name $\times$ ContinueLabel

## Behaviour

```
EvalLEAVESTATENODE(a:LEAVESTATENODE) \equiv
    choose sn: sn \in STATENODE ^ sn.stateName = a.s-State-name ^
        sn.stateNodeKind = stateNode }\wedge\mathrm{ sn.parentStateNode = Self.currentParentStateNode
        // assertion: sn = Self.previousStateNode
        Self.stateNodesToBeLeft := collectCurrentSubStates(sn)
    endchoose
    Self.agentMode3 := leavingStateNode
    Self.agentMode4 := leavePhase
    Self.currentLabel:= undefined
    Self.continueLabel := a.s-CONTINUELABEL
```

Given the State-name and the currentParentStateNode, the state node to be left is determined. This has to be done at execution time, as the state node instance is not known during compilation. Agent modes are set such that the sequence of steps needed to leave the state node is performed.

## Reference sections

See also clause F3.2.3.2.16 for information on how state nodes are left.

## F3.2.1.5 Undefined behaviour

Undefined behaviour is represented by the following program:

```
UNDEFINEDBEHAVIOUR \equiv
    Self.program := UNDEFINED-BEHAVIOUR-PROGRAM
```

UndEFINED-BEHAVIOUR-PROGRAM:
// the contents of this program is not defined

The content of the program UNDEFINED-BEHAVIOUR-PROGRAM is not specified. Whenever the further behaviour of the system is undefined, the current agent is switched to this program.

This local undefinedness condition is in fact global as the program Undefined-BEHAVIOURProgram could involve setting program for all agents.

## F3.2.2 Compilation function

The following two functions form the interface between the compilation and the dynamic semantics. For all the behaviour parts that involve transitions, the corresponding runtime representation of the transitions is generated.

```
getStateTransitions(s: State-node): SEmTRANSITION-set = def
    { mk-SEmTRANSITION(i.s-Signal-identifier,
        if i.s-Provided-expression = undefined then
            undefined
        else
            i.s-Provided-expression.startLabel
        endif,
        if i.s-PRIORITY = undefined then undefined else 1 endif,
        i.s-Transition.startLabel,
        undefined)
    |i\ins.s-Input-node-set }}
    { mk-SemTransition(NONE, sp.s-Provided-expression.startLabel,
        undefined, sp.s-Transition.startLabel, undefined)
    |p \ins.s-Spontaneous-transition-set }}
    { mk-SEmTRANSITION(NONE, c.s-Continuous-expression.startLabel,
        c.s-Priority-name, c.s-Transition.startLabel, undefined)
    | fs.s-Continuous-signal-set }}
    { mk-SEmTransition(NONE, undefined, undefined, c.s-Transition.startLabel,
        if c.s-State-exit-point-name = undefined then DEFAULT else c.s-State-exit-point-name endif)
    |c\ins.s-Connect-node-set }
getStateStartTransitions(sn: State-start-node): STARTTRANSITION= def
    mk-STARTTRANSITION(sn.s-Transition.startLabel, sn.s-State-entry-point-name)
getNamedStartTransitions(sn: Named-start-node): STARTTrANSITION=def
    mk-STARTTRANSITION(sn.s-Transition.startLabel, sn.s-State-entry-point-name)
getProcStartTransitions(sn: Procedure-start-node): STARTTRANSITION=def
    mk-StartTrANSItION(sn.s-Transition.startLabel, undefined)
getStartTransitions(s: (State-start-node }\cup\mathrm{ Named-start-node }\cup\mathrm{ Procedure-start-node)-set):
        STARTTRANSITION-set =def
```

```
    { if sn \in State-start-node then getStateStartTransitions(sn)
    elseif sn \inNamed-start-node then getNamedStartTransitions(sn)
    elseif sn \in Procedure-start-node then getProcStartTransitions(sn)
    endif |sn \ins}
getFreeActions(actions: Free-action-set): FREEACTION-set =def
    { mk-FREEACTION(f.s-Connector-name, f.s-Transition.startLabel) |f\inactions }
```

Here we present the function that compiles an SDL-2010 state machine description into an ASM representation. A special labelling of graph nodes is used to model specific control-flow information. Intuitively, node labels relate individual operations of an SDL-2010 agent to transition rules in the resulting SAM model. The effect of state transitions of SDL-2010 agents is then modelled by firing the related transition rules in an analogous order.

Labels are abstractly represented by a static domain LABEL.

```
static domain LABEL
```

To start with the compilation, we first need a function to find unique labels for a syntactic entity. The second argument is introduced to allow for more than one such label within the same SDL-2010 pattern
monitored uniqueLabel: DEFINITIONASI $\times$ NAT $\rightarrow$ LABEL
For this function, it holds that

```
constraint \(\forall d_{1}, d_{2} \in\) DEFINITIONAS1: \(\forall i_{1}, i_{2} \in\) NAT:
    uniqueLabel \(\left(d_{1}, i_{1}\right)=\) uniqueLabel \(\left(d_{2}, i_{2}\right) \Leftrightarrow\left(d_{1}=d_{2} \wedge i_{1}=i_{2}\right)\)
```

Finally, to formalize the compilation, we also need an auxiliary function generating a sequence out of a set. This function is used when the sequence of events has to be computed but does not really matter. See for instance Decision-node and Range-condition.

```
setToSeq(s: \(X\)-set): \(X^{*}=_{\text {def }}\)
    if \(s=\varnothing\) then empty else
            let \(e l=c\).take in
            \(\langle e l\rangle \frown \operatorname{setToSeq}(s \backslash\{e l\})\)
        endlet
    endif
```

The compilation is formalized in terms of the following two compilation functions, one for transition behaviour and one for expression behaviour.

```
compile: DEFINITIONASI }->\mathrm{ BEHAVIOUR
compileExpr: DEFINITIONASI × LABEL }->\mathrm{ BEHAVIOUR
```

The computed value of an expression $e$ is always stored at value(uniqueLabel ( $e, 1$ ), Self).
The two compilation functions are gradually introduced by defining a series of compilation patterns and the corresponding results; each individual pattern is uniquely associated with a certain type of node in the AST to be compiled. Afterwards, the function startLabel is defined also with a series of patterns in clause F3.2.2.4

## F3.2.2.1 States and triggers

The following parts are considered to form the definition of the function compile if put together with the following header. The contents of the case expression are all the compilation cases as given below.
compile(a: DEFINITIONAS1): BEHAVIOUR $=_{\text {def }}$
case $a$ of

All the contents of this function are given as patterns and what the result of the function is for these patterns. The default case when no pattern is matching is the collected set of all the results of all children nodes.

The handling of inheritance is done in the dynamic part. What you find below is the compilation of the plain behaviour descriptions.

The definition of the compilation function is done using a series of auxiliary derived functions.

```
| v=Variable-definition( name, *, init) =>
    if init }=\mathrm{ undefined then
            compileExpr(init, uniqueLabel(v,1)) \cup
            {mk-PRIMITIVE(uniqueLabel(v,1),mk-TASK(name,uniqueLabel(init,1),false,undefined)) }
    else }
    endif
```

| State-transition-graph( *, start, states, freeActions) =>
compile(start) $\cup$
$\mathbf{U}\{$ compile $(s) \mid s \in$ states $\} \cup$
$\mathbf{U}\{$ compile $(f) \mid f \in$ freeActions $\}$
| Procedure-graph( start, states, freeActions) =>
compile(start) $\cup$
$\mathbf{U}\{$ compile $(s) \mid s \in$ states $\} \cup$
$\mathbf{U}\{$ compile $(f) \mid f \in$ freeActions $\}$
$\mid$ State-start-node ${ }^{*}$, transition) $=>$ compile(transition)
| Procedure-start-node(transition) => compile(transition)
| Named-start-node(*, trans) => compile(trans)
| State-node( ${ }^{*}$, *, *, inputs, spontaneous, continuous, conns, *) =>
$\mathbf{U}\{$ compile $(i) \mid i \in$ inputs $\} \cup$
$\mathbf{U}\{$ compile $(s) \mid s \in$ spontaneous $\} \cup$
$\mathbf{U}\{$ compile $(c) \mid c \in$ continuous $\} \cup$
$\mathbf{U}\{$ compile $(c) \mid c \in$ conns $\}$
$\mid i=\operatorname{Input-node}\left({ }^{*}, *\right.$, vars, provided, transition) $=>$
if provided $=$ undefined then $\varnothing$ else compileExpr(provided, undefined) endif $\cup$
\{ mk-PRImitivE(uniqueLabel(i,idx),
if $\operatorname{vars}[i d x] \neq$ undefined then
$\mathbf{m k}-A S S I G N P A R A M E T E R S(v a r s[i d x], i d x$,
uniqueLabel(i,idx))
else mk-SKIP( uniqueLabel(i,idx))
endif)
$\mid$ idx $\in$ toSet(1..vars.length -1$)\} \cup$
$\{\mathbf{m k}-$ PRIMITIVE(uniqueLabel(i, vars.length),
if vars $[$ vars.length $] \neq$ undefined then
mk-ASSIGNPARAMETERS(vars[vars.length], vars.length, transition.startLabel)
else mk-SKIP(transition.startLabel)
endif)
$\} \cup$
compile(transition)
| Spontaneous-transition(provided, transition) =>
if provided $=$ undefined then $\varnothing$ else compileExpr(provided, undefined) endif $\cup$
compile(transition)
| Continuous-signal(*, condition, *, transition) =>
compileExpr(condition, undefined) $\cup$
compile(transition)
| Connect-node(*, transition) => compile(transition)
| Free-action(*, transition) => compile(transition)
$\mid t=T r a n s i t i o n(n o d e s$, endnode) $=>$
if $t$.parentAS1.parentAS1.s-State-name $\neq$ undefined then
\{ mk-PRIMITIVE (uniqueLabel ( $a, 1$ ),
mk-LEAVESTATENODE(t.parentAS1.parentAS1.s-State-name, $\operatorname{startLabel((if~nodes~=~empty~then~endnode~else~nodes.head~endif)))~\} ~}$
else $\varnothing$ endif $\cup$
compileNodes $\cup$
compile(endnode)
where
compileNodes: BEHAVIOUR $=$ def
if nodes = empty then $\varnothing$
else compileExpr(nodes.last, endnode. startLabel) $\cup$
$\mathbf{U}\{$ compileExpr(nodes[i], nodes[i+1]. startLabel) $\mid i \in 1$..nodes.length -1$\}$
endif
endwhere

## F3.2.2.2 Terminators

| Terminator(terminator) => compile(terminator)
| $n=$ Named-nextstate(stateName, undefined) =>
\{ mk-PRIMITIVE(uniqueLabel( $n, 1$ ),
mk-ENTERSTATENODE(stateName, undefined, empty)) \}
|n=Named-nextstate(stateName, Nextstate-parameters(exprList, entry)) =>
if exprList = empty then $\varnothing$
else compileExpr $(\operatorname{exprList}$. last, uniqueLabel $(n, 1)) \cup$
$\mathbf{U}\{$ compileExpr $($ exprList $[i]$, exprList $[i+1]$. startLabel $) \mid i \in 1 .$. exprList.length -1$\}$
endif $\cup$
\{ mk-PRIMITIVE(uniqueLabel(n,1), mk-ENTERSTATENODE(stateName, entry, <uniqueLabel(e,1)|e in exprList >)) \}
| $n=$ Dash-nextstate(HISTORY) =>
\{ $\mathbf{m k}-\operatorname{PRIMITIVE}$ (uniqueLabel(n,1), mk-ENTERSTATENODE(HISTORY, undefined, empty)) \}
$\mid s=$ Stop-node () =>
\{mk-PRIMITIVE(uniqueLabel(s,1), mk-STOP()) \}
| $a=$ Action-return-node () ) ${ }^{\text {> }}$
\{mk-PRIMITIVE(uniqueLabel( $a, 1$ ), mk-RETURN
(if parentASlofKind(a,Composite-state-type-definition).parentASl $\in$
Composite-state-type-definition then DEFAULT else undefined endif)) \}
| $v=$ Value-return-node $($ expr $)$ =>
compileExpr(expr, uniqueLabel $(v, 1)) \cup$
\{mk-PRIMITIVE(uniqueLabel(v,1), mk-RETURN(uniqueLabel(expr,1))) \}
| $n=$ Named-return-node(name) =>
\{mk-PRIMITIVE(uniqueLabel(n,1), mk-RETURN(name)) \}
| $j=$ Join-node(connector) =>
\{mk-PRIMITIVE(uniqueLabel( $j, 1$ ), mk-SKIP(connector)) \}
|b=Break-node(connector) =>
\{mk-PRIMITIVE(uniqueLabel(b,1), mk-BREAK(connector)) \}
| $c=$ Continue-node(connector) $=>$
\{ $\mathbf{m k}-\operatorname{PRIMITIVE}($ uniqueLabel( $(, 1)$, mk-CONTINUE(connector)) \}
| d=Decision-node(question, answerset, elseanswer) =>
(let aseq $=$ answerset.setToSeq in
compileExpr(question, aseq[1].startLabel) $\cup$
\{ compileExpr(aseq[idx].s-implicit,
if $i d x=$ aseq.length then uniqueLabel $(d, 1)$ else aseq[idx+1].startLabel endif)
$\mid i d x \in \operatorname{toSet}(1 . . a s e q . l e n g t h)\} \cup$
\{ mk-PRIMITIVE(uniqueLabel(d, 1),
mk-DECISION(uniqueLabel(question, 1),

```
    { mk-ANSWER(uniqueLabel(ans.s-implicit, 1), ans.s-Transition.startLabel)
    |ans \in answerset },
    if elseanswer=undefined then undefined else elseanswer.s-Transition endif)) }
endlet) }
U{compile(ans.s-Transition)|ans \in answerset }}
compile(elseanswer.s-Transition)
```

This concludes the definition of the compile function.
endcase // end of the compile function definition

## F3.2.2.3 Actions

The following compilation parts define the function compileExpr with the following header.

```
compileExpr(a: DEFINITIONAS1, next: LABEL): BEHAVIOUR = def
    case a of
```

All the contents of this function are given as patterns and what the result of the function for these patterns is. The default result when no pattern is matching is the empty set. All the patterns given below may use the variable next referring to the next label to process.

```
| Graph-node(action) => compileExpr(action, next)
| a=Assignment(id, expr) =>
    compileExpr(expr, uniqueLabel(a,1))\cup
    {mk-PRIMITIVE(uniqueLabel(a,1), mk-TaSK(id, uniqueLabel(expr,1), false, next) )}
| o=Output-node(sig, exprList, delay, priority, dest, via ) =>
    if dest \inIdentifier then
        if exprList = empty then \varnothing
        else compileExpr(exprList.last, uniqueLabel(o,1))\cup
            U{ compileExpr(exprList[i], exprList[i+1]. startLabel) |i\in 1..exprList.length - 1 }
            endif }
            compileExpr(delay, uniqueLabel(o,1))\cup
            compileExpr(priority, uniqueLabel(o,1))\cup
            {mk-PRIMITIVE(uniqueLabel(o,1),
                mk-OUtPUT(sig, <uniqueLabel(e,1)|e in exprList>,
                    uniqueLabel(delay,1), uniqueLabel(priority,1), dest, via, next)) }
    else
            if exprList = empty then \varnothing
            else compileExpr(exprList.last, dest.startLabel) \cup
            U{ compileExpr(exprList[i], exprList[i+1]. startLabel) |i\in 1..exprList.length - 1 }
            endif }
            compileExpr(dest, uniqueLabel(o,1)) \cup
            compileExpr(delay, uniqueLabel(o,1))\cup
            compileExpr(priority, uniqueLabel(o,1))\cup
            {mk-PRIMITIVE(uniqueLabel(o,1),
            mk-OUTPUT(sig, <uniqueLabel(e,1)|e in exprList>,
                                    uniqueLabel(delay,1), uniqueLabel(priority,1), uniqueLabel(dest,1), via, next)) }
    endif
| c=Create-request-node(agentId, exprList) =>
            if exprList = empty then \varnothing
            else compileExpr(exprList.last, uniqueLabel(c,1))\cup
            U{ compileExpr(exprList[i], exprList[i+1]. startLabel) |i\in 1..exprList.length - 1 }
            endif }
            {mk-PRIMITIVE(uniqueLabel(c,1),
            mk-CREATE(agentId, <uniqueLabel(e,1)|e in exprList>, next)) }
| c=Call-node(*, procedureId, exprList) =>
    if exprList = empty then \varnothing
    else compileExpr(exprList.last, uniqueLabel(c,1))\cup
            U{ compileExpr(exprList[i], exprList[i+1]. startLabel)|i\in 1..exprList.length - 1 }
```

```
    endif }
    (let paramDef = procedureId.idToNodeAS1.s-Procedure-formal-parameter-seq in
        {\mathbf{mk}-PRIMITIVE(uniqueLabel(c,1),
                mk-CALL(procedureId,
                <( if paramDef[idx] \in In-parameter
                then uniqueLabel(exprList[idx], 1)
                    else exprList[idx]
                endif )
                |idx in (1..exprList.length ) >, uniqueLabel(c,1),
                next)) }
    endlet)
| c=Compound-node(name, variables, eh, initNodes, trans, stepNodes) =>
    {mk-PRIMITIVE(uniqueLabel(c,1),
        mk-SCOPE(name, variables,
                if initNodes = empty then trans.startLabel else initNodes.head.startLabel endif,
                if stepNodes = empty then trans.startLabel else stepNodes.head.startLabel endif,
                next))}}
    compile(eh)\cup
    compileExpr(trans, undefined) \cup
    if stepNodes = empty then }
    else compileExpr( stepNodes.last, trans.startLabel) }
        U{compileExpr( stepNodes[i], stepNodes[i+1]. startLabel)|i\in 1..stepNodes.length - 1 }
    endif }
    if initNodes = empty then }
    else compileExpr( initNodes.last, trans.startLabel) \cup
        \{ compileExpr( initNodes[i],initNodes[i+1]. startLabel)|i\in 1..initNodes.length - 1 }
    endif
| s=Set-node(expr,timerId, exprList) =>
    if exprList = empty then }
    else compileExpr(exprList.last, expr.startLabel) }
        U{ compileExpr(exprList[i], exprList[i+1]. startLabel)|i\in 1..exprList.length - 1}
    endif }
    compileExpr(expr, uniqueLabel(s,1))\cup
    {\mathbf{mk}-PRIMITIVE(uniqueLabel( }s,1)
            mk-SET(uniqueLabel(expr,1), timerId, <uniqueLabel(e,1)|e in exprList >, next))}
|=Reset-node(timerId, exprList) =>
    if exprList = empty then \varnothing
    else compileExpr(exprList.last, uniqueLabel(r,1))\cup
            \{ compileExpr(exprList[i], exprList[i+1]. startLabel)|i\in 1..exprList.length - 1 }
    endif }
    {\mathbf{mk}-PRIMITIVE(uniqueLabel(r,1),
            mk-RESET(timerId,<uniqueLabel(e,1)|e in exprList>,next)) }
| r=Range-condition(items) =>
    (let iseq = items.setToSeq in
    {mk-PRIMITIVE(uniqueLabel(r,1),
            mk-OPERATIONAPPLICATION(sdlTrue.idToNodeAS1, empty,
                uniqueLabel(r, iseq.length+1))) }}
            { compileExpr(iseq[idx],uniqueLabel(r,idx))|idx \intoSet(1..iseq.length)}}
            { mk-PRIMITIVE(uniqueLabel(r, idx),
            mk-OPERATIONAPPLICATION(sdlOr,
                < uniqueLabel(r,idx+1), uniqueLabel(iseq[idx],1) >,
                if idx=1 then next else iseq[idx-1].startLabel endif))
    idx }\in\operatorname{toSet(1..iseq.length) }}
    { mk-PRIMITIVE(uniqueLabel(r, 0), mk-BREAK(undefined)) }
    endlet)
```

The Range-condition above is computed as follows. First, a true value is evaluated. Then all items are sequentialized and evaluated from the last to the first; the results are cumulated using AND. Afterwards, the enclosing scope is left using a break.

```
| o=Open-range(id, expr) =>
    compileExpr(expr, uniqueLabel(o, 1)) \cup
    { mk-PRIMITIVE(uniqueLabel(o, 1),
        mk-OPERATIONAPPLICATION(id.idToNodeAS1,
            < rangeCheckValue, uniqueLabel(expr, 1) >, next)) }
| c=Closed-range(r1,r2) =>
    compileExpr(r1, r2.startLabel) }
    compileExpr(r2, uniqueLabel(c,1)) \cup
    { mk-PRIMITIVE(uniqueLabel(c, 1),
            mk-OPERATIONAPPLICATION(sdlAnd, < uniqueLabel(r1, 1), uniqueLabel(r2, 1) >, next)) }
| l=Literal(id) =>
    {\mathbf{mk}-PRIMITIVE(uniqueLabel(l,1),
        mk-OPERATIONAPPLICATION(id.idToNodeAS1, empty, next)) }
| c=Conditional-expression(boolExpr,consExpr,altExpr) =>
    compileExpr(boolExpr, uniqueLabel(c, 2))\cup
    compileExpr(consExpr, next) }
    compileExpr(altExpr, next) }
    {mk-PRIMITIVE(uniqueLabel(c,2),
            mk-OPERATIONAPPLICATION(sdlTrue.idToNodeAS1, empty,uniqueLabel(c, 1))) } \cup
    { mk-PRIMITIVE(uniqueLabel(c, 1),
        mk-DECISION(uniqueLabel(boolExpr, 1),
            {\mathbf{mk}-ANSWER(uniqueLabel(c, 2), consExpr.startLabel) },altExpr.startLabel)) }
| e=Equality-expression(first, second) =>
    compileExpr(first, second.startLabel) \cup
    compileExpr(second, uniqueLabel(e,1))\cup
    {mk-PRIMITIVE(uniqueLabel(e,1),
        mk-EQUALITY(uniqueLabel(first,1), uniqueLabel(second,1), next)) }
| o=Operation-application(id, exprList) =>
    if exprList = empty then \varnothing
    else compileExpr(exprList.last, uniqueLabel(o,1))\cup
        U{ compileExpr(exprList[i], exprList[i+1]. startLabel) |i\in 1..exprList.length - 1 }
    endif }
    {mk-PRIMITIVE(uniqueLabel(o,1),
        mk-OPERATIONAPPLICATION(id.idToNodeAS1,
                < uniqueLabel(e, 1)|e in exprList>,
            next)) }
|=Range-check-expression(range, expr) =>
    compileExpr(expr, uniqueLabel(r,2)) \cup
    compileExpr(range, undefined) }
    {mk-PRIMITIVE(uniqueLabel(r,2),
            mk-SETRANGECHECKVALUE(uniqueLabel(expr,1), uniqueLabel(r,1))) }}
    {\mathbf{mk}-PRIMITIVE(uniqueLabel(r,1),
        mk-SCOPE(undefined, }\varnothing\mathrm{ , range.startLabel, undefined, next)) }
| v=Variable-access(id) =>
    {mk-PRIMITIVE(uniqueLabel(v,1), mk-VAR(id,next)) }
| n=Now-expression() =>
    {\mathbf{mk}-PRIMITIVE(uniqueLabel(n,1), mk-SYSTEmVALUE(kNow, next)) }
| p=Parent-expression() =>
    {\mathbf{mk}-PRIMITIVE(uniqueLabel(p,1), mk-SySTEMVALUE(kParent,next)) }
| o=Offspring-expression() =>
    {\mathbf{mk}-PRIMITIVE(uniqueLabel(o,1), mk-SYSTEMVALUE(kOffspring,next)) }
| s=Self-expression() =>
    {mk-PRImitiVE(uniqueLabel(s,1), mk-SYSTEMVALUE(kSelf, next)) }
| s=Sender-expression () =>
    {\mathbf{mk}-PRIMITIVE(uniqueLabel(s,1),\mathbf{mk}-SySTEMVALUE(kSender,next)) }
```

```
| t=Timer-active-expression(id, exprList) =>
    if exprList = empty then \varnothing
    else compileExpr(exprList.last, uniqueLabel(t,1))\cup
            U{compileExpr(exprList[i], exprList[i+1]. startLabel)|i\in 1..exprList.length - 1 }
    endif }
    {mk-PRIMITIVE(uniqueLabel(t,1),
        mk-TimerACtive(id, < uniqueLabel(e,1)|e in exprList >,next))}
| a=Any-expression(id) =>
    {\mathbf{mk}-PRIMITIVE(uniqueLabel(a,1), mk-ANYVALUE(id,next)) }
|=Value-returning-call-node(*, procedureId, exprList) =>
    if exprList = empty then \varnothing
    else compileExpr(exprList.last, uniqueLabel(v,1))\cup
        U{compileExpr(exprList[i], exprList[i+1]. startLabel)|i\in 1..exprList.length - 1 }
    endif }
    (let paramDef = procedureId.idToNodeASl.s-Procedure-formal-parameter-seq in
        {\mathbf{mk}-PRIMITIVE(uniqueLabel(v,1),
            mk-CALL(procedureId,
            < (if paramDef[idx] \in In-parameter
            then uniqueLabel(exprList[idx], 1)
            else exprList[idx]
                endif )
                |idx in (1..exprList.length )>, uniqueLabel(v,1),
                next)) }
    endlet)
```

This concludes the definition of the expression compilation function.
endcase // end of the compileExpr function definition

## F3.2.2.4 Start labels

This clause introduces the function startLabel, which defines the start labels of all behavioural syntax constructs.

```
startLabel(x: DEFINITIONAS1): LABEL = def
    case }x\mathrm{ of
    |=Variable-definition(*, *, init) =>
        if init = undefined then undefined else init.startLabel endif
    |=State-start-node(*,*, trans) => startLabel(trans)
    p=Procedure-start-node(*, trans) => startLabel(trans)
    |=Input-node(*, *, *, *, *, trans) => startLabel(trans)
    |=Spontaneous-transition(*, *, trans) => startLabel(trans)
    c=Continuous-signal(*, *, *, trans) => startLabel(trans)
    | c=Connect-node(*, *, trans) => startLabel(trans)
    |=Free-action(*,trans) => startLabel(trans)
    | t=Transition(nodes, endnode) =>
        if t.parentASl.parentASl \in State-node then uniqueLabel(t,1) // insert the Leavestatenode
        elseif nodes = empty then startLabel(endnode)
        else startLabel(nodes.head)
        endif
    |=Graph-node(action, *) => startLabel(action)
    |=Assignment(*, expr) => startLabel(expr)
    | o= Output-node(*, expr, dest, *) =>
        if dest }=\mathrm{ undefined then startLabel(dest)
        elseif expr = empty then uniqueLabel(o,1)
        else startLabel(expr.head) endif
    | c=Create-request-node (*, exprList) =>
        if exprList = empty then uniqueLabel(c,1) else exprList.head.startLabel endif
    | c=Call-node(*, *, exprList) =>
            if exprList = empty then uniqueLabel(c,1) else exprList.head.startLabel endif
    | c=Compound-node(*, *, *, *,trans, *) => uniqueLabel(c,1)
    s=Set-node(when, *, *) => startLabel(when)
```

```
\(\mid r=\) Reset-node(*, exprList) \(=>\)
    if exprList \(=\) empty then uniqueLabel \((r, 1)\) else exprList.head.startLabel endif
\(\mid t=\) Terminator(terminator, *) \({ }^{*}\) startLabel(terminator)
\(\mid n=\) Named-nextstate( \({ }^{*}\), undefined) \(=>\) uniqueLabel \((n, 1)\)
| \(n=\) Named-nextstate( \({ }^{*}\), Nextstate-parameters(exprList, *)) \(=>\)
    if exprList = empty then uniqueLabel \((n, 1)\) else exprList.head.startLabel endif
\(\mid n=\) Dash-nextstate \(\left({ }^{*}\right)\) => uniqueLabel \((n, 1)\)
|s=Stop-node() => uniqueLabel \((s, 1)\)
|a=Action-return-node() => uniqueLabel \((a, 1)\)
\(v=\) Value-return-node \((\) expr \()=>\) uniqueLabel \((v, 1)\)
|n=Named-return-node(expr) \(\Rightarrow>\) uniqueLabel \((n, 1)\)
\(j=\operatorname{Join-node}(*)\) => uniqueLabel \((j, 1)\)
b= Break-node(*) => uniqueLabel( \(b, 1\) )
c= Continue-node \(\left({ }^{*}\right)\) => uniqueLabel \((c, 1)\)
\(\mid d=\) Decision-node(question, \(\left.{ }^{*}, *, *\right)\) => startLabel(question)
| \(\mathrm{a}=\operatorname{Decision-answer~}(r, *)\) => startLabel \((r)\)
| \(n=\) Named-start-node(*, *, trans) => startLabel(trans)
o=Open-range \((*\), expr \()=>\) startLabel \((\) expr \()\)
c=Closed-range \((*, *)\) => uniqueLabel \((c, 1)\)
| \(l=\operatorname{Literal}(*)\) => uniqueLabel \((l, 1)\)
\(\mid c=C o n d i t i o n a l-e x p r e s s i o n(*, ~ *, ~ *) ~=>~ u n i q u e L a b e l ~(~ c, ~ 1) ~\)
Equality-expression(first, *) => first.startLabel
\(\mid r=\) Range-check-expression \((*\), expr \()\) => expr.startLabel
\(\mid v=\) Variable-access(id) \(=>\) uniqueLabel \((v, 1)\)
\(\mid o=\) Operation-application \((*\), exprList \()=>\)
    if exprList = empty then uniqueLabel \((o, 1)\) else exprList.head.startLabel endif
\(\mid v=\operatorname{Identifier}\left({ }^{*}, *\right)=>\) uniqueLabel \((v, 1)\)
|n=Now-expression ()\(=>\) uniqueLabel \((n, 1)\)
\(\mid s=\) Self-expression () => uniqueLabel \((s, 1)\)
\(p=\) Parent-expression ()\(=>\) uniqueLabel \((p, 1)\)
| \(o=\) Offspring-expression ()\(=>\) uniqueLabel \((o, 1)\)
s=Sender-expression() => uniqueLabel( \(s, 1\) )
\(\mid t=\) Timer-active-expression \((*\), exprList \()=>\)
    if exprList \(=\) empty then uniqueLabel \((t, 1)\) else exprList.head.startLabel endif
\(\mid a=\) Any-expression \((*)\) => uniqueLabel \((a, 1)\)
\(\mid v=\) Value-returning-call-node \((*\), ,, exprList \()=>\)
    if exprList \(=\) empty then uniqueLabel \((v, 1)\) else exprList.head.startLabel endif
endcase
```


## F3.2.3 SDL-2010 abstract machine programs

For each SDL-2010 specification, the set of legal system runs are built using the SDL-2010 abstract machine and the compilation in clause F3.2.2.

## F3.2.3.1 System initialization

Starting from any pre-initial state of $S_{0}$, the initialization rules describe a recursive unfolding of the specified system instance according to its initial hierarchical structure. For each SDL-2010 agent instance, a corresponding ASM agent is created and initialized. Furthermore, ASM agents are created to model links and SDL-2010 agent sets.


Figure F3-3 - Activity phases of SDL-2010 agents and agent sets (level 1)

During its lifetime, an agent first is in mode "initialisation", where its internal structure is built up. Then, it enters the mode "execution" and remains in this mode unless it is terminated.

## F3.2.3.1.1 Pre-initial system state

This clause states some constraints on the set of initial states $S_{0}$ of the abstract state modelling a given SAM, i.e., the set of pre-initial states of the SAM. Further restrictions are defined in previous clauses, marked by the keyword initially. Usually, there is more than one pre-initial system state. It is only required that the system starts in one of these states.

```
initially
    if rootNodeAS1.s-Agent-definition = undefined then
        system.agentAS1 = rootNodeAS1.s-Agent-definition ^
        system.owner = undefined }
        system.agentMode1 = initialisation ^
        system.program = AGENT-SET-PROGRAM
    else
        system.program = undefined
    endif
```

For a given SDL-2010 specification, the initial constraint distinguishes two cases. The first case applies when an agent definition is part of the SDL-2010 specification, i.e., when rootNodeAS1.s-Agent-definition $\neq$ undefined. Only then is the semantics defined to yield a dynamic behaviour. Since the system agent is the root of the agent hierarchy, it has no owner (system.owner $=$ undefined). The SAM program of the agent system is the program applying to SDL-2010 agent sets in general. Further functions and domains are initialized when this program is executed, or are derived functions or derived domains. In the second case, no system agent is defined in the SDL-2010 specification; therefore, no behaviour is assigned via program.

## F3.2.3.1.2 Agent set creation, initialization, and removal

ASM agents modelling SDL-2010 agent sets are created during system initialization and possibly dynamically, during system execution. They can be understood as containers that reflect certain structural aspects of SDL-2010 systems, in particular agent hierarchy and the connection structure. These structural aspects are crucial to the intelligibility of SDL-2010 specifications, and are therefore represented in the formal model, too.

```
CREATEALLAGENTSETS(ow:AGENT, atd:Agent-type-definition) \equiv
    do forall ad: ad \in atd.collectAllAgentDefinitions
        CreateAgentSet(ow,ad)
    enddo
    where
        collectAllAgentDefinitions(atd: Agent-type-definition): Agent-definition-set = = def
        if atd.s-Agent-type-identifier = undefined then
            atd.s-Agent-definition-set
        else let typedef: Agent-type-definition = atd.s-Agent-type-identifier.idToNodeAS1 in
                atd.s-Agent-definition-set \cup typedef.collectAllAgentDefinitions
            endlet
            endif
    endwhere
```

SDL-2010 agent sets are created when the surrounding SDL-2010 agent is initialized right after its creation. For each agent definition found via collectAllAgentDefinitions, an SDL-2010 agent set is created, taking inheritance into account.

```
CREATEAGENTSET(ow:SDLAGENT, ad:Agent-definition) \equiv
    let typedef: Agent-type-definition=ad.s-Agent-type-identifier.idToNodeAS1 in
    extend AGENT with sas
        sas.agentAS1 := ad
        sas.owner := ow
        CreateAlLGATES (sas, typedef)
        sas.program := AGENT-SET-PROGRAM
```

sas.agentMode1 := initialisation
endextend endlet

Creation of an SDL-2010 agent set is modelled by creating an ASM agent and initializing its control block. In particular, the node Agent-definition of the AST is assigned to the function agentAS1, the owner is determined, and the initial program is set. To complete the creation of the agent set, its interface as given by all its gates is created. Thus, these gates are ready to be connected by the owner of the agent set, an SDL-2010 agent instance. Further functions and domains are initialized when Agent-Set-Program is executed, or are derived functions or derived domains. The initial agent instances of the considered SDL-2010 agent set are created when this program is executed. Apart from the creation of gates, there are strong similarities between this rule macro and the initial constraint, because system is an SDL-2010 agent set too.

The creation of SDL-2010 agent set instances relies on information of the abstract syntax tree. An element of domain Agent-definition defines the root from which this information can be accessed. In particular, there is an agent type identifier, which is a link to the agent type definition providing the internal structure of the agents, and their behaviour.

```
AgENT-SET-PROGRAM:
if Self.agentMode1 = initialisation then
    InITAGENTSET
endif
if Self.agentMode1 = execution then
    ExECAGENTSET
endif
```

Depending on the current agent mode, level 1, the activity phase is selected. After a single initialization step, the agent set is switched to the execution mode.

```
INITAGENTSET \equiv
    let typedef: Agent-type-definition = Self.agentAS1.s-Agent-type-identifier.idToNodeAS1 in
    if typedef.s-Agent-kind = SYSTEM then
        CreateAlLGates(Self, typedef)
    endif
    CreateAllAGENTS(Self, Self.agentASl)
    Self.agentMode1:= execution
    endlet
```

The initialization of agent sets (and hence also of the agent system) is given by the rule macro InitAgentSet, which is applied in the program Agent-Set-Program. During initialization, the initial agent instances - in the case of system a single agent instance - are created. After this initialization, the ASM agent is switched to the execution mode.
In case of the SDL-2010 agent set system, the gates of the system instance are created. The reasons why this is done during initialization (and not at creation as for other agent sets) are technical.

```
RemoveAllagentSets (ow:SdLAGENT) \(\equiv\)
    do forall sas: sas \(\in \operatorname{SDLAGENTSET} \wedge\) sas.owner \(=\) ow
        RemoveAgentSet(sas)
    enddo
RemoveAgentset (sas:SDLAGENTSET) \(\equiv\)
    sas.owner \(:=\) undefined
    sas.program \(:=\) undefined
```

Removal of an agent set is modelled by resetting the program (and the owner) to undefined.

## F3.2.3.1.3 Agent creation, initialization, and removal

The creation of SDL-2010 agent instances happens during system initialization, and possibly dynamically, during system execution. The creation as defined by the rule macro CreateAgent leaves an agent in what is called "pre-initial state". The agent's "initial state" is reached after agent initialization, which is defined subsequently.


Figure F3-4 - Activity phases of SDL-2010 agents: initialization (level 2)

The initialization of an agent is decomposed into a sequence of phases, as shown in the state diagram above. In each of these phases, certain parts of the agent's structure are created. After agent initialization, the agent execution is started.

```
CREATEALLAGENTS(ow:SDLAGENT, ad:Agent-definition) \equiv
    do forall i:i\in1..ad.s-Number-of-instances.s-Initial-number
        CreateAgent(ow, undefined, ad)
    enddo
```

The initial number of agent instances of an agent set is defined in its Agent-definition. The macro Createallagents is used during system initialization, and possibly during system execution, when agent instances containing agent sets themselves are created dynamically.

```
CREATEAGENT(ow:SDLAGENTSET, pa: [SDLAGENT], ad:Agent-type-definition) \equiv
    extend AGENT with sa
        INITAGENTCONTROLBLOCK(sa,ow, pa,ad)
        CREATEINPUTPORT(sa)
        sa.agentMode1 := initialisation
        sa.agentMode2 := initialising1
        sa.program := AGENT-PROGRAM
    endextend
where
```

```
InitAgentControlBlock(sa: SdLAGENt, ow:SdLAGENTSET, pa: [SdLAGENT],
```

InitAgentControlBlock(sa: SdLAGENt, ow:SdLAGENTSET, pa: [SdLAGENT],
ad:Agent-type-definition) $\equiv$
ad:Agent-type-definition) $\equiv$
sa.agentAS1 := ad
sa.agentAS1 := ad
sa.owner := ow
sa.owner := ow
sa.isActive $:=$ undefined
sa.isActive $:=$ undefined
sa.currentStartNodes $:=\varnothing$
sa.currentStartNodes $:=\varnothing$
sa.currentExitStateNodes $:=\varnothing$
sa.currentExitStateNodes $:=\varnothing$
sa.currentConnector $:=$ undefined
sa.currentConnector $:=$ undefined
sa.callingProcedureNode $:=$ undefined
sa.callingProcedureNode $:=$ undefined
sa.currentSignalInst $:=$ undefined
sa.currentSignalInst $:=$ undefined
sa.parent $:=$ if $p a \neq$ undefined then pa.selfPid else undefined endif
sa.parent $:=$ if $p a \neq$ undefined then pa.selfPid else undefined endif
sa.sender := nullPid
sa.sender := nullPid
sa.offspring := nullPid
sa.offspring := nullPid
sa.selfPid $:=\mathbf{m k}-P I D(s a$, undefined $)$
sa.selfPid $:=\mathbf{m k}-P I D(s a$, undefined $)$
if $p a \neq$ undefined then
if $p a \neq$ undefined then
pa.offspring := mk-PID(sa, undefined)
pa.offspring := mk-PID(sa, undefined)
endif
endif
let ownerDef: Agent-type-definition $=$

```
let ownerDef: Agent-type-definition \(=\)
```

```
                ow.agentAS1.s-Agent-type-identifier. idToNodeAS1 in
    if ownerDef. s-Agent-kind }\in{\mathrm{ {SYSTEM, BLOCK} then // containing agent set
        sa.stateAgent := sa
    elseif ownerDef.s-Agent-kind = PROCESS then // next level agent set
            sa.stateAgent := ow.owner.stateAgent
            else
        sa.stateAgent := sa
    endif
    endlet
endwhere
```

To create an agent, the controlled domain AGENT is extended. The control block of this new agent is initialized. An input port for receiving signals from other agents is created and attached to the new agent. The setting of agent modes and assignment of a program completes the creation of the agent.

```
AgEnt-Program:
if Self.agentModel = initialisation then
    INITAGENT
elseif Self.agentMode1 = execution then
    if Self.ExecRightPresent then
        EXECAGENT
    else
        GETEXEcRIGHT
    endif
endif
```

Depending on the current agent mode level 1, the activity phase is selected. After initialization, the agent is switched to the execution mode. Additionally, the agent synchronizes in case it belongs to a set of nested agents, in order to obtain an interleaving execution amongst these agents.

```
INITAGENT =
    let myDefinition: Agent-type-definition = Self.agentAS1.s-Agent-type-identifier.idToNodeAS1 in
    if Self.agentMode2 = initialising1 then
        CreateAgentVariables(Self,myDefinition )
        CreateAllAgentSets(Self, myDefinition )
        CREATESTATEMACHINE(myDefinition .s-State-machine)
        Self.agentMode2 := initialising2
    elseif Self.agentMode2 = initialising2 then
        CreateAllChannels(Self,myDefinition )
        // no implicit links (done by DeliverSignals)
        Self.agentMode2 := initialisingStateMachine
    elseif Self.agentMode2 = initialisingStateMachine then
        InITSTATEMACHINE
    elseif Self.agentMode2 = initialisationFinished then
        Self.agentModel := execution
        Self.agentMode2 := startPhase
    endif
    endlet
```

The initialization of agent instances starts in the "pre-initial state" and consists of four phases, triggered by agent modes. In the first phase, the inner "structure" of the agent is built up. This structure consists of the agent's local variable instances, its agent sets, and its state machine. A state machine is created even if it is not defined in the SDL-2010 specification; in this case, no behaviour is associated with the state machine. The information about this structure is drawn from the abstract syntax tree, in particular, from the part of tree representing the agent's type definition.

Once the structure of the agent has been created, channels and links are established. Next, the state machine is initialized, i.e., a "hierarchical inheritance state graph" modelling the agent's state machine is unfolded in a sequence of steps. Finally, execution is triggered by setting the agent modes.

Removal of an agent is modelled by resetting the program (and the owner) to undefined, and by removing all owned link agents.

## F3.2.3.1.4 Procedure creation and initialization

The creation of SDL-2010 procedure instances happens dynamically, during system execution. The creation as defined by the rule macro CreateProcedure leaves a procedure in what is called "preinitial" state.


Figure F3-5 - Activity phases of SDL-2010 agents: firing of transitions (level 4)

The initialization of a procedure is decomposed into a sequence of phases, as shown in the state diagram above. In each of these phases, certain parts of the procedure's structure are created. After procedure initialization, the agent execution is continued.

```
CreateProcedure(pd:Procedure-definition, vl: [VALUELABEL], cl:[CONTINUELABEL]) \equiv
    CreateProcedureGraph(pd, vl,cl)
    Self.agentMode3 := initialisingProcedure
    Self.agentMode4:= initialisingProcedureGraph
INITPROCEDURE \equiv
    if Self.agentMode4 = initialisingProcedureGraph then
        InITPROCEDUREGRAPH
    elseif Self.agentMode4 = initialisationFinished then
        Self.stateNodesToBeEntered :=
            {\mathbf{mk}-STATENODEWITHENTRyPoINT (Self.currentProcedureStateNode, undefined)}
        Self.agentMode3 := enteringStateNode
        Self.agentMode4 := startPhase
        Self.currentLabel:= undefined
    endif
```

The initialization of procedure instances starts in the "pre-initial state" and consists of two phases, triggered by agent modes. In the first phase, the inner "structure" of the procedure is built up. This structure consists of the procedure's local variable instances, and its state machine. The information about this structure is drawn from the abstract syntax tree, in particular, from the part of tree representing the procedure's type definition.
Once the structure of the procedure has been created, the state machine is initialized, i.e., a "hierarchical inheritance state graph" modelling the procedure's state machine is unfolded in a sequence of steps. Finally, execution is triggered by setting the agent modes, and by assigning the state node to be entered.

## F3.2.3.1.5 Gate creation

Exchange of signals between SDL-2010 agents is modelled by means of gates from a controlled domain GATE. A gate forms an interface for serial and unidirectional communication between two or more agents.

```
CrEATEALLGATES(ow:AGENT, atd: Agent-type-definition) \equiv
    do forall gd: gd \in atd.collectAllGateDefinitions
        CreateGate(ow,gd)
    enddo
    where
        collectAllGateDefinitions(atd: Agent-type-definition): Gate-definition-set =def
            if atd.s-Agent-type-identifier = undefined then
            atd.s-Gate-definition-set
            else
                    let typedef: Agent-type-definition = atd.s-Agent-type-identifier.idToNodeAS1 in
                    atd.s-Gate-definition-set }
            typedef.collectAllGateDefinitions
            endlet
            endif
    endwhere
```

SDL-2010 agent sets are created when the surrounding SDL-2010 agent is initialized right after its creation. For each gate definition found via collectAllGateDefinitions, a gate is created, taking inheritance into account.

```
CREATEGATE(ow:AGENT, gd:Gate-definition) =
    if gd.s-In-signal-identifier-set }=\varnothing\mathrm{ then
        extend GATE with g
            g.myAgent := ow
            g.gateAS1 := gd
            g.schedule := empty
            g.direction := inDir
        endextend
    endif
    if gd.s-Out-signal-identifier-set }=\varnothing\mathrm{ then
            extend GATE with g
                g.myAgent := ow
            g.gateAS1 := gd
            g.schedule := empty
            g.direction := outDir
        endextend
    endif
```

For each SDL-2010 gate, one or two elements of the controlled domain GATE (also called "gates") are added, depending on whether the gate is uni-directional or bi-directional. The decision of which gates to create is based upon the signal identifier sets in the inward and outward direction, respectively. For each gate, the owning agent, the AST node representing the gate definition, and the direction are assigned to the corresponding functions. Furthermore, the schedule, i.e., the sequence of signals waiting to be forwarded, is initialized to be empty.

```
CREATEINPUTPORT(ow:AGENT) \equiv
    extend GATE with g
        g.myAgent := ow
        g.gateAS1 := undefined
        g.schedule := empty
        g.direction := inDir
        ow.inport:= g
    endextend
```

As it has turned out, input ports have strong similarities with elements of the domain GATE (called "gates"). Therefore, input ports are modelled as gates, and the same functions are defined and initialized. In addition, the created gate explicitly becomes the input port of the owning agent.

## F3.2.3.1.6 Channel creation

Channels are modelled through unidirectional channel paths connecting a pair of gates.

```
CREATEALLChANNELS(ow:AGENT, atd:Agent-type-definition) \(\equiv\)
    do forall \(c d\) : \(c d \in\) atd.collectAllChannelDefinitions
        CREATECHANNEL(ow, cd)
    enddo
    where
        collectAllChannelDefinitions(atd: Agent-type-definition): Channel-definition-set \(=_{\text {def }}\)
            if atd.s-Agent-type-identifier \(=\) undefined then
                atd.s-Channel-definition-set
            else
                let typedef: Agent-type-definition = atd.s-Agent-type-identifier.idToNodeAS1 in
                atd.s-Channel-definition-set \(\cup\)
                typedef .collectAllChannelDefinitions
                endlet
            endif
    endwhere
```

Channels are created by agents during the second phase of their initialization. For each element found via collectAllChannelDefinitions, a channel is created, taking inheritance into account.

```
CREATECHANNEL(ow:AGENT, cd:Channel-definition) =
    do forall cp:cp\incd.s-Channel-path-set
        CreateChanNELPath(ow, cd.s-NODELAY, cp,cd)
```

Creating a channel amounts to creating the specified channel paths.

```
CREATECHANNELPATH(ow:AGENT, nd:[NODELAY], cp:Channel-path, cd:Channel-definition) \equiv
    let origDef: Gate-definition = cp.s-Originating-gate.idToNodeAS1 in
    let destDef: Gate-definition = cp.s-Destination-gate.idToNodeASl in
    choose fromGate: fromGate \inGATE ^ fromGate.gateASI= origDef ^
        (OuterGate(ow, fromGate, inDir) \vee InnerGate(ow, fromGate, outDir) )
        choose toGate: toGate \in GATE ^ toGate.gateASl = destDef ^
            (OuterGate(ow, toGate, outDir) \vee InnerGate(ow, toGate, inDir) )
            CREATELINK(ow,fromGate, toGate, nd, cp.s-Signal-identifier-set, cd)
        endchoose
    endchoose
    where
        OuterGate(ow: AGENT, g: GATE, dir: DIRECTION): BOOLEAN = def
            g.myAgent =ow.owner }\wedge\mathrm{ g.direction = dir
        InnerGate(ow: AGENT, g: GATE, dir: DIRECTION): BOOLEAN = = def
            g.myAgent.owner =ow \wedge g.direction = dir
    endwhere
```

A channel path is modelled as a link between two gates. The gates to be connected have already been created together with their agent sets. Originating and destination gates are distinguished, which defines the direction of the channel path. The correspondence between gate identifiers (referring to the AST) and gate instances is obtained by exploiting the functions myAgent and direction defined on gates.

## F3.2.3.1.7 Link creation and removal

Agents of type LINK model the transport of signals. The behaviour of link agents is defined by the ASM program Link-Program.

In addition to modelling explicit channel paths, links are used to model implicit channel paths that connect input gates (as defined by the derived function ingates) with the input port of an agent.

```
CREATELINK(ow:AGENT, fromGate:GATE, toGate:GATE, nd:[NODELAY], w:In-signal-identifier-set,
    \(c d:[\) Channel-definition \(]) \equiv\)
    extend LINKwith \(l\)
        l.channelAS1 := cd
        l.owner := ow
        l.from := fromGate
        l.to := toGate
        l.noDelay := nd
        l.with := w
        l.program := LINK-PROGRAM
    endextend
LINK-PRoGRAM:
        if Self.from.queue \(\neq\) empty then
            let \(s i=\) Self.from.queue.head in
                if applicable(si.signalType,si.toArg,si.viaArg,Self.from,Self) then
                DELETE(si,Self.from)
                Insert(si,now+Self.delay,Self.to)
                si.viaArg := si.viaArg \}
                        \{Self.from.gateAS1.identifier \({ }_{1}\),
                                Self.channelAS1.identifier \(\left.{ }_{1}\right\}\)
                endif
            endlet
        endif
```

A link agent models the connection between a pair of gates. Since links are finally combined into channel paths and channels, respectively, a delay characteristic is associated with them. Also, the signals that can be transported by the link are determined. Link-Program defines the dynamic behaviour of link agents.

```
REMOVEALLLINKS(ow:AGENT) \equiv
    do forall l:l\inLINK^ l.owner =ow
        REmOvELINK(l)
    enddo
REMOVELINK(l:LINK) \equiv
    l.program := undefined
    l.owner := undefined
```

Removal of a link agent is modelled by deleting the program and the owner.

## F3.2.3.1.8 Variable creation

For each agent, composite state, procedure, and compound node instance, a set of local variables may be declared in an SDL-2010 specification. This leads to nested scopes, where a scope is associated with each refined state node.

```
CreateAgentVARIABLES(sa:SDLAGENT, atd:Agent-type-definition) \equiv
    extend StateID with sid
        sa.topStateId := sid
        if sa.stateAgent = sa then
            sa.state := initAgentState(undefined, sid,undefined,atd.collectAllVariableDefinitions)
        else
            sa.stateAgent.state := initAgentState(sa.stateAgent.state,
```

```
            sid, sa.owner.owner.topStateId, atd.collectAllVariableDefinitions)
    endif
endextend
where
    collectAllVariableDefinitions(atd: Agent-type-definition):Variable-definition-set = =ef
        if atd.s-Agent-type-identifier = undefined then
            atd.s-Variable-definition-set
        else
            let typedef: Agent-type-definition = atd.s-Agent-type-identifier.idToNodeAS1 in
            atd.s-Variable-definition-set }
            typedef.collectAllVariableDefinitions
            endlet
        endif
endwhere
```

The outermost scope is associated with the top-level state node of an agent. It is created together with that state node. In case of nested process agents, the scopes of contained agents are added to the scope of the outermost agent.

```
CreateCompositeStateVariables(sa:SdlAGEnt, sn:StateNode,
    cstd:Composite-state-type-definition) \equiv
    extend STateID with sid
        sn.stateId := sid
        sa.stateAgent.state := initAgentState(sa.stateAgent.state, sid,
            if sn.parentStateNode = undefined then sn.parentStateNode.stateId else undefined endif,
            cstd.collectAllVariableDefinitions1)
    endextend
    where
        collectAllVariableDefinitionsl(cstd: Composite-state-type-definition):
            Variable-definition-set = def
            if cstd.s-Composite-state-type-identifier = undefined then
            cstd.s-Variable-definition-set
            else
            let typedef: Composite-state-type-definition =
                    cstd.s-Composite-state-type-identifier.idToNodeAS1 in
            cstd.s-Variable-definition-set \cup
            typedef .collectAllVariableDefinitions1
            endlet
            endif
    endwhere
```

With each composite state, a new scope is associated, which is located below the scope of the parent state node.

```
CREATEPROCEDUREVARIABLES(sa:SDLAGENT, sn:STATENODE, pd:Procedure-definition) \equiv
    extend StateId with sid
    sn.stateId := sid
    let outParams: Out-parameter* = < p in pd.collectAllProcedureFPars:
                    ( }p\in\mathrm{ Out-parameter)> in
    sa.stateAgent.state := initProcedureState(sa.stateAgent.state, sid,
        sn.parentStateNode.stateId, pd.collectAllVariableDefinitions2,
        pd.collectAllProcedureFPars, empty,
        < p.s-Parameter.identifier }|\mathrm{ | in outParams>)
    endlet
    endextend
    where
        collectAllVariableDefinitions2(pd: Procedure-definition): Variable-definition-set =def
            if pd.s-Procedure-identifier = undefined then
                pd.s-Variable-definition-set
```

```
    else
        let procdef: Procedure-definition = pd.s-Procedure-identifier.idToNodeAS1 in
        pd.s-Variable-definition-set }
        procdef.collectAllVariableDefinitions2
        endlet
    endif
    collectAllProcedureFPars(pd:Procedure-definition): Procedure-formal-parameter* = def
    if pd.s-Procedure-identifier = undefined then
        pd.s-Procedure-formal-parameter-seq
    else
        let procdef: Procedure-definition = pd.s-Procedure-identifier.idToNodeAS1 in
        procdef.collectAllProcedureFPars}
        pd.s-Procedure-formal-parameter-seq
        endlet
    endif
endwhere
```

With each procedure state, a new scope is associated, which is located below the scope of the parent state node.

```
CrEATECompoundNodEVARIABLES(sa:SDLAGENT, scope: SCOPE) \equiv
    extend STATEID with sid
        sa.currentStateId := sid
        scopeName(Self, sid) := scope.s-Connector-name
        scopeContinueLabel(Self, sid) := scope.s-ConTINUELABEL
        scopeStepLabel(Self, sid) := scope.s-STEPLABEL
        sa.stateAgent.state := initAgentState(sa.stateAgent.state, sid,
            sa.currentStateId, scope.s-Variable-definition-set)
    endextend
```

With each compound node, a new scope is associated, which is located below the current scope.

## F3.2.3.1.9 State machine creation and initialization

The behaviour of an SDL-2010 agent is given by a state machine, which may be omitted if the agent is passive. This state machine is modelled as a "hierarchical inheritance graph", which is unfolded recursively.

```
CREATESTATEMACHINE(smd:[State-machine]) \equiv
    CreateTopStatePartition(smd)
```

When an SDL-2010 agent is created, the macro CreateStateMachine is applied with the effect that the root node (topStateNode) of the "hierarchical inheritance state graph" is created. If the SDL-2010 agent has behaviour, the root node is refined (and possibly specialized) subsequently. If the agent is passive, no refinement is made. The unfolding of the graph is treated by the macro InitStateMachine.

If an SDL-2010 agent has behaviour, a "hierarchical inheritance state graph" modelling the agent's state machine is built, node-by-node. This graph forms the basis for entering and leaving states, and for selecting transitions. Inheritance is taken into account during execution, and is not handled by transformations. The unfolding of the graph is controlled by the following macro.

```
INITSTATEMACHINE \equiv
    if Self.stateNodesToBeCreated }\not=\varnothing\mathrm{ then
        CrEateStateNode
    elseif Self.statePartitionsToBeCreated }\not=\varnothing\mathrm{ then
        CreateStatePartition
    elseif Self.stateNodesToBeSpecialised }\not=\varnothing\mathrm{ then // these are composite states!
        CreatEInHERITEDSTATE
    elseif Self.stateNodesToBeRefined }\not=\varnothing\mathrm{ then
```

CreateStateRefinement
else
Self.agentMode2 := initialisationFinished
endif
Nodes to be created are kept in the agent's state components stateNodesToBeCreated, statePartitionsToBeCreated, stateNodesToBeSpecialised, and stateNodesToBeRefined, and are treated in that order. Unfolding of the graph updates these state components and ends with the graph being completed, i.e., no further nodes to be created.

## F3.2.3.1.10 Procedure graph creation and initialization

The behaviour of a procedure is given by a procedure graph. This procedure graph is modelled as a "hierarchical inheritance graph", which is unfolded recursively.

CREATEPRocedureGraph(pd:Procedure-definition, vl:[VALUELABEL], cl:CoNTINUELABEL) $\equiv$ CreateProcedureStateNode $(p d, v l, c l)$

When a procedure is called, the macro CreateProcedureGraph is applied with the effect that the root node of the "hierarchical inheritance state graph" modelling the procedure is created. The unfolding of the graph is treated by the macro InitProcedureGraph.

```
INITPROCEDUREGRAPH \equiv
    if Self.stateNodesToBeCreated }\not=\varnothing\mathrm{ then
        CreateStateNode
    elseif Self.statePartitionsToBeCreated }\not=\varnothing\mathrm{ then
        CreateStatePartition
    elseif Self.stateNodesToBeSpecialised }\not=\varnothing\mathrm{ then // these are composite states!
        CrEATEINHERITEDSTATE
    elseif Self.stateNodesToBeRefined }\not=\varnothing\mathrm{ then
        CREATESTATEREFINEMENT
    else
        Self.agentMode4 := initialisationFinished
    endif
```

Nodes to be created are kept in the agent's state components stateNodesToBeCreated, statePartitionsToBeCreated, stateNodesToBeSpecialised and stateNodesToBeRefined, and are treated in that order. Unfolding of the graph updates these state components and ends with the graph being completed, i.e., no further nodes to be created.

## F3.2.3.1.11 State node creation

The creation of state nodes is modelled by extending the controlled domain StateNode. A macro is defined to handle the creation of state nodes. State partitions are also modelled as elements of the domain STATENODE, but are not treated in this clause.

```
CREATESTATENODE \equiv
    choose snd: snd \in Self.stateNodesToBeCreated
        Self.stateNodesToBeCreated := Self.stateNodesToBeCreated \{snd}
        extend STATENODE with sn
            sn.stateAS1 := snd // used, e.g., as argument for startLabel
            sn.owner:= Self
            sn.parentStateNode := Self.currentParentStateNode
            sn.stateNodeKind := stateNode
            sn.stateName := snd.s-State-name
            sn.stateTransitions := snd.getStateTransitions
            sn.startTransitions := \varnothing // updated if the state node is refined
            if snd.s-Composite-state-type-identifier }=\mathrm{ undefined then
                Self.stateNodesToBeRefined := Self.stateNodesToBeRefined }\cup{sn
                    Self.stateNodesToBeSpecialised := Self.stateNodesToBeSpecialised }\cup{sn
                    let parent: Composite-state-type-definition=
```

```
            snd.s-Composite-state-type-identifier.idToNodeAS1 in
                        sn.stateDefinitionAS1 := parent
                endlet
            endif
    endextend
endchoose
```

State nodes are created as part of a state transition graph, which is unfolded node by node. The nodes to be created are kept in the agent's state component stateNodesToBeCreated. If that set is not empty, this means that the unfolding of a state transition graph is currently in progress, and some element of the set is chosen. When a state node is created, its bookkeeping information is initialized. Since being a regular state node, the created state node may have a substructure; it is included in the set of state nodes to be refined.

```
CreateProcedureStateNode(pd:Procedure-definition, vl:[VALUELABEL], cl:CoNTINUELABEL) \(\equiv\)
    extend STATENODE with sn
        sn.procedureAS1 := pd
        sn.owner := Self
        sn.parentStateNode \(:=\) Self.currentParentStateNode
        sn.stateNodeKind \(:=\) procedureNode
        sn.stateName := mk-Name("")
        sn.stateTransitions \(:=\varnothing\)
        sn.startTransitions \(:=\varnothing \quad / /\) updated if the state node is refined
        sn.resultLabel := vl
        Self.stateNodesToBeRefined \(:=\{s n\}\)
        Self.stateNodesToBeCreated \(:=\varnothing\)
        Self.statePartitionsToBeCreated \(:=\varnothing\)
        Self.stateNodesToBeSpecialised \(:=\{s n\}\)
        Self.currentProcedureStateNode \(:=s n\)
        Self.callingProcedureNode \(:=\) sn
        CreateProcedureVariables(Self,sn,pd)
        SaveProcedureControlBlock( \(s n, c l\) )
    endextend
```

Procedure state nodes are the top-level nodes of a procedure graph, which is unfolded node by node subsequently. These nodes are created dynamically, when a procedure call is made. Thus, recursive procedure calls can be handled in a uniform way.

## F3.2.3.1.12 State partition creation

The creation of state partitions is modelled by extending the controlled domain STATENODE. Several macros are defined to handle the creation of various kinds of state partitions, namely the top state partition, (regular) state partitions, and state partitions introduced to model inheritance.

```
CREATETOPSTATEPARTITION(smd:[State-machine]) \equiv
    extend StateNode with sn
    sn.owner := Self
    Self.topStateNode := sn
    sn.parentStateNode := undefined
    sn.stateNodeKind := statePartition
    sn.stateTransitions := \varnothing
    sn.startTransitions:= \varnothing // updated if the state partition is refined
    if smd }\not==\mathrm{ undefined then
            let parent: Composite-state-type-definition =
                smd.s-Composite-state-type-identifier.idToNodeAS1 in
                sn.stateDefinitionAS1 := parent
            endlet
            sn.stateName := smd.s-State-name
            Self.stateNodesToBeRefined := {sn}
            Self.stateNodesToBeSpecialised := {sn}
        else
```

```
    sn.stateName := mk-Name("^pdummy^p")
    Self.stateNodesToBeRefined := 
    Self.stateNodesToBeSpecialised := 
    endif
    Self.stateNodesToBeCreated := \varnothing
    Self.statePartitionsToBeCreated := \varnothing
endextend
```

The unfolding of the "hierarchical inheritance state graph" modelling an agent's state machine starts with the creation of the root node, as defined by the macro CreateTopStatePartition. When a root node is created, its bookkeeping information is initialized. In particular, the root node is classified as a state partition. If the agent has behaviour, the root node has a substructure, and is therefore included in the set of state nodes to be refined. Further state components of the agent are reset before starting the unfolding of the graph.

```
CREATESTATEPARTITION \equiv
    choose spd: spd \in Self.statePartitionsToBeCreated
        Self.statePartitionsToBeCreated := Self.statePartitionsToBeCreated \{spd}
        extend STATENODE with sn
            sn.partitionAS1 := spd // used, e.g., as argument for startLabel
            sn.owner := Self
            sn.parentStateNode := Self.currentParentStateNode
            sn.stateNodeKind := statePartition
            sn.stateName := spd.s-Name
            sn.stateTransitions := \varnothing
            sn.startTransitions := \varnothing // updated if the state partition is refined
            do forall }cd\mathrm{ : cd }\in\mathrm{ spd.s-Connection-definition-set
            if cd E Entry-connection-definition then
                    entryConnection(cd.s-Outer-entry-point.adaptEntryPoint, sn) :=
                        adaptEntryPoint(cd.s-Inner-entry-point)
            elseif cd \in Exit-connection-definition then
                exitConnection(cd.s-Inner-exit-point, sn) := cd.s-Outer-exit-point
                    endif
            enddo
            Self.currentParentStateNode.statePartitionSet :=
            Self.currentParentStateNode.statePartitionSet }\cup{sn
            Self.stateNodesToBeRefined := Self.stateNodesToBeRefined }\cup{sn
            Self.stateNodesToBeSpecialised := Self.stateNodesToBeSpecialised }\cup{sn
        endextend
    endchoose
    where
        adaptEntryPoint(entry: Name }\cup\mathrm{ DEFAULT): STATEENTRYPOINT = def
            if entry = DEFAULT then undefined else entry endif
    endwhere
```

(Regular) state partitions are created as part of a state aggregation node, which is unfolded node by node. The partitions to be created are kept in the agent's state component statePartitionsToBeCreated. If that set is not empty, this means that the unfolding of a state aggregation node is currently in progress, and some element of the set is chosen. When a state partition is created, its bookkeeping information is initialized. Modelling a state partition, the created state node may have a substructure, and is therefore included in the set of state nodes to be refined.

## CREATEINHERITEDSTATE $\equiv$

choose sns: sns $\in$ Self.stateNodesToBeSpecialised Self.stateNodesToBeSpecialised $:=$ Self.stateNodesToBeSpecialised $\backslash\{$ sns $\}$ let $c s t d$ : Composite-state-type-definition $=$ sns.stateDefinitionAS1 in if cstd.s-Composite-state-type-identifier $\neq$ undefined then
let parent: State-node $=c s t d . \mathrm{s}$-Composite-state-type-identifier.idToNodeAS1 in

```
        extend StateNode with sn
                        sn.stateAS1 := parent
                        sn.owner := Self
                sn.parentStateNode := sns.parentStateNode
                sn.stateNodeKind := sns.stateNodeKind
                sn.stateName := sns.stateName
                sn.stateTransitions:= 
                sn.startTransitions := \varnothing // updated if the state node is refined
                sns.inheritedStateNode := sn
                Self.stateNodesToBeRefined := Self.stateNodesToBeRefined }\cup{sn
                Self.stateNodesToBeSpecialised := Self.stateNodesToBeSpecialised }\cup{sn
        endextend
        endlet
    else
        sns.inheritedStateNode := undefined
            endif
    endlet
endchoose
```

Specialization of composite state types is modelled by adding another dimension to the hierarchical state graph, yielding a "hierarchical inheritance state graph". Formally, specialization is a relation between composite state types. In the state graph, it is modelled by an inheritance relation among state node instances. More specifically, if a state node is refined, and the refinement is defined using specialization, then a root node that is inherited by the refined state node, and has the composite state type being specialized, is created. By adding the root node to the set of state nodes to be refined, a "hierarchical inheritance state graph" modelling the specialization is subsequently attached to this root node.

## F3.2.3.1.13 Composite state creation

All (regular) state nodes, state partitions, and procedure nodes are candidates for refinement and, if refined, for specialization. Refinements are defined by a composite state type, which includes another composite state type in case of specialization. In this clause, several macros treating these aspects are introduced.

```
CREATESTATEREFINEMENT \equiv
    choose snr: snr \in Self.stateNodesToBeRefined
        Self.stateNodesToBeRefined := Self.stateNodesToBeRefined \ {snr}
        Self.currentParentStateNode := snr
        if snr.stateNodeKind = procedureNode then
            CrEATEPRoCEDUREVARIABLES(Self, snr, snr.procedureASl)
            CreateProcedureGraphNodeS(snr, snr.procedureAS1.s-Procedure-graph)
        else
            let parent: Composite-state-type-definition = snr.stateDefinitionAS1 in
            CREATECOMPOSITESTATEV ARIABLES(Self, snr,
                parent)
            CreateCompositeState(snr,
                parent)
            endlet
        endif
    endchoose
```

When a state node, state partition, or procedure node is created, it is added to a set of state nodes to be refined. In the macro CreateStateRefinement, an arbitrary element of this set is selected, and it is checked whether a refinement applies. Refinements are then treated by the macro CreateCompositeState.

```
CREATECOMPOSITESTATE(sn:STATENODE, cstd:Composite-state-type-definition) \(\equiv\)
    let \(s r=c s t d\). s-implicit in
        if \(s r \in\) Composite-state-graph then
            CreateCompositeStateGraph \((s n, s r)\)
```

elseif $s r \in$ State-aggregation-node then
CreateStateAgaregationNode ( $s n, s r$ )
endif
endlet
If a state is structured, it is refined into either a composite state graph or a state aggregation node. Based on this distinction, further rule macros are applied.

```
CREATECOMPOSITESTATEGRAPH(psn:STATENODE, csgd:Composite-state-graph) \equiv
    psn.stateNodeRefinement := compositeStateGraph
    psn.startTransitions := getStartTransitions({csgd.s-State-transition-graph.s-State-start-node})}
        getStartTransitions(csgd.s-Named-start-node-set)
    psn.freeActions:= getFreeActions(csgd.s-State-transition-graph.s-Free-action-set)
    CrEATESTATETRANSITIONGRAPH(psn,csgd.s-State-transition-graph.s-State-node-set)
```

Creating a composite state graph means creating its state transition graph.

```
CrEateStateTransitionGraph(psn:StateNode, nodes: State-node-set ) \equiv
    Self.stateNodesToBeCreated := nodes
    Self.currentParentStateNode := psn
```

Creating a state transition graph means creating its state nodes. Creation of state nodes is performed in a series of subsequent ASM steps. These steps are triggered by assigning the state node definitions to the agent's state component stateNodesToBeCreated.

```
CREATEPROCEDUREGRAPHNODES(psn:STATENODE, pg:Procedure-graph) \equiv
    psn.stateNodeRefinement := compositeStateGraph
    psn.startTransitions := getStartTransitions({pg.s-Procedure-start-node})
    psn.freeActions := getFreeActions(pg.s-Free-action-set)
    CrEATESTATETRANSITIONGRAPH(psn, pg.s-State-node-set)
    Self.stateNodesToBeCreated := pg.s-State-node-set
    Self.currentParentStateNode := psn
```

Creating a procedure graph means creating its state nodes.

```
CREATESTATEAGGREGATIONNODE(psn:STATENODE, sand:State-aggregation-node) \equiv
    psn.stateNodeRefinement := stateAggregationNode
    Self.statePartitionsToBeCreated := sand.s-State-partition-seq.toSet
    Self.currentParentStateNode := psn
    psn.statePartitionSet := \varnothing
```

Creating a state aggregation node means creating its state partitions, which is performed in a series of subsequent ASM steps. These steps are triggered by assigning the state partition definitions to the agent's state component statePartitionsToBeCreated.

## F3.2.3.2 System execution

After initialization, SDL-2010 agents start their execution. The execution of the system is modelled by the concurrent execution of all its agents.

## F3.2.3.2.1 Agent set execution

```
ExECAGENTSET =
    let child = take ({ag \inSDLAGENT: ag.owner = Self ^ag.agentMode1 = initialisation }) in
        if child = undefined then
            DELIVERSIGNALS
        endif
    endlet
```

The behaviour of agent sets is formalized below.

```
choose g: g\in Self.ingates ^g.queue = empty
    let si=g.queue.head in
        DELETE(si,g)
        if si.toArg \inPID ^ si.toArg }\not=\mathrm{ undefined then
            choose sa: sa \in SDLAGENT ^ sa.owner = Self ^ sa.selfPid = si.toArg
                INSERT(si, si.arrival, sa.inport)
            endchoose
        else
            choose sa: sa }\in\mathrm{ SDLAGENT ^ sa.owner = Self
                INSERT(si, si.arrival, sa.inport)
            endchoose
        endif
    endlet
endchoose
```


## F3.2.3.2.2 Agent execution

The execution of SDL-2010 agents is modelled by a start phase followed by alternating phases, namely transition selection and transition firing. To distinguish between these phases, corresponding agent modes are defined. When in agent mode selectingTransition (agentMode2), the agent attempts to select a transition, obeying a number of constraints. In agent mode firingTransition, a previously selected transition is fired.


Figure F3-6 - Activity phases of SDL-2010 agents: execution (level 2)
An agent reaches the execution phase after it has completed its initialization. The execution phase consists of three sub-phases as shown in the state diagram. Two of these sub-phases will in turn be refined, which is indicated by the double line.

```
ExEcAGENT =
    if Self.agentMode2 = startPhase then
        EXECUTIONSTARTPHASE
    elseif Self.agentMode2 = firingTransition then
        FireTransition
    elseif Self.agentMode2 = selectingTransition then
        SelectTransition
    elseif Self.agentMode2 = stopping then
        StopPHASE
    endif
```

The execution of agents is given by the rule macro ExECAgent. Depending on the current agent mode, the corresponding execution phases are selected.

GETExECRIGHT $\equiv$
if Self.stateAgent.isActive $=$ undefined then Self.stateAgent.isActive $:=$ Self
endif

```
RETURNEXECRIGHT \equiv
    Self.stateAgent.isActive := undefined
ExecRightPresent(sa:SDLAGENT): BOOLEAN = def
    let myDef: Agent-type-definition = sa.owner.agentAS1.s-Agent-type-identifier.idToNodeAS1 in
    sa.stateAgent.isActive = sa \vee myDef.s-Agent-kind \in{BLOCK, SYSTEM}
    endlet
```


## F3.2.3.2.3 Starting agent execution

When the execution phase starts, several initializations are made: the set of state nodes to be entered is initialized to consist of the top state node; furthermore, the execution is switched to entering state nodes.

```
EXECUTIONSTARTPHASE \equiv
    Self.isActive := undefined
    Self.stateNodesToBeEntered :=
        {\mathbf{mk}-StateNodEWithEntryPoint (Self.topStateNode,undefined)}
    Self.agentMode2 := firingTransition
    Self.agentMode3 := enteringStateNode
    Self.agentMode4 := startPhase
    Self.currentLabel := undefined
```


## F3.2.3.2.4 Transition selection

In agent mode selectingTransition (agentMode2), an SDL-2010 agent searches for a fireable transition. SDL-2010 imposes certain rules on the search order. For instance, priority input signals have to be checked before ordinary input signals, and these have in turn to be checked before continuous signals can be consumed. Furthermore, a transition emanating from a substate has higher priority than a conflicting transition emanating from any of the containing states. Finally, redefined transitions take precedence over conflicting inherited transitions. These and some more constraints have to be observed when formalizing the transition selection.


Figure F3-7 - Activity phases of SDL-2010 agents: selecting transition (level 3)

In order to structure the transition selection, several agent mode levels are defined. The uppermost level is shown in the diagram, where the agent mode selectingTransition is refined into four sub-modes (agentMode3). Some of these sub-modes will in turn be refined later.

```
SELECtTRANSITION \equiv
    if Self.agentMode3 = startSelection then
        SelectTransitionStartPhase
```

```
elseif Self.agentMode3 = selectStartTransition then
        SELECTSTARTTRANSITION
elseif Self.agentMode3 = selectExitTransition then
        SelectExitTransition
elseif Self.agentMode3 = selectFreeAction then
        SelectFreeAction
elseif Self.agentMode3 = selectPriorityInput then
        SelectPriorityInput
elseif Self.agentMode3 = selectInput then
        Selectinput
elseif Self.agentMode3 = selectContinuous then
        SelectContinuous
endif
```

Transition selection starts with an attempt to select a start transition, free action, priority input, an ordinary input, and finally, a continuous signal (in that order). If no transition has been selected, the selection process is repeated/aborted. The evaluation of provided expressions and continuous expressions may alter the local state of the process, which may lead to different results depending on the evaluation order.

```
TRANSITIONFOUND(t:SEMTRANSITION) \equiv
    Self.currentParentStateNode := Self.stateNodeChecked.parentStateNode
    Self.previousStateNode := Self.stateNodeChecked
    Self.currentStateId := Self.stateNodeChecked.parentStateNode.stateId
    Self.currentLabel := t.s2-LABEL // second label
    Self.agentMode2 := firingTransition
    Self.agentMode3:= firingAction
    RETURNEXECRIGHT
```

As soon as a selectable transition is found, the start label of the transition is assigned, and the agent modes are set to firingTransition and firingAction, respectively. Also, the current parent state node is set, which determines the current state name scope. This scope information is used when an Enterstatenode-primitive is evaluated.

```
STARTTRANSITIONFOUND( }t:STARTTRANSITION, psn:STATENODE) 
    Self.currentParentStateNode := psn
    Self.currentStateId := psn.stateId
    Self.currentLabel := t.s-LABEL
    Self.agentMode2 := firingTransition
    Self.agentMode3 := firingAction
    RETURNEXECRIGHT
```

As soon as a selectable start transition is found, the start label of the transition is assigned, and the agent modes are set to firingTransition and firingAction, respectively. Also, the current parent state node is set, which determines the current state name scope. This scope information is used when an EnterStateNode-primitive is evaluated.

```
ExitTransitionFound (et:SemTransition, psn:STATENODE) \(\equiv\)
    Self.currentParentStateNode \(:=p s n\)
    Self.currentStateId := psn.stateId
    Self.currentLabel := et.s-LABEL
    Self.agentMode 2 := firingTransition
    Self.agentMode3 \(:=\) firingAction
    ReturnExecRight
```

As soon as a selectable exit transition is found, the start label of the transition is assigned, and the agent modes are set to firingTransition and firingAction, respectively. Also, the current parent state node is set, which determines the current state name scope. This scope information is used when a LeavestateNode-primitive is evaluated.

Self.currentParentStateNode $:=p s n$
Self.currentStateId := psn.stateId
Self.currentLabel $:=$ fa.s-LABEL
Self.agentMode2 := firingTransition
Self.agentMode3 := firingAction
Returnexecright
As soon as a free action is found, the start label of the transition is assigned, and the agent modes are set to firingTransition and firingAction, respectively. Also, the current parent state node is set, which determines the current state name scope.

## F3.2.3.2.5 Starting selection of transitions

When the selection of transition starts, several initializations are made: the input port is "frozen", meaning that its state at the beginning of the selection is the basis for this selection cycle. This does not prevent signal instances to arrive while the selection is active; however, these signals will not be considered before the next selection cycle. Furthermore, the selection is switched to checking priority signals.

```
SelectTransitionStartPhase \(\equiv\)
    if Self.currentStartNodes \(\neq \varnothing\) then
        Self.stateNodeChecked \(:=\) undefined
        Self.agentMode3 \(:=\) selectStartTransition
    elseif Self.currentExitStateNodes \(\neq \varnothing\) then
        Self.stateNodeChecked \(:=\) undefined
        Self.agentMode3 \(:=\) selectExitTransition
    elseif Self.currentConnector \(\neq\) undefined then
        Self.agentMode3 := selectFreeAction
    else
        Self.inputPortChecked := Self.inport.queue
        Self.agentMode3 \(:=\) selectPriorityInput
        Self.agentMode 4 := startPhase
    endif
```


## F3.2.3.2.6 Start transition selection

Selection of a start transition is performed by checking, for all current start nodes, whether a start transition can be selected.

```
SELECTSTARTTRANSITION \equiv
    if Self.stateNodeChecked = undefined then
        let snwen = take(Self.currentStartNodes) in
            if snwen }=\mathrm{ undefined then
                Self.currentStartNodes := Self.currentStartNodes \{snwen}
                Self.startNodeChecked := snwen
                Self.stateNodeChecked := snwen.s-STATENODE
            endif
        endlet
    else
        let t= take({tr \in Self.stateNodeChecked.startTransitions:
            tr.s-STATEENTRYPOINT = Self.startNodeChecked.s-implicit }) in
            if }t\not=\mathrm{ undefined then
                StartTransitionFound(t, Self.startNodeChecked.s-STATENODE)
            else
                Self.stateNodeChecked :=
                                    take({sn1 \in Self.stateNodesToBeChecked:
                                    directlyInheritsFrom(Self.stateNodeChecked,sn1)})
            endif
        endlet
    endif
```

Start transitions are associated directly with the refined node, and are distinguished by their state entry point.

## F3.2.3.2.7 Exit transition selection

```
SeLectExitTransition \equiv
    let snwex = take(Self.currentExitStateNodes) in
    if Self.stateNodeChecked = undefined then
            if snwex = undefined then
                Self.currentExitStateNodes := Self.currentExitStateNodes \{snwex}
                Self.exitNodeChecked := snwex
                Self.stateNodeChecked := snwex.s-STATENODE
            endif
    else
        let t= take({tr \in Self.stateNodeChecked.stateTransitions.exitTransitions:
            tr.s-STATEExITPoINT = Self.exitNodeChecked.s-STATEEXITPOINT}) in
            if }t\not=\mathrm{ undefined then
                ExitTransitionFound (t,snwex.s-STATENODE)
            else
                Self.stateNodeChecked :=
                take({sn1 \in Self.stateNodesToBeChecked:
                                    directlyInheritsFrom(Self.stateNodeChecked,sn1)})
            endif
        endlet
    endif
    endlet
```

Exit transitions are associated with the containing node, and are distinguished by their state exit point.

## F3.2.3.2 $\mathbf{8}$ Free action selection

```
SELECTFREEACTION \equiv
    let fa = take({elem }\in\mathrm{ Self.stateNodeChecked.freeActions:
        elem.s-Connector-name = Self.currentConnector.s-Connector-name}) in
        if fa\not= undefined then
            Self.currentConnector:= undefined
            FreeActionFound(fa, Self.currentParentStateNode)
        else
            Self.stateNodeChecked :=
                take({sn1 \in Self.stateNodesToBeChecked:
                            directlyInheritsFrom(Self.stateNodeChecked,sn1)})
        endif
    endlet
```

Free actions are associated directly with the refined node, and are distinguished by their connector name.

## F3.2.3.2.9 Priority input selection

Selection of a priority input is performed by checking, for each signal instance of the agent's input port, all current state nodes. Inheritance is taken into account by checking, for each state node, the inherited state nodes.


Figure F3-8 - Activity phases of SDL-2010 agents: selecting priority inputs (level 4)
The selection of a priority input consists of the sub-phases (agentMode4) shown in the diagram. At any time during the selection phase, an attempt to select a spontaneous signal may be made, depending on the value of the monitored predicate Self.spontaneous.

```
SELECTPRIORITYINPUT \equiv
    if Self.agentMode4 = startPhase then
        SelPRIORITYINPUTSTARTPHASE
    elseif Self.agentMode4 = selectionPhase then
        SelPriorityInputSelectionPhase
    elseif Self.agentMode4= selectSpontaneous then
        SElECTSPONTANEOUS
    endif
```

This ASM macro defines the upper level control structure of the priority input selection. Depending on the agent mode agentMode4, further action is defined in the corresponding ASM macro. This control structure is part of the previous state diagram.

```
SELPRIORITYInPUTSTARTPHASE \equiv
    if Self.inputPortChecked # empty then
        Self.signalChecked := Self.inputPortChecked.head
        Self.SignalSaved := false
        Self.stateNodesToBeChecked := collectCurrentSubStates(Self.topStateNode)
        Self.stateNodeChecked := undefined
        Self.agentMode4:= selectionPhase
    else
        Self.agentMode3 := selectContinuous
        Self.agentMode4 := startPhase
        RETURNEXECRIGHT
    endif
```

When the selection starts, it is checked whether the input port carries signals. If so, several initializations are made: the first signal instance to be checked is determined, the state nodes to be checked are set, and the selection is activated. If the input port is empty, the selection of continuous signals is triggered.

```
SELPRIORITYINPUTSELECTIONPHASE \equiv
    if Self.stateNodeChecked = undefined then
        NextStateNodeToBeChecked
    elseif Self.spontaneous then
        Self.agentMode4 := selectSpontaneous
        Self.agentMode5 := selectionPhase
    else
        let t= take({tr \in Self.stateNodeChecked.stateTransitions.priorityInputTransitions:
            tr.s-SIGNAL = Self.signalChecked.signalType }) in
            if }t\not=\mathrm{ undefined then
            Self.currentSignalInst := Self.signalChecked
            Self.sender := Self.signalChecked.signalSender
```

```
                DELETE(Self.signalChecked, Self.inport)
                TRANSITIONFOUND( }t
            else
                Self.stateNodeChecked := undefined
            endif
    endlet
endif
where
    NEXTSTATENODETOBECHECKED \equiv
    if Self.stateNodesToBeChecked }\not=\varnothing\wedge\neg\mathrm{ Self.SignalSaved then
                SelectNextStateNode
    else
            NEXTSIGNALTOBECHECKED
            Self.stateNodesToBeChecked := collectCurrentSubStates(Self.topStateNode)
            Self.stateNodeChecked := undefined
    endif
    SelectNEXtSTATENODE \equiv
    let sn=Self.stateNodesToBeChecked.selectNextStateNode in
        if }sn=\mathrm{ undefined then
            UNDEFINEDBEHAVIOUR
            elseif sn.stateNodeKind = procedureNode then
                Self.stateNodesToBeChecked := Self.stateNodesToBeChecked \
                    collectCurrentSubStates(sn.getPreviousStatePartition)
            // only state partitions of the state machine to be considered here
            elseif sn.stateNodeKind = statePartition then
                Self.stateNodesToBeChecked := Self.stateNodesToBeChecked \{sn}
            elseif sn.stateNodeKind = stateNode then
                let curSigId: Identifier = Self.signalChecked.signalType in
                    Self.stateNodeChecked := sn
                Self.stateNodesToBeChecked := Self.stateNodesToBeChecked \{sn}
                Self.transitionsToBeChecked :=
                            {t \in sn.stateTransitions.inputTransitions: t.s-SIGNAL = curSigId }
                if Self.signalChecked.signalType \in
                        sn.stateAS1.s-Save-signalset.s-Signal-identifier-set then
                        Self.SignalSaved := true
                endif
            endlet
            endif
    endlet
    NEXTSIGNALTOBECHECKED \equiv
    let si= nextSignal(Self.signalChecked, Self.inputPortChecked) in
            if si\not= undefined then
            Self.signalChecked := si
            Self.SignalSaved := false
            else
                Self.agentMode3 := selectInput
                Self.agentMode4 := startPhase
                RETURNEXECRIGHT
            endif
    endlet
endwhere
```

For a given signal instance in the input port, all current state nodes of the agent are checked in an arbitrary order, beginning, for each state partition, with the innermost state node. The latter reflects the priority among conflicting transitions. Furthermore, when a particular state node is being checked, the inherited state nodes are checked next, i.e., inheritance is taken into account at execution time and not handled by transformations. As a redefinition takes precedence over the redefined transition, the
inherited nodes are to be checked only if the current signal instance is neither saved nor consumed in the current state.

If the given signal instance is not a priority input in the current states of the agent, the next signal instance of the input port is checked. This is repeated until either all signals have been checked, or a priority input has been found. In the former case, the selection of an input transition is triggered.

## F3.2.3.2.10 Input selection

Selection of an input is performed by checking, for each signal instance of the agent's input port, all current state nodes until a signal instance satisfying certain conditions is found. If no such signal instance is found, the selection of a continuous signal is triggered.


Figure F3-9 - Activity phases of SDL-2010 agents: selecting inputs (level 4)
The selection of an ordinary input consists of the sub-phases shown in the state diagram. In comparison to the selection of a priority input, an evaluation phase is added. This phase is entered when a provided expression has to be evaluated. At any time during the selection phase, an attempt to select a spontaneous signal may be made, depending on the value of the monitored predicate Self.spontaneous.

```
SELECTINPUT \(\equiv\)
    if Self.agentMode4 \(=\) startPhase then
        SELInPuTSTARTPHASE
    elseif Self.agentMode4 = selectionPhase then
        SelinputSelectionPhase
    elseif Self.agentMode \(4=\) evaluationPhase then
        SelinputEvaluationPhase
    elseif Self.agentMode4 \(=\) selectSpontaneous then
        SelectSpontaneous
    endif
```

This ASM macro defines the upper level control structure of the input selection. Depending on the agent mode agentMode3, further action is defined in the corresponding ASM macro. This control structure is part of the previous state diagram.

```
SELInPUTSTARTPHASE \equiv
    if Self.inputPortChecked }=\mathrm{ empty then
        Self.signalChecked := Self.inputPortChecked.head
        Self.SignalSaved := false
        Self.stateNodesToBeChecked := collectCurrentSubStates(Self.topStateNode)
        Self.stateNodeChecked := undefined
        Self.transitionsToBeChecked := \varnothing
        Self.agentMode4 := selectionPhase
    else
        Self.agentMode3 := selectContinuous
```

```
    Self.agentMode4 := startPhase
    RETURNEXECRIGHT
endif
```

When the selection starts, it is checked whether the input port contains signals. If so, several initializations are made: the first signal instance to be checked is determined, the state nodes to be checked are set, the transitions to be checked are reset, and the selection is activated. If the input port is empty, the selection of a continuous signal is triggered.

```
SeLInPuTSELECtIONPHASE \equiv
    if Self.stateNodeChecked = undefined then
        NextStateNodeToBeChecked1
    elseif Self.spontaneous then
        Self.agentMode4 := selectSpontaneous
        Self.agentMode5 := selectionPhase
    elseif Self.transitionsToBeChecked }\not=\varnothing\mathrm{ then
        choose t:t : Self.transitionsToBeChecked
            Self.transitionsToBeChecked := Self.transitionsToBeChecked \{t}
            if t.s-LABEL = undefined then
                    EvaluAtEENABLINGCONDITION}(t
            else
                    Self.currentSignalInst := Self.signalChecked
                    Self.sender:= Self.signalChecked.signalSender
                    DELETE(Self.signalChecked,Self.inport)
                    TrANSITIONFOUND(t)
            endif
        endchoose
    else
        Self.stateNodeChecked := undefined
    endif
    where
```

        EvaluateEnablingCondition \((t: S E M T R A N S I T I O N) ~ \equiv\)
            Self.transitionChecked \(:=t\)
            Self.currentStateId \(:=\) Self.stateNodeChecked.parentStateNode.stateId
            Self.currentLabel \(:=t . \mathbf{s}-L A B E L\)
            Self.agentMode4 := evaluationPhase
                NextStatenodetobeChecked \(\equiv\)
            if Self.stateNodesToBeChecked \(\neq \varnothing \wedge \neg\) Self.SignalSaved then
                SelectnextStateNode1
            else
                if \(\neg\) Self.SignalSaved then // implicit transition
                    DELETE(Self.signalChecked,Self.inport)
                endif
                NextSignalToBeChecked
                        Self.stateNodesToBeChecked := collectCurrentSubStates(Self.topStateNode)
                    Self.stateNodeChecked \(:=\) undefined
            endif
        SelectNextStateNodel \(\equiv\)
            let \(s n=\) Self.stateNodesToBeChecked.selectNextStateNode in
                    if \(s n=\) undefined then
                        UndefinedBehaviour
            elseif sn.stateNodeKind = procedureNode then
                        Self.stateNodesToBeChecked \(:=\) Self.stateNodesToBeChecked \(\backslash\)
                        collectCurrentSubStates(sn.getPreviousStatePartition)
                            // only state partitions of the state machine to be considered here
                    elseif sn.stateNodeKind \(=\) statePartition then
                    Self.stateNodesToBeChecked \(:=\) Self.stateNodesToBeChecked \(\backslash\{\) sn \(\}\)
                    elseif sn.stateNodeKind \(=\) stateNode then
    ```
                Self.stateNodeChecked := sn
                Self.stateNodesToBeChecked := Self.stateNodesToBeChecked \{sn}
            Self.transitionsToBeChecked := {t\in sn.stateTransitions.inputTransitions:
                        t.s-SIGNAL = Self.signalChecked.signalType}
            if Self.signalChecked.signalType }
                sn.stateAS1.s-Save-signalset.s-Signal-identifier-set then
                    Self.SignalSaved := true
            endif
        endif
    endlet
    NEXTSIGNALToBEChECKED1 \equiv
    let si= nextSignal(Self.signalChecked,Self.inputPortChecked) in
        if si\not= undefined then
            Self.signalChecked := si
            Self.SignalSaved := false
        else
            Self.agentMode3 := selectContinuous
            Self.agentMode4 := startPhase
            RETURNEXECRIGHT
        endif
    endlet
endwhere
```

For a given signal instance in the input port, all current state nodes of the agent are checked in an arbitrary order, beginning, for each state partition, with the innermost state node. The latter reflects the priority among conflicting transitions. Furthermore, when a particular state node is being checked, the inherited state nodes are checked next, i.e., inheritance is taken into account at execution time and not handled by transformations. As a redefinition takes precedence over the redefined transition, the inherited nodes are to be checked only if the current signal instance is neither saved nor consumed in the current state.

If the given signal instance is saved in the current states of the agent, the next signal instance of the input port is checked. This is repeated until either all signals have been checked, or an input has been selected. In the former case, the selection of a continuous signal is triggered.

```
SeLInPuTEvaluATIONPHASE \equiv
    if Self.currentLabel =| undefined then
        choose b: b \in behaviour ^b.s-LABEL = Self.currentLabel
            EVAL(b.s-ACTION)
        endchoose
    elseif semvalueBool(value(Self.transitionChecked.s-LABEL,Self)) then
            Self.currentSignalInst := Self.signalChecked
            Self.sender:= Self.signalChecked.signalSender
            DELETE(Self.signalChecked,Self.inport)
            TransitionFound(Self.transitionChecked)
    else
        Self.agentMode4 := selectionPhase
    endif
```

If an input transition has a provided expression, this expression has to be evaluated before continuing with the selection. As this evaluation consists of several actions in general, another agent mode, evaluationPhase, is entered. After completion of the evaluation, either the considered input signal is consumed, or the selection continues.

## F3.2.3.2.11 Continuous signal selection

Selection of an input is performed by checking, for each signal instance of the agent's input port, all current state nodes until a signal instance satisfying certain conditions is found. If no such signal instance is found, this cycle of transition selection ends, and another cycle is started.


Figure F3-10 - Activity phases of SDL-2010 agents: selecting continuous signals (level 4)

The selection of a continuous signal consists of the sub-phases shown in the state diagram. The control is identical to the selection of an ordinary input.

```
SELECTCONTINUOUS \equiv
    if Self.agentMode4 = startPhase then
        SelContinuousStartPhase
    elseif Self.agentMode4 = selectionPhase then
        SelContinuousSelEctionPhase
    elseif Self.agentMode4 = evaluationPhase then
        SelContinuousEvaluationPhase
    elseif Self.agentMode4 = selectSpontaneous then
        SelectSpontanEous
    endif
```

This ASM macro defines the upper level control structure of the continuous signal selection. Depending on the agent mode agentMode4, further action is defined in the corresponding ASM macro. This control structure is part of the previous state diagram.

```
SeLCONTINUOUSSTARTPHASE \equiv
    Self.stateNodesToBeChecked := collectCurrentSubStates(Self.topStateNode)
    Self.stateNodeChecked := undefined
    Self.transitionsToBeChecked := \varnothing
    Self.agentMode4:= selectionPhase
```

When the selection starts, several initializations are made: the state nodes to be checked are set, the transitions to be checked are reset, and the selection is activated.

```
SelContinuousSelectionPhASE \equiv
    if Self.stateNodeChecked = undefined then
        NEXTSTATENODEToBECHECKED2
    elseif Self.spontaneous then
        Self.agentMode4 := selectSpontaneous
        Self.agentMode5 := selectionPhase
    else
        let t= selectContinuousSignal(Self.transitionsToBeChecked,Self.continuousPriorities) in
            if }t\not=\mathrm{ undefined then
            Self.transitionsToBeChecked := Self.transitionsToBeChecked \{t}
            if t.s-LABEL = undefined then
                    EvaluateEnabLINGCondition1(t)
            else
                    TRANSITIONFOUND(t)
            endif
        else
            NexTStatENODETOBECHECKED2
        endif
```

endlet
endif
where
EVALUATEENABLINGCONDITION1 $(t: S E M T R A N S I T I O N) ~ \equiv$
Self.transitionChecked $:=t$
Self.currentStateId $:=$ Self.stateNodeChecked.parentStateNode.stateId
Self.currentLabel $:=t . s-L A B E L$
Self.agentMode $4:=$ evaluationPhase
NextStatenodetobechecked $2 \equiv$
if Self.stateNodesToBeChecked $\neq \varnothing$ then
if Self.stateNodeChecked $=$ undefined then
SelectNextStateNode2
else
CHECKFORINHERITEDSTATENODES
endif
else
Self.agentMode3 $:=$ startSelection RETURNEXECRIGHT
endif
SelectnextStatenode $2 \equiv$
let $s n=$ Self.stateNodesToBeChecked.selectNextStateNode in
if $s n=$ undefined then
UndEFINEDBEHAVIOUR
elseif sn.stateNodeKind $=$ procedureNode then
Self.stateNodesToBeChecked $:=$ Self.stateNodesToBeChecked $\backslash$ collectCurrentSubStates(sn.getPreviousStatePartition)
// only state partitions of the state machine to be considered here
elseif sn.stateNodeKind $=$ statePartition then
Self.stateNodesToBeChecked $:=$ Self.stateNodesToBeChecked $\backslash\{s n\}$
elseif $s n$. stateNodeKind $=$ stateNode then
Self.stateNodeChecked $:=$ sn
Self.stateNodesToBeChecked $:=$ Self.stateNodesToBeChecked $\backslash\{s n\}$
Self.transitionsToBeChecked $:=$ sn.stateTransitions.continuousSignalTransitions
Self.continuousPriorities $:=\varnothing$
endif
endlet
CHECKFORINHERITEDSTATENODES $\equiv$
let $s n=$ Self.stateNodeChecked in
let $s n 1=$ selectInheritedStateNode(sn, Self.stateNodesToBeChecked) in
if $\operatorname{sn} 1 \neq$ undefined then
Self.stateNodesToBeChecked $:=$ Self.stateNodesToBeChecked $\backslash\{$ snl $\}$
Self.stateNodeChecked := sn1
Self.transitionsToBeChecked :=
sn1.stateTransitions.continuousSignalTransitions
Self.continuousPriorities :=Self.continuousPriorities $\cup$
$\{t . \mathbf{s}-N A T \mid t \in$ sn.stateTransitions.continuousSignalTransitions $\}$
else
Self.stateNodeChecked := undefined
endif
endlet
endlet
endwhere
All current state nodes of the agent are checked in an arbitrary order, beginning, for each state partition, with the innermost state node. The latter reflects the priority among conflicting transitions. Furthermore, when a particular state node is being checked, the inherited state nodes are checked.

Finally, redefined transitions take precedence over conflicting inherited transitions also in case of continuous signals. If no continuous signal is found, another cycle of the transition selection is started.

```
SELCONTINUOUSEVALUATIONPHASE \(\equiv\)
    if Self.currentLabel \(\neq\) undefined then
        choose \(b: b \in\) behaviour \(\wedge b . \mathbf{s}-L A B E L=\) Self.currentLabel
            \(\operatorname{EVAL}(b . s-A C T I O N)\)
        endchoose
    elseif semvalueBool(value(Self.transitionChecked.s-LABEL,Self)) then
        TransitionFound(Self.transitionChecked)
    else
        Self.agentMode4 := selectionPhase
    endif
```

For each continuous signal, the continuous expression has to be evaluated. As this evaluation consists of several actions in general, another agent mode, evaluationPhase, is entered. After completion of the evaluation, either the considered continuous signal is consumed, or the selection continues.

## F3.2.3.2.12 Spontaneous transition selection

Selection of a spontaneous transition is performed by checking, at any time during the selection process, a single spontaneous transition.


Figure F3-11 - Activity phases of SDL-2010 agents: selecting spontaneous transitions (level 5)
Since any time the agent mode selectSpontaneous is entered, only one spontaneous transition is checked, there are only two sub-modes (agentMode5), as shown in the diagram.

```
SELECTSPONTANEOUS \equiv
    if Self.agentMode5 = selectionPhase then
        SelSpontanEOUSSElECtIONPHASE
    elseif Self.agentMode5 = evaluationPhase then
        SElSponTANEOUSEvaluATIONPHASE
    endif
```

This ASM macro defines the upper level control structure of the spontaneous transition selection. Depending on the agent modeagentMode5, further action is defined in the corresponding ASM macro. This control structure is part of the previous state diagram.

```
SELSPONTANEOUSSELECTIONPHASE \equiv
    if Self.stateNodeChecked.stateTransitions.spontaneousTransitions \not=\varnothing then
        choose t:t\in Self.stateNodeChecked.stateTransitions.spontaneousTransitions
            if t.s-LABEL }\not=\mathrm{ undefined then
                EvALUATEENABLINGCONDITION2(t)
            else
                Self.sender := Self.selfPid
                    TransitionFound(t)
            endif
        endchoose
    else
        Self.agentMode4 := selectionPhase
```

endif
where

```
    EvaluateEnablingCondition2(t:SEmTRANSITION) \(\equiv\)
    Self.transitionChecked \(:=t\)
    Self.currentStateId \(:=\) Self.stateNodeChecked.parentStateNode.stateId
    Self.currentLabel \(:=t . \mathrm{s}-\) LABEL
    Self.agentMode5 := evaluationPhase
```

endwhere

For a given state node, an arbitrary spontaneous transition is selected, and it is checked whether this transition is fireable.

```
SELSPONTANEOUSEVALUATIONPHASE }
    if Self.currentLabel }=\mathrm{ undefined then
        choose b: b E behaviour ^b.s-LABEL = Self.currentLabel
            EvAL(b.s-ACTION)
        endchoose
    elseif semvalueBool(value(Self.transitionChecked.s-LABEL,Self)) then
        Self.sender := Self.selfPid
        TrANSITIONFOUND(Self.transitionChecked)
    else
        Self.agentMode4 := selectionPhase
    endif
```

If a spontaneous transition has a provided expression, this expression has to be evaluated before continuing with the selection. As this evaluation consists of several actions in general, another agent mode, evaluationPhase, is entered. After completion of the evaluation, either the considered spontaneous transition is selected, or the selection of priority input, input or continuous signals is resumed.

## F3.2.3.2.13 Transition firing

The firing of a transition is decomposed into the firing of individual actions, which may in turn consist of a sequence of steps. At the beginning of a transition, the current state node is left; at the end, either a state node is entered, or a termination takes place.


Figure F3-12 - Activity phases of SDL-2010 agents: firing transitions (level 3)

```
FIRETRANSITION \equiv
    if Self.agentMode3 = firingAction then
        FireAction
    elseif Self.agentMode3 = leavingStateNode then
        LEAVESTATENODES
    elseif Self.agentMode3 = enteringStateNode then
        ENTERSTATENODES
```

```
elseif Self.agentMode3 = exitingCompositeState then
    ExITCOMPOSITESTATE
elseif Self.agentMode3 = initialisingProcedure then
        InITPROCEDURE
endif
```

Firing of a transition consists of firing a sequence of actions. Once started, transitions are completely executed.

## F3.2.3.2.14 Firing of actions

```
FIREAction \equiv
    if Self.currentLabel }=\mathrm{ undefined then
        choose b: b b behaviour }\wedgeb.s-LABEL = Self.currentLabel
            EvAL(b.s-ACTION)
        endchoose
    else
        Self.agentMode2 := selectingTransition
        Self.agentMode3 := startSelection
        RETURNEXECRIGHT
    endif
```

Firing of actions is defined by the selection and evaluation of the corresponding SAM primitives. Once started, the firing of actions continues until either a transition is completed (i.e., the current label has the value undefined) or until the agent mode is changed during the evaluation of a primitive. This is, for instance, the case when a state node is entered. The function currentLabel uniquely identifies a behaviour primitive.

## F3.2.3.2.15 Entering of state nodes

```
ENTERSTATENODES \equiv
    if Self.agentMode4 = startPhase then
        EnTERSTATENODESSTARTPHASE
    elseif Self.agentMode4 = enterPhase then
        EnterStateNodesEnterPHASE
    elseif Self.agentMode4 = enteringFinished then
        ENTERSTATENODESENTERINGFINISHED
    endif
```

State nodes are entered when the execution of an agent starts, and possibly when a next state action is executed. When this phase is started, a single state node with an entry point has already been selected. Depending on the structure of the hierarchical graph, further state nodes to be entered may be encountered when this single state node is entered.


Figure F3-13 - Activity phases of SDL-2010 agents: entering state node (level 4)

```
ENTERSTATENODESSTARTPHASE \equiv
    Self.agentMode4 := enterPhase
```

At the beginning of this phase, the set of entered state nodes is initialized. This set is updated every time another state node is entered, and evaluated at the end of the phase to determine the set of current state nodes of the agent.

```
ENTERSTATENODESENTERPHASE \equiv
    if Self.stateNodesToBeEntered }\not=\varnothing\mathrm{ then
        choose snwen: snwen \in Self.stateNodesToBeEntered
            snwen.s-STATENODE.currentSubStates := 
            snwen.s-STATENODE.currentExitPoints := 
            snwen.s-STATENODE.previousSubStates := \varnothing
            if snwen.s-STATENODE.parentStateNode }\not=\mathrm{ undefined then
                snwen.s-STATENODE.parentStateNode.currentSubStates :=
                snwen.s-STATENODE.parentStateNode.currentSubStates }\cup{\mathrm{ snwen.s-STATENODE}
            endif
            if snwen.s-STATENODE.stateNodeRefinement = undefined then
                REFINEMENTUNDEF(snwen)
            elseif snwen.s-STATENODE.stateNodeRefinement = stateAggregationNode then
                REFINEMENTSTATEAGGRNODE(snwen)
            elseif snwen.s-STATENODE.stateNodeRefinement = compositeStateGraph then
                REFINEMENTCOMPSTATENODE(snwen)
            endif
        endchoose
    else
    Self.agentMode4 := enteringFinished
endif
where
```

```
REFINEMENTUndEF(snwen:STATENodEWITHENTRYPoint) \(\equiv\)
    let \(s n:[\) StateNode \(]=\)
            take \((\{\) snl \(\in\) STATENODE: directlyInheritsFrom(snwen.s-STATENODE,snl) \(\})\) in
        if \(s n \neq\) undefined then
            // refinement possibly inherited
            Self.stateNodesToBeEntered \(:=\) Self.stateNodesToBeEntered \(\backslash\{\) snwen \(\} \cup\)
                \{ mk-StateNodeWithEntryPoint(sn,
                    snwen.s-implicit) \}
            else
            Self.stateNodesToBeEntered \(:=\) Self.stateNodesToBeEntered \(\backslash\{\) snwen \(\}\)
            endif
        endlet
```

RefinementstateAgarnode(snwen:STATENODEWITHENTRYPoint) $\equiv$
if snwen s-implicit $=$ HISTORY then
Self.stateNodesToBeEntered $:=$ Self.stateNodesToBeEntered $\backslash\{$ snwen $\} \cup$

$s \in$ snwen.s-STATENODE.previousSubStates $\}$
else
Self.stateNodesToBeEntered $:=$ Self.stateNodesToBeEntered $\backslash\{$ snwen $\} \cup$
\{ mk-STATENODEWITHENTRYPOINT(sp,
entryConnection(snwen.s-implicit, sp))|
$s p \in$ snwen.s-STATENODE.statePartitionSet $\}$
endif
let cstd: Composite-state-type-definition =
snwen.s-STATENODE. stateDefinitionAS1 in
let aggr: State-aggregation-node $=c s t d$.s-implicit in
if aggr.s-Entry-procedure-definition $\neq$ undefined then
CreateProcedure(aggr.s-Entry-procedure-definition, undefined,
undefined)
endif
endlet

```
        if comp.s-Entry-procedure-definition }=\mathrm{ undefined then
            CREATEPROCEDURE(comp.s-Entry-procedure-definition, undefined,
                undefined)
            endif
    endlet
    if snwen.s-implicit = HISTORY then
    Self.stateNodesToBeEntered := Self.stateNodesToBeEntered \{snwen}}
        { mk-STATENODEWITHENTRYPOINT(s, HISTORY)|
                s \in snwen.s-STATENODE.previousSubStates }
    else
    Self.currentStartNodes := Self.currentStartNodes }\cup{\mathrm{ snwen }
    endif
endwhere
```

Entering of state nodes continues until the set stateNodesToBeEntered is empty. A distinction is made between state nodes with and without a refinement. If there is a refinement into a state aggregation node, then the entry procedure of that node is to be executed, and all state partitions are to be entered. If there is a refinement into a composite state graph, then a start transition has to be selected and executed, which determines a substate to be entered. Finally, if the state node is not refined, it may be belong to a composite state with a state type inheriting from another state type, where it is refined.

EnterStateNodesEnteringFinished $\equiv$
Self.agentMode $2:=$ selectingTransition
Self.agentMode3 := startSelection
RETURNEXECRIGHT
When the set stateNodesToBeEntered is empty, the transition selection is activated by setting the agent modes accordingly.

## F3.2.3.2.16 Leaving of state nodes

```
LEAVESTATENODES \equiv
    if Self.agentMode4 = leavePhase then
        LEAVESTATENODESLEAVEPHASE
        elseif Self.agentMode4 = leavingFinished then
            LEAVESTATENODESLEAVINGFINISHED
        endif
```

State nodes are left when transitions are fired. The set of state nodes to be left has already been determined when this rule macro is applied.


Figure F3-14 - Activity phases of SDL-2010 agents: leaving state node (level 4)

```
LEAVESTATENODESLEAVEPHASE \equiv
    let sn=Self.stateNodesToBeLeft.selectNextStateNode in
        if }sn=\mathrm{ undefined then
            Self.agentMode4 := leavingFinished
        else
            Self.stateNodesToBeLeft := Self.stateNodesToBeLeft \{sn}
            sn.parentStateNode.currentSubStates:= sn.parentStateNode.currentSubStates \{sn}
            sn.parentStateNode.previousSubStates := sn.parentStateNode.previousSubStates }\cup{sn
            if sn.stateNodeRefinement = compositeStateGraph then
```

```
            let cstd : Composite-state-type-definition =
                        sn.stateAS1.s-Composite-state-type-identifier.idToNodeAS1 in
            let comp : Composite-state-graph = cstd.s-implicit in
                if comp.s-Exit-procedure-definition }=\mathrm{ undefined then
                    CREATEPROCEDURE(comp.s-Exit-procedure-definition,undefined,
                    undefined)
                endif
            endlet
        elseif sn.stateNodeRefinement = stateAggregationNode then
            let cstd: Composite-state-type-definition=
                sn.stateAS1.s-Composite-state-type-identifier.idToNodeAS1 in
            let aggr: State-aggregation-node = cstd.s-implicit in
                if aggr.s-Exit-procedure-definition }==\mathrm{ undefined then
                    CREATEPROCEDURE(aggr.s-Exit-procedure-definition, undefined,
                    undefined)
            endif
            endlet
        endif
    endif
endlet
```

In the leave phase, state nodes that have been collected are left, from bottom to top, with possible synchronization at state aggregation nodes. If defined, exit procedures are executed.

```
LEAVESTATENODESLEAVINGFINISHED \equiv
    if Self.stateNodeToBeExited }\not=\mathrm{ undefined then
        Self.currentExitStateNodes := {Self.stateNodeToBeExited }
        Self.stateNodeToBeExited := undefined
        Self.agentMode3 := exitingCompositeState
    else
        Self.agentMode3 := firingAction
        Self.currentLabel := Self.continueLabel
        Self.continueLabel := undefined
    endif
```

When the leaving of a state node has been completed, either the exiting of a state node or firing of the current transition has to be continued.

## F3.2.3.2.17 Exiting of composite states

```
ExITCOMPOSITESTATE \equiv
    if Self.stateNodeToBeExited }\not=\mathrm{ undefined then
        let sn=Self.stateNodeToBeExited.s-STATENODE in
        if sn.stateNodeKind = stateNode then
            Self.currentExitStateNodes := {Self.stateNodeToBeExited }
            Self.stateNodeToBeExited := undefined
            Self.agentMode2 := selectingTransition
            Self.agentMode3 := startPhase
        elseif sn.stateNodeKind = statePartition then
            sn.parentStateNode.currentExitPoints := sn.parentStateNode.currentExitPoints
                \cup ~ \{ S e l f . s t a t e N o d e T o B e E x i t e d . s - S T A T E E X I T P O I N T \}
            Self.stateNodesToBeLeft:= {sn}
            Self.agentMode3 := leavingStateNode
            Self.agentMode4 := leavePhase
            endif
        endlet
    elseif Self.currentExitStateNodes }\not=\varnothing\mathrm{ then
        let snwex = take(Self.currentExitStateNodes) in
            let sn= snwex.s-STATENODE in
            if sn.parentStateNode.currentSubStates }=\varnothing\mathrm{ then
                let ep = take(sn.parentStateNode.currentExitPoints) in
                    Self.stateNodeToBeExited := mk-STATENODEWITHExitPoinT(
```

```
                    sn.parentStateNode, exitConnection(ep,sn))
                    Self.currentExitStateNodes := \varnothing
                        endlet
            else
                        Self.currentExitStateNodes := \varnothing
                Self.agentMode2 := selectingTransition
                Self.agentMode3 := startPhase
            endif
        endlet
    endlet
endif
```


## F3.2.3.2.18 Stopping agent execution

An agent ceases to exist as soon as all contained agents have been removed.

```
STOPPHASE \equiv
    if \forallsas \in SDLAGENTSET: (sas.owner = Self }=>\neg\existssa\inSDLAGENT: sa.owner = sas) then
        RemoveAllAgentSets(Self)
        RemoveAgent(Self)
    endif
```


## F3.2.3.3 Interface between execution and compilation

The execution of agents requires certain behaviour parts (called "compilation units") to be treated during compilation. Compilation units are sequences of actions of an agent that, once started, are executed without being interleaved by other actions of this agent or an agent belonging to the same set of nested agents:

- (Regular) transitions: Each transition starts with the evaluation of input parameters (if any), followed by an action "leaveStateNode", followed by Transition as defined in the abstract syntax. If the terminator of the transition is a Nextstate-node, the transition ends with an action "enterStateNode".
- Start transitions (Named-start-node, State-start-node, Procedure-start-node): These are associated with the containing state node.
- Exit transitions (Named-return-node): These are associated with the set of transitions of the containing state node.
- Expressions: During the selection phase, enabling conditions and continuous signals have to be evaluated. In these cases, the evaluation of an expression is a compilation unit.
Each compilation unit has a start label. Once a start label is assigned to the function currentLabel of an agent, the sequence of actions that begins with this label - the evaluation of an expression or the firing of a transition - is sequentially executed. This means that whenever an action has been executed, the compilation determines the continue label such that the next action follows. The termination of this sequence is "signalled" by having the continue label set to undefined after the last action of the sequence.

During compilation, a function uniqueLabel: DEFINITIONAS1 $\times$ NAT $\rightarrow$ LABEL associates unique labels with each node of the AST. The unique labels of nodes corresponding to compilation units are used as starting labels. Furthermore, labels are used to retrieve the result of the evaluation of expressions.

## F3.3 Data semantics

## F3.3.1 Predefined data

An operator is functional if it is predefined. The built-in procedures for structures and literals are treated as predefined.

```
            ( procedure.identifier..s-Qualifier.head \in Package-qualifier ^
                procedure.identifier l.s-Qualifier.head.s-Package-name.s-TOKEN = "Predefined")
    \checkmark ~ i s S p e c i a l S t r u c t O p ( p r o c e d u r e )
    \checkmark ~ i s S p e c i a l L i t e r a l O p ( p r o c e d u r e ) ~
intype(procedure: PROCEDURE, name: Name): BOOLEAN = def
    procedure.identifierrl.s-Qualifier.last.s-Data-type-name = name
compute (procedure: PROCEDURE, values: VALUE*): VALUEOREXCEPTION = def
    if intype (procedure, IntegerType.s-Name) then computeInteger(procedure, values)
    elseif intype (procedure, BooleanType.s-Name) then computeBoolean(procedure, values)
    elseif intype (procedure, CharacterType.s-Name) then computeChar(procedure, values)
    elseif intype (procedure, RealType.s-Name) then computeReal(procedure, values)
    elseif intype (procedure, DurationType.s-Name) then computeDuration(procedure, values)
    elseif intype (procedure, TimeType.s-Name) then computeTime(procedure, values)
    elseif intype (procedure, StringType.s-Name) then computeString(procedure, values)
    elseif intype (procedure, ArrayType.s-Name) then computeArray(procedure, values)
    elseif intype (procedure, PowersetType.s-Name) then computePowerset(procedure, values)
    elseif intype (procedure, BagType.s-Name) then computeBag(procedure, values)
    elseif isSpecialStructOp(procedure) then computeStruct(procedure, values)
    elseif isSpecialLiteralOp (procedure) then computeLiteral(procedure, values)
    else
        raise(OutOfRange)
    endif
```

The TOKEN domain consists of character strings. The function emptyToken is therefore an empty character string.

```
emptyToken: TOKEN = = def
```

The function definingSort computes the scope in which an operator was defined.

```
definingSort(p: PROCEDURE): Identifier = def
    p.parentAS1.identifier 
```

The function procName computes the token of an operator.

```
procName(p: PROCEDURE): TOKEN = 
```

    p.s-Operation-name.s-TOKEN
    
## F3.3.1.1 Predefined Data Types, Exceptions and Boolean Operations

A set of functions refers to predefined Data-type-definition nodes from the package Predefined.

```
BooleanType: Identifier = \(_{\text {def }}\)
    mk-Identifier(<mk-Package-qualifier(mk-Name("Predefined"))>, mk-Name("Boolean"))
CharacterType: Identifier \(=_{\text {def }}\)
    mk-Identifier(<mk-Package-qualifier(mk-Name("Predefined"))>, mk-Name("Character"))
StringType: Identifier \(=_{\text {def }}\)
    mk-Identifier(<mk-Package-qualifier(mk-Name("Predefined"))>, mk-Name("String"))
IntegerType: Identifier \(=_{\text {def }}\)
    mk-Identifier(<mk-Package-qualifier(mk-Name("Predefined"))>, mk-Name("Integer"))
RealType: Identifier \(=\) def
    mk-Identifier(<mk-Package-qualifier(mk-Name("Predefined"))>, mk-Name("Real"))
ArrayType: Identifier \(=\) def
    mk-Identifier(<mk-Package-qualifier(mk-Name("Predefined"))>, mk-Name("Array"))
PowersetType: Identifier \(=_{\text {def }}\)
    mk-Identifier(<mk-Package-qualifier(mk-Name("Predefined"))>, mk-Name("Powerset"))
DurationType: Identifier \(=_{\text {def }}\)
    mk-Identifier(<mk-Package-qualifier(mk-Name("Predefined"))>, mk-Name("Duration"))
TimeType: Identifier \(=_{\operatorname{def}}\)
    mk-Identifier(<mk-Package-qualifier(mk-Name("Predefined"))>, mk-Name("Time"))
```

```
BagType:Identifier =
    mk-Identifier(<mk-Package-qualifier(mk-Name("Predefined"))>, mk-Name("Bag"))
PidType:Identifier = def
    mk-Identifier(<mk-Package-qualifier(mk-Name("Predefined"))>, mk-Name("Pid"))
```

Furthermore, there are a number of predefined identifiers for exceptions.

```
OutOfRange: Identifier \(=_{\text {def }}\)
    mk-Identifier(<mk-Package-qualifier(mk-Name("Predefined"))>, mk-Name("OutOfRange"))
InvalidReference: Identifier \(=_{\text {def }}\)
    mk-Identifier(<mk-Package-qualifier(mk-Name("Predefined"))>,mk-Name("InvalidReference"))
NoMatchingAnswer: Identifier \(=_{\text {def }}\)
    mk-Identifier(<mk-Package-qualifier(mk-Name("Predefined"))>,mk-Name("NoMatchingAnswer "))
UndefinedVariable: Identifier \(=_{\text {def }}\)
    mk-Identifier(<mk-Package-qualifier(mk-Name("Predefined"))>,mk-Name("UndefinedVariable"))
UndefinedField: Identifier \(=_{\text {def }}\)
    mk-Identifier(<mk-Package-qualifier(mk-Name("Predefined"))>, mk-Name("UndefinedField"))
InvalidIndex: Identifier \(=_{\text {def }}\)
    mk-Identifier(<mk-Package-qualifier(mk-Name("Predefined"))>, mk-Name("InvalidIndex"))
DivisionByZero: Identifier \(=\) def
    mk-Identifier(<mk-Package-qualifier(mk-Name("Predefined"))>, mk-Name("DivisionByZero"))
EmptyException: Identifier \(=_{\text {def }}\)
    mk-Identifier(<mk-Package-qualifier(mk-Name("Predefined"))>, mk-Name("Empty"))
InvalidCall: Identifier \(=_{\text {def }}\)
    \(\mathbf{m k}-I d e n t i f i e r(<\mathbf{m k}-P a c k a g e-q u a l i f i e r(\mathbf{m k}-N a m e(\) "Predefined"))>, mk-Name("InvalidCall"))
InvalidSort: Identifier \(=_{\text {def }}\)
    mk-Identifier(<mk-Package-qualifier(mk-Name("Predefined"))>, mk-Name("InvalidSort"))
```

To raise an exception, the function raise is used. Each Predefined exception is an Identifier and is a member of the EXCEPTION domain (see clause F3.2.1.1.6). If raise is invoked the further behaviour of the system is not defined by SDL-2010.

```
raise(ex:Identifier): Identifier = = def
    UNDEFINEDBEHAVIOUR
```

There are also the following predefined operation signatures:

```
sdlAnd: Static-operation-signature = def
    mk-Operation-signature(mk-Name("and"),
        < (BooleanType),(BooleanType)>)
sdlOr: Static-operation-signature = = def
    mk-Operation-signature(mk-Name("or"),
        < (BooleanType),(BooleanType)>)
sdlTrue: Literal-signature = def
    mk-Literal-signature (mk-Name("true"), mk-Result(BooleanType), undefined)
```


## F3.3.1.2 Boolean

The function computeBoolean determines the value of an application of a Predefined Boolean operator.

```
SDLBOOLEAN = def BOOLEAN }\times\mathrm{ Identifier
computeBoolean(procedure: PROCEDURE, values: VALUE*):VALUEOREXCEPTION = = def
    let restype =definingSort(procedure) in
    case procedure.procName of
    | "not" => mk-SDLBOOLEAN(\neg values.head.semvalueBool, restype)
    | "and" => mk-SDLBOOLEAN(values.head.semvalueBool ^ values.tail.head.semvalueBool, restype)
    | "or" => mk-SDLBOOLEAN(values.head.semvalueBool v values.tail.head.semvalueBool, restype)
    | "xor" => mk-SDLBOOLEAN(\neg (values. head.semvalueBool }\Leftrightarrow\mathrm{ values.tail.head.semvalueBool),
                restype)
```

```
    | "=>" => mk-SDLBOOLEAN(values.head.semvalueBool => values.tail.head.semvalueBool,
    restype)
    endcase
    endlet
```

semvalueBool(v:SDLBOOLEAN): BOOLEAN $=_{\text {def }} v . s$-BOOLEAN

## F3.3.1.3 Integer

```
SDLINTEGER = def NAT }\times\mathrm{ Identifier
semvalueInt(v:SDLINTEGER): NAT= def v.s-NAT
computeInteger(procedure: PROCEDURE, values: VALUE*): VALUEOREXCEPTION = def
    let restype = definingSort(procedure) in
    if procedure \in Literal-signature then
        integerLiteral(0,procedure.procName, restype)
    elseif procedure.procName = "-" ^ values.length = 1 then
        mk-SDLINTEGER(0 - values.head.semvalueInt, restype)
    elseif procedure.procName \in {"+", "-", "*", "/", "mod", "rem", "<", ">", "<=", ">=", "power"}
    then
        let vall = values[1]. semvalueInt, val2 = values[2]. semvalueInt in
            case procedure.procName of
            | "+" => mk-SDLINTEGER (vall+val2, restype)
            | "-"=> mk-SDLINTEGER (vall - val2, restype)
            |"*"=> mk-SDLINTEGER (vall * val2, restype)
            | "/"=>
                    if val2 = 0 then
                        raise(DivisionByZero)
            else
                mk-SDLINTEGER (intDiv(val1,val2), restype)
            endif
            | "mod"=>
                if val2 = 0 then
                    raise(DivisionByZero)
            else
                mk-SDLINTEGER (intMod(val1,val2), restype)
            endif
            | "rem"=>
                if val2 = 0 then
                raise(DivisionByZero)
            else
                mk-SDLINTEGER (intRem(vall,val2), restype)
            endif
            | "power"=> mk-SDLINTEGER (intPower(vall,val2), restype)
            | "<" => mk-SDLBOoLEAN(vall < val2, BooleanType)
            | "<=" => mk-SDLBOOLEAN(vall \leq val2, BooleanType)
            | ">" => mk-SDLBOoLEAN(vall > val2, BooleanType)
            | ">="=> mk-SDLBOoLEAN(vall \geq val2, BooleanType)
            endcase
            endlet
            else raise(OutOfRange)
    endif
    endlet
```

The function numberValue determines the NAT associated with a single character in the range " 0 " to "9".
numberValue(c:TOKEN): NAT = ${ }_{\text {def }}$
case $c$ of
| "0" => 0
| "1" => 1

```
| "2" => 2
" "3" => 3
| "4" => 4
| "5" => 5
| "6" => 6
| "7" => 7
| "8" => 8
| "9" => 9
endcase
```

The function integerLiteral returns the SDLINTEGER value for a real literal.

```
integerLiteral(num: NAT, proc: TOKEN, type: Identifier): SDLINTEGER = def
    if proc = emptyToken then
            mk-SDLINTEGER (num, type)
    else
            integerLiteral(num*10 + numberValue(proc.head), proc.tail, type)
    endif
```

The function intDiv returns the result of integer-dividing its arguments.

```
intDiv(a: NAT, b: NAT):NAT = def
    if }a\geq0\wedgeb>a\mathrm{ then 0
    elseif }a\geq0\wedgeb\leqa\wedgeb>0 then 1+\operatorname{intDiv(a-b,b)
    elseif }a\geq0\wedgeb<0\mathrm{ then - -intDiv(a,-b)
    elseif }a<0\wedgeb<0\mathrm{ then intDiv (-a,-b)
    elseif }a<0\wedgeb>0\mathrm{ then - intDiv (-a,b)
    else raise(DivisionByZero)
    endif
```

The function intMod returns the result of the integer-modulo operation.

```
intMod(a: NAT, b: NAT):NAT = def
    if }a\geq0\wedgeb>0\mathrm{ then intRem(a,b)
    elseif b<0 then intMod(a,-b)
    elseif }a<0\wedgeb>0\wedge\operatorname{intRem}(a,b)=0\mathrm{ then intRem(a,b)
    elseif }a<0\wedgeb>0\wedge\operatorname{intRem}(a,b)<0 then b+\operatorname{intRem}(a,b
    else raise(DivisionByZero)
    endif
```

The function intRem returns the result of the integer-remainder operation.

```
intRem( \(a\) : NAT, \(b:\) NAT): \(N A T=_{\text {def }}\)
    \(a-b * \operatorname{intDiv}(a, b)\)
```

The function intPower returns the result of the integer-power operation.

```
intPower(a: NAT, b: NAT):NAT = def
    if b=0 then 1
    elseif }a=0\mathrm{ then 0
    elseif b>0 then a* intPower(a,b-1)
    else intDiv(intPower(a,b+1),a)
    endif
```


## F3.3.1.4 Character

Character values are represented by their name.

```
SDLCHARACTER }=\mathrm{ def Name }\times\mathrm{ Identifier
computeChar(procedure: PROCEDURE, values: VALUE*): VALUEOREXCEPTION = def
    let restype = definingSort(procedure) in
    if procedure \in Literal-signature then
        mk-SDLCHARACTER(procedure.s-Literal-name, restype)
```

```
elseif procedure.procName = "num" then
    mk-SDLINTEGER(charValue(values.head.s-Name), IntegerType)
elseif procedure.procName = "chr" then
    mk-SDLCHARACTER( values.head.semvalueInt.charChr, restype)
else raise(OutOfRange)
endif
endlet
```

The function charValue returns the numerical value of the character.

```
charValue(ch: Name): NAT = def
    let myDef: Value-data-type-definition = CharacterType.idToNodeAS1 in
    let literals = myDef.s-Literal-signature-set in
        take({L.s-Literal-natural | L Eliterals: L.s-Literal-name =ch})
    endlet
```

The function charChr returns the character for a given Integer.

```
charChr(a: NAT): Name = = def
    if }a>128\mathrm{ then charChr(a-128)
    elseif }a<0\mathrm{ then charChr(a+128)
    else
        let char: Value-data-type-definition = CharacterType.idToNodeAS1 in
        let literals = char.s-Literal-signature-set in
            take({L.s-Literal-name | L \in literals: L.Literal-natural =a})
    endif
```


## F3.3.1.5 Real

The Predefined type Real is represented as a rational number, with numerator and denominator.

```
SDLREAL = = def NAT }\timesNAT\timesIdentifier
semvalueRealNum(v: SDLREAL): NAT = def v.S-NAT
semvalueRealDen(v: SDLREAL): NAT = def V.S2-NAT
semvalueReal(v: SDLREAL): REAL= =ef
    let res: REAL = v.semvalueRealNum / v.semvalueRealDen in
        res
    endlet
computeReal(procedure: PROCEDURE, values: VALUE*): VALUEOREXCEPTION = def
    let restype = definingSort(procedure) in
    if procedure \inLiteral-signature then
        realLiteral(0,1,procedure.procName, restype)
    elseif procedure.procName = "-" ^ values.length = 1 then
        mk-SDLREAL(0 - values.head.semvalueRealNum, values.head.semvalueRealDen, restype)
    elseif procedure.procName \in{"+", "-", "*", "/", "<", ">", "<=", ">="} then
        let numl = values[1].semvalueRealNum in
        let denl = values[1]. semvalueRealDen in
        let num2 = values[2]. semvalueRealNum in
        let den2 = values[2]. semvalueRealDen in
            case procedure.procName of
                | "+" => mk-SDLREAL(num1*den2 + num2*den1, den1*den2, restype)
                | "-"=> mk-SDLREAL(num1*den2 - num2*den1, den1*den2, restype)
                | "*"=> mk-SDLREAL(num1*num2, den1*den2, restype)
                | "/"=>
                    if num2 = 0 then
                            raise(DivisionByZero)
                else
                    mk-SDLREAL(num1*num2, den1*den2, restype)
                    endif
```

```
        | "<" => mk-SDLBOOLEAN(num1*den2 < num2*den1, BooleanType)
        | "<=" => mk-SDLBOOLEAN(num1*den2 \leqnum2*den1, BooleanType)
        | ">" => mk-SDLBOoLEAN(num1*den2 \geq num2*den1, BooleanType)
        | ">="=> mk-SDLBOOLEAN(num1*den 2 \geq num2*den1,BooleanType)
        endcase
        endlet
elseif procedure.procName = "float" then
    mk-SDLREAL(semvalueInt(values.head), 1, restype)
elseif procedure.procName = "fix" then
    mk-SDLINTEGER(computeFix(values.head.semvalueRealNum,
        values.head.semvalueRealDen), IntegerType)
else raise(OutOfRange)
endif
endlet
```

The function realLiteral returns the SDLREAL value for a real literal.

```
realLiteral(num: NAT, den: NAT, proc: TOKEN, type: Identifier): SDLREAL = def
    if proc = emptyToken then
        mk-SDLREAL(num, den, type)
    elseif proc.head = "." then
        realLiteral(num*10,den*10, proc.tail, type )
    elseif den = 1 then
        realLiteral(num*10 + numberValue(proc.head), den, proc.tail, type)
    else
        realLiteral(num*10 + numberValue(proc.head), den, proc.tail, type)
    endif
```

The function computeFix returns the NAT value given numerator and denominator.

```
computeFix(num: NAT, den: NAT): NAT = def
    if num<0 then
        - computeFix(- num, den) -1
    elseif num < den then
        0
    else
        computeFix (num - den, den) + 1
    endif
```


## F3.3.1.6 Duration

The domain SDLDURATION is based on the domain SDLREAL.

```
SDLDURATION = =def DURATION }\times\mathrm{ Identifier
computeDuration(procedure: PROCEDURE, values: VALUE*):VALUE = def
    computeReal(procedure, values)
```


## F3.3.1.7 Time

The domain SDLTime is based on the domain SDLREAL.

```
SDLTIME }=\mp@subsup{=}{\mathrm{ def }}{}\mathrm{ TIME }\times\mathrm{ Identifier
computeTime(procedure: PROCEDURE, values:VALUE*):VALUE = def
    let restype = definingSort(procedure) in
    if procedure \inLiteral-signature then
        realLiteral(0,1,procedure.procName, restype)
    else
    case procedure.procName of
        | "time"=>
        let val: SDLREAL = values.head in
            mk-SDLREAL(val.s-NAT, val.s2-NAT, RealType)
        endlet
```

```
    | "<" => computeReal(procedure, values)
    | "<=" => computeReal(procedure, values)
    | ">" => computeReal(procedure, values)
    | ">=" => computeReal(procedure, values)
    | "+" => computeReal(procedure, values)
    | "-" =>
        if values.head \inSDLTIME ^ values.tail.head }\in\mathrm{ SDLDURATION then
        computeReal(procedure, values)
    else
        let res: SDLREAL = computeReal(procedure,values) in
                mk-SDLREAL(res.s-NAT, res.s2-NAT, RealType)
        endlet
    endif
endcase
endif
endlet
```


## F3.3.1.8 String

A string type is defined as a sequence of its element type.

```
SDLSTRING = def VALUE * }\times\mathrm{ Identifier
computeString (procedure: PROCEDURE, values: VALUE*): VALUEOREXCEPTION = def
let restype = definingSort(procedure) in
    case procedure.procName of
    | "emptystring"=>mk-SDLSTRING(empty, restype)
    | "mkstring"=> mk-SDLSTRING(<values.head>, restype)
    | "make"=> mk-SDLSTRING(<values.head>, restype)
    | "length"=> mk-SDLInTEGER (values.head. s-VALUE-seq.length, IntegerType)
    | "first"=> values.head. s-VALUE-seq.head
    | "last"=> values.head. s-VALUE-seq.last
    | "//"=> mk-SDLSTRING(values[1]. s-VALUE-seq `values[2].s-VALUE-seq, restype)
    | "extract"=>
        let string = values[1]. s-VALUE-seq in
        let intval: SDLINTEGER = values[2] in
        let index = intval.s-NAT in
            if index < 0 v index> string.length then
                raise(InvalidIndex)
            else
                string[index]
            endif
        endlet
    | "modify"=>
            let intval: SDLINTEGER = values[2] in
            let index = intval.s-NAT in
            let front = substr(values[1].s-VALUE-seq, 1, index-1) in
            let back = substr(values[1].s-VALUE-seq, index+1, values[1].s-VALUE-seq.length - index) in
                if InvalidIndex = front }\vee\mathrm{ InvalidIndex = back then raise(InvalidIndex)
                    else
                            mk-SDLSTRING(front }\mp@subsup{<}{}{\mathrm{ values[3]>}}\frown\mathrm{ back, restype)
                endif
            endlet
    | "substring"=>
                            let from: SDLINTEGER = values[2] in
                        let to: SDLInTEGER = values[3] in
                        let val=substr(values[1].s-VALUE-seq, from.s-NAT, to.s-NAT) in
                        if InvalidIndex = val then raise(InvalidIndex)
                            else mk-SDLSTRING(val, restype) endif
                    endlet
    | "remove"=>
            let intval: SDLINTEGER = values[2] in
```

```
        let index = intval.s-NAT in
        let front=substr(values[1].s-VALUE-seq, 1, index-1) in
        let back = substr(values[1].s-VALUE-seq, index+1, values[1].s-VALUE-seq.length - index) in
            if InvalidIndex = front v InvalidIndex = back then raise(InvalidIndex) else
                mk-SDLSTRING(front`back, restype)
            endif
        endlet
    endcase
endlet
```

The function substr computes the substring of a string value.

```
substr(str: VALUE*,start: NAT, len: NAT): VALUE* \cup EXCEPTION = def
    if start }\leq0\veelen\leq0\vee start+len-1> str.length then
        raise(InvalidIndex)
    elseif len =0 then
        empty
    else
        substr(str,start,len-1)}\frown<str[start+len-1]>
    endif
```


## F3.3.1.9 Array

An array is represented as a set of index/itemsort pairs, with an optional default value.


```
VALUEPAIR = def VALUE }\times VALUE
computeArray(procedure: PROCEDURE, values: VALUE*):VALUEOREXCEPTION = def
    let restype = definingSort(procedure) in
    if procedure.procName = "Make" then
        if values.length =0 then
            mk-SDLARRAY(\varnothing, undefined, restype)
        else
            mk-SDLARRAY(\varnothing,values.head, restype)
        endif
    elseif procedure.procName = "Modify" then
        let }a=\mathrm{ values[1], index = values[2], value = values[3] in
            mk-SDLARRAY(modifyArray(a.s-VALUEPAIR-set, index, value), a.s-VALUE, restype)
        endlet
    elseif procedure.procName = "Extract" then
        let v=\operatorname{take({ f.s2-VALUE |f\in values[1].s-VALUEPAIR-set: f.s-VALUE = values[2]}) in}
            if v= undefined then
                if values[1].s-VALUE = undefined then
                raise(InvalidIndex)
                    else
                        values[1].s-VALUE
            else
                v
        endlet
    else raise(OutOfRange)
    endif
    endlet
modifyArray(a: VALUEPAIR-set, index: VALUE, value: VALUE): VALUEPAIR-set =def
    { item|item }\in\mathrm{ a: item.s-VALUE }\not=\mathrm{ index }}\cup{\mathbf{mk}-VALUEPAIR(index,value)
```


## F3.3.1.10 Powerset

A Powerset is represented as a set.

```
computePowerset (procedure: PROCEDURE, values: VALUE*): VALUEOREXCEPTION = \({ }_{\mathrm{def}}\)
    let restype \(=\) definingSort(procedure) in
    case procedure.procName of
    | "empty"=> mk-SDLPOWERSET( \(\varnothing\),restype)
    |"in"=> mk-SDLBOOLEAN(values[1] є values[2].s-VALUE-set, BooleanType)
    |"incl"=> mk-SDLPOWERSET(values[2].s-VALUE-set \(\cup\{\) values[1] \}, restype)
    | "del"=> mk-SDLPOWERSET(values[2].s-VALUE-set \\{values[1] \}, restype) }
    |"く"=> mk-SDLBooLEAN(values[1].s-VALUE-set \(\subset\) values[2].s-VALUE-set, BooleanType)
    | "<=" \(=>\) mk-SDLBooLEAN(values[1].s-VALUE-set \(\subseteq\) values[2].s-VALUE-set, BooleanType)
    |">"=> mk-SDLBOoLEAN(values[2].s-VALUE-set \(\subset\) values[1].s-VALUE-set, BooleanType)
    |">="=> mk-SDLBOOLEAN(values[2].s-VALUE-set \(\subseteq\) values[1].s-VALUE-set, BooleanType)
    | "and"=> mk-SDLPOWERSET(values[1].s-VALUE-set \(\cap\) values[2].s-VALUE-set, restype)
    | "or"=> mk-SDLPOWERSET(values[1].s-VALUE-set \(\cup\) values[2].s-VALUE-set, restype)
    | "length"=> mk-SDLINTEGER( | values[1].s-VALUE-set |, IntegerType)
    | "take"=> if values[1].s-VALUE-set \(=\varnothing\) then
                raise(EmptyException)
                    else
                values[1]. s-VALUE-set.take
            endif
    endcase
    endlet
```


## F3.3.1.11 Bag

A Bag is represented as a set of value-frequency pairs.

```
SDLBAG = def FREQUENCY-set }\times\mathrm{ Identifier
FREQUENCY = def VALUE }\timesNA
computeBag (procedure: PROCEDURE, values: VALUE*): VALUEOREXCEPTION = def
    let restype = definingSort(procedure) in
    case procedure.procName of
    | "empty"=> mk-SDLBAG(\varnothing,restype)
    | "in"=> mk-SDLBooLEAN(bagcount(values[1], values[2]) = 0, BooleanType)
    "incl"=> mk-SDLBAG(bagincl(values[1], values[2]), restype)
    |"del"=> mk-SDLBAG(bagdel(values[1], values[2]), restype)
    | "<"=> mk-SDLBooLEAN(baginbag(values[1], values[2]), BooleanType)
    | "<="=> mk-SDLBOOLEAN(\neg baginbag(values[2], values[1]), BooleanType)
    | ">"=> mk-SDLBOOLEAN(baginbag(values[2], values[1]), BooleanType)
    | ">="=> mk-SDLBOOLEAN(\neg baginbag(values[1], values[2]), BooleanType)
    | "and"=> mk-SDLBAG(bagand(values[1], values[2]), restype)
    | "or"=> mk-SDLBAG(bagor(values[1], values[2]), restype)
    | "length"=> mk-SDLINTEGER(baglength(values[1].s-FREQUENCY-set), IntegerType)
    | "take"=> values[1].s-FREQUENCY-set.take.s-VALUE
    endcase
    endlet
bagcount(item: VALUE, bag: SDLBAG): NAT = def
    let eleml = {elem.s-NAT |elem \in bag.s-FREQUENCY-set: elem.s-VALUE = item } in
        if eleml = \varnothing then 0 else elem1.take endif
    endlet
bagincl(item: VALUE, bag: SDLBAG): FREQUENCY-set =def
    if bagcount(item, bag) \not=0 then
        {if elem.s-VALUE = item then mk-FREQUENCY(item, elem.s-NAT+1) else elem endif |
                        elem \in bag.s-FREQUENCY-set }
    else
        bag.s-FREQUENCY-set \cup {mk-FREQUENCY (item, 1)}
    endif
```

```
bagdel(item: VALUE, bag: SDLBAG): FREQUENCY-set = def
    if bagcount(item, bag) }=1\mathrm{ then
            {if elem.s-VALUE = item then mk-FREQUENCY(item, elem.s-NAT-1) else elem endif |
            elem }\in\mathrm{ bag.s-FREQUENCY-set}
    else
        bag.s-FREQUENCY-set \{ mk-FREQUENCY(item, 1)}
    endif
baginbag(smaller: SDLBAG, larger: SDLBAG): BOOLEAN =def
    \forallelem \in smaller.s-FREQUENCY-set: bagcount(elem.s-VALUE, larger) < elem.s-NAT
bagand(a: SDLBAG,b:SDLBAG):FREQUENCY-set = def
    { mk-FREQUENCY (x.s-VALUE, min(bagcount(x.s-VALUE,a),bagcount(x.s-VALUE,b)))|
        x\ina.s-FREQUENCY-set: bagcount(x.s-VALUE, b)>0}
min(a: NAT,b:NAT ):NAT = }\mp@subsup{=}{\operatorname{def}}{}\mathrm{ if }a>b\mathrm{ then a else b endif
bagor(a: SDLBAG,b: SDLBAG): FREQUENCY-set =def
    { mk-FREQUENCY(x.s-VALUE, bagcount(x.s-VALUE,a) + bagcount(x.s-VALUE, b) )
        | x a a.s-FREQUENCY-set }
    \cup \{ x \| x \in b . s - F R E Q U E N C Y - s e t : ~ b a g c o u n t ( x . s - V A L U E , ~ a ) = 0 \}
baglength(a: FREQUENCY-set):NAT = def
    if }a=\varnothing\mathrm{ then 0
    else let x=a.take in
        x.s-NAT + baglength(a\{x})
        endlet
    endif
```


## F3.3.2 Pid types

A PID value is represented by an agent and an interface.

```
PID \(=_{\text {def }}\) VALIDPID \(\cup\) NULLPID
NULLPID \(=_{\text {def }}\{\mathbf{m k}-N u l l-l i t e r a l-s i g n a t u r e(m k-N a m e(" n u l l "), ~ P i d t y p e, ~ u n d e f i n e d) ~\} ~\)
VALIDPID \(=_{\text {def }}\) SDLAGENT \(\times\) [Interface-definition]
static nullPid: PID \(=_{\text {def }}\) take (NULLPID)
```

The static function nullPid is the special PID value for the unique named element of the Pid sort (denoted by "null") that does not identify any agent and is the unique element of NULLPID.

## F3.3.3 Constructed types

## F3.3.3.1 Structures

A structure value is identified by its type name, and the field list. The field names are a list, rather than a set because Make operator uses the order of the fields rather than the field names.


```
FIELD = def Name }\times\mathrm{ VALUE
isSpecialStructOp(procedure: PROCEDURE): BOOLEAN = = def
    let procsort = procedure.definingSort,pn= procedure.procName in
    (\exists str \in SDLSTRUCTURE: (procsort = str.s-Identifier )) ^
    ( (pn = "Make")
    \vee (pn= "Undefined")
    \vee ~ ( \exists ~ f l d ~ \in ~ p r o c s o r t . s - F I E L D - s e q : ~ ( p n = f l d . s - N a m e ~ ` ~ " M o d i f y " ) ) )
    \vee ~ ( \exists f l d ~ \in ~ p r o c s o r t . s - F I E L D - s e q : ~ ( p n = f l d . s - N a m e ~ ` ~ " E x t r a c t " ) ) )
    \vee ~ ( \exists ~ f l d ~ \in ~ p r o c s o r t . s - F I E L D - s e q : ~ ( p n = f l d . s - N a m e ~ ` ~ " P r e s e n t " ) ) ~ )
```

The function computeStruct gives the value of applying the language-defined operators for structures.

```
computeStruct(procedure: PROCEDURE, values: VALUE*): VALUEOREXCEPTION \(=\mathrm{def}\)
    let structsort \(=\) definingSort(procedure), \(p n=\) procedure.procName in
    if \(p n=\) "Undefined" then
            structUndefined(structsort)
    elseif \(p n=\) "Make " then
            structMake(structsort, empty, structsort.s-FIELD-seq, values)
    elseif ( \(\exists\) fld \(\in\) structsort.s-FIELD-seq: \((p n=\) fld.s-Name \(\frown\) "Modify") then
            let \(f n \frown\) "Modify" \(=p n\) in
            structModify(fn, structsort, values.head, empty, structsort.s-FIELD-seq)
        endlet
    elseif ( \(\exists\) fld \(\in\) structsort.s-FIELD-seq: ( \(p n=\) fld.s-Name \(\frown\) "Extract") then
        let \(f n \frown\) "Extract" \(=p n\) in
            structExtract(fn, structsort)
        endlet
    elseif \((\exists\) fld \(\in\) structsort.s-FIELD-seq: \((p n=\) fld.s-Name \(\frown\) "Present" \())\) then
        let \(f n \frown\) "Present" \(=p n\) in
            structFieldPresent(fn, structsort)
        endlet
    else raise(OutOfRange)
    endif
    endlet
```

The function structMake creates a structure value with the fields initialized to the list of values. It should be called externally (internally it is recursive) with a structure value, an empty list of new fields (newflds) and a list of old fields (oldflds) that each has a field name defined, and a list of one or more values. The new fields (newflds) and old fields (oldflds) are used in the internal recursion.

```
structMake(st: SDLSTRUCTURE, newflds: FIELD*, oldflds: FIELD*, values: VALUE*):VALUE = def
    if values.length < oldflds.length then structMake(st, newflds,oldflds,values }~\mathrm{ undefined)
    elseif values.length =0\vee oldflds.length =0 then
        mk-SDLSTRUCTURE(newflds, st.s-Identifier)
    else
        structMake(st, newflds` mk-FIELD(oldflds.head.s-Name,values.head),
            oldflds.tail, values.tail )
    endif
```

The function structUndefined returns the true if (and only if) all the fields are undefined.

```
structUndefined(st: SDLSTRUCTURE): SDLBOOLEAN = def
    mk-SDLBoolEAN(semvalueBool(\forallvalue \in st.s-FIELD.s-VALUE: (value = undefined)), BooleanType)
```

The function structExtract returns the field with a given name from a list of fields.

```
structExtract(fieldname:Name, structtype: SDLSTRUCTURE):VALUE = def
    let valueset ={f.s-VALUE |f\in structtype.s-FIELD-seq: f.s-Name = fieldname } in
        if valueset = \varnothing then raise(UndefinedField)
        else valueset.take
        endif
    endlet
```

The function structModify returns a new structure with one field changed. It should be called externally (internally it is recursive) with the field name, a structure value, the new value for the field, an empty list of new fields (newflds) and a list of old fields (oldflds) that each have a field name defined. The new fields (newflds) and old fields (oldflds) are used in the internal recursion.

```
structModify(fn: Name, struct: SDLSTRUCTURE, val: VALUE, newflds: FIELD*, oldflds: FIELD*):
```

```
    SDLSTRUCTURE \(=_{\text {def }}\)
if oldflds.length \(=0\) then
    mk-SDLSTRUCTURE(newflds, struct.s-Identifier)
else
    structModify(fn, struct, val,
        newflds \(\frown\)
            mk-FIELD(oldflds.head.s-Name,
                if oldflds.head.s-Name = fieldname then val else oldflds.head.s-VALUE endif),
        oldflds.tail)
endif
```

The function structFieldPresent returns the true if the specified field has a value．

```
structFieldPresent(fn: Name, st: SDLSTRUCTURE): SDLBOOLEAN = def
    mk-SDLBOoLEAN(semvalueBool(fn.parentAS1.s-FIELD.s-VALUE ₹ undefined), BooleanType)
```


## F3．3．3．2 Literals

Values of a literal sort are represented by the type in which the literal is defined，and the literal signatures：

```
SDLLITERALS = def Literal-signature }\times\mathrm{ Identifier
isSpecialLiteralOp(procedure: PROCEDURE): BOOLEAN = def
    let procsort = procedure.definingSort,pn= procedure.procName in
    (\exists lit \in SDLLITERALS: (procsort = lit.s-Identifier )) ^
    ( pn \in { "<", ">","<=",">=", "first", "last", "succ", "pred", "num" })
```

The function computeLiteral gives the value of applying the language－defined operators for structures．

```
computeLiteral(procedure:PROCEDURE, values:VALUE*): [VALUE ]=⿱⿰㇒一大口
    let restype = definingSort(procedure) in
    let defi:Value-data-type-definition = restype.idToNodeAS1 in
    if procedure.procName \in { "<", ">","<=",">=" } then
        let vl = values.head.s-Literal-signature.literalNum in
        let v2 = values.tail.head.s-Literal-signature.literalNum in
        case procedure.procName of
        | ">" => mk-SDLBOOLEAN(v1 > v2,BooleanType)
        | ">=" => mk-SDLBOOLEAN(v1 \geq v2,BooleanType)
        | "<" => mk-SDLBOOLEAN(v1 < v2,BooleanType)
        | "<=" => mk-SDLBOoLEAN(vl \leqv2,BooleanType)
        endcase
        endlet
    elseif procedure.procName = "first" then
        literalMinimum (defi.s-Literal-signature-set)
    elseif procedure.procName = "last" then
        literalMaximum (defi.s-Literal-signature-set)
    elseif procedure. procName = "succ" then
        literalSucc(defi.s-Literal-signature-set, values.head)
    elseif procedure. procName = "pred" then
        literalPred(defi.s-Literal-signature-set, values.head)
    elseif procedure. procName = "num" then
        mk-SDLINTEGER(literalNum(values.head).semvalueInt, IntegerType)
    else
        undefined
    endif
    endlet
literalNum(s: Literal-signature): NAT = def
    s.s-Literal-natural
```

```
literalValue(s: Literal-signature): VALUE \(=_{\text {def }}\)
    mk-SDLLITERALS(s, s.s-Result)
literalMinimum(s: Literal-signature-set): VALUE \(=_{\text {def }}\)
    take(\{sl.literalValue
        \(\mid s 1 \in s: \forall s 2 \in s: s 2 . l i t e r a l N u m>s 1\).literalNum \(\})\)
literalMaximum(s: Literal-signature-set): VALUE \(=_{\text {def }}\)
    take (\{s1.literalValue
        \(\mid s 1 \in s: \forall s 2 \in s: s 2 . l i t e r a l N u m<s 1\).literalNum \(\})\)
literalSucc(s: Literal-signature-set, val: SDLLITERALS): VALUE \(=_{\mathrm{def}}\)
    if val \(=\) literalMaximum \((s\), val.s-Identifier \()\) then literalMinimum( \(s\), val.s-Identifier \()\)
    else
        take (\{sl.literalValue \(\mid s l \in s \wedge\)
                        (sl.literalNum > val.s-NAT) \(\wedge\)
            \((\forall s 2 \in s:(s 2 . l i t e r a l N u m \leq s . l i t e r a l N u m) \vee(s 1\).literalNum \(\leq s 2\).literalNum \())\}\)
    endif
literalPred(s: Literal-signature-set, val: SDLINTEGER): VALUE \(=_{\text {def }}\)
    if val \(=\) literalMinimum \((s\), val.s-Identifier) then literalMaximum ( \(s\), val.s-Identifier)
    else
        take (\{sl.literalValue \(\mid s l \in s \wedge\)
            (sl.literalNum < val.s-NAT) ^
            \((\forall s 2 \in s:(s 2 . l i t e r a l N u m \leq s 1 . l i t e r a l N u m) \vee(s . l i t e r a l N u m \leq s 2 . l i t e r a l N u m))\}\)
    endif
```


## F3.3.3.2 Choice

Further study is required for this subject.

## F3.3.4 Variables with Aggregation-kind REF

Further study is required for this subject.

## F3.3.5 State access

The STATE domain consists of substates (associations of values for a specific STATEID), and super states (associations between super state and substate). In case a certain variable is bound to an in/out parameter in a substate, it refers to the variable in the caller's state.

```
STATE = def NAMEDVALUE-set }\times\mathrm{ SUPERSTATE-set
NAMEDVALUE = def STATEID }\times\mathrm{ Variable-identifier }\times[\mathrm{ [BOUNDVALUE }
BOUNDVALUE = def VALUE \cup Variable-identifier
SUPERSTATE = def STATEID }\times\mathrm{ STATEID
initAgentState(state: [STATE], newid: STATEID, id: [STATEID], declarations: DECLARATION-set): STATE = def
    let newsub = initDeclarations(newid, declarations) in
    if state = undefined then
        mk-STATE(newsub, \varnothing, \varnothing)
    else
    let newsuper = if id = undefined then }\varnothing\mathrm{ else { mk-SUPERSTATE(id, newid)} endif in
        mk-STATE(state.s-NAMEDVALUE-set }\cup\mathrm{ newsub, state.s-SUPERSTATE-set }\cup\mathrm{ newsuper)
    endif
    endlet
initProcedureState(state: STATE, newid: STATEID, id: STATEID, vars: DECLARATION-set,
    declarations: DECLARATION*,
    values:VALUE*,variables:Variable-identifier*): STATE = def
```

```
    let newsub = assignValues(initDeclarations(newid, vars }\cup\mathrm{ declarations.toSet),
                                    newid,declarations,
                                    values, variables) in
    let newsuper = mk-SUPERSTATE(id, newid) in
        mk-STATE(state.s-NAMEDVALUE-set }\cup\mathrm{ newsub, state.s-SUPERSTATE-set }\cup{\mathrm{ newsuper })
    endlet
initDeclarations(newid: STATEID, decls: DECLARATION-set): NAMEDVALUE-set =def
    { mk-NAMEDVALUE(newid, d.identifier, d.s-Constant-expression)
        |d\in decls:d\in Variable-definition}}
    { mk-NAMEDVALUE(newid, d.identifier }\mp@subsup{}{l}{
        undefined)
        |d\in decls: d \in Procedure-formal-parameter }
```

The function assignValues puts a sequence of parameter values into a named values set for a given state id.

```
assignValues(namedvalues:NAMEDVALUE-set, id: STATEID, decls:DECLARATION*
    values:VALUE*,variables:Variable-identifier*): NAMEDVALUE-set = = def
    if values = empty then
        namedvalues
    else
    if decls.head \in In-parameter then
        assignValues(setValue(namedvalues, id, variables.head,values.head),
                        id, decls.tail, values.tail, variables.tail)
    else
        assignValues(namedvalues, id, decls.tail, values.tail, variables.tail)
    endif
```

The function setValue puts a single value into a named values set for a given state id.

```
setValue(namedvalues: NAMEDVALUE-set, id: STATEID, varname:Identifier, value:VALUE):
    NAMEDVALUE-set = def
    { binding | binding \in namedvalues:
        binding.s-Variable-identifier }=\mathrm{ varname }\vee\mathrm{ binding.s-STATEID }\not=id}
    { mk-NAMEDVALUE(id, varname, value) }
```

The function getValue returns the association between id and varname in namedvalues.

```
getValue(namedvalues: NAMEDVALUE-set, id: STATEID, varname:Identifier): NAMEDVALUE-set = def
```



```
        b.s-STATEID = id ^ b.s-Variable-identifier = varname }
```

The function eval returns the value associated with a state, a state id, and a name. If there is named value for the state and identified variable, there can be at most one. If this named value has a bound value that is a value, this is the result. Otherwise, if the bound value is a variable identifier, this bound variable must be a variable in the caller (the state id that caused this state id to exist), because static semantics ensures each variable exists. In this case eval is called recursively to return the value (in the named values for the state) for the bound variable and the caller (the state id that caused this state id to exist). Otherwise the bound value is undefined, and undefined returned. If no named value is associated, the static semantics ensures the variable exists, so the identified variable must be associated with the caller (the state id that caused this state id to exist). In this case eval is called recursively to return the value (in the named values for the state) for the given variable and the caller state.

```
eval(varname:Identifier, state:STATE, id:STATEID): VALUEOREXCEPTION = def
    let callerid = caller(state,id) in
            let namedval = getValue(state.s-NAMEDVALUE-set, id, varname) in
                if namedval }\not=\varnothing\mathrm{ then
                    if namedval.take.s-BOUNDVALUE \in VALUE then
                    namedval.take.s-BOUNDVALUE
```

```
            elseif namedval.take.s-BOUNDVALUE \in Variable-identifier then
                                    eval(namedval.take.s-BounDVALUE, state, callerid)
            else // the BOUNDVALUE is undefined
                raise(UndefinedVariable)
            endif
        else
            eval(varname, state, callerid)
        endif
        endlet
    endlet
```

The function update modifies a binding of a name to a value.

```
update(name:Identifier, value:VALUE, state:STATE, id:STATEID): STATE = def
    let val = getValue(state.s-NAMEDVALUE-set, id, name) in
        if val= \varnothing then
            update(name, value, state, caller(state, id))
        elseif val.take \in NAMEDVALUE then
            mk-STATE(setValue(state.s-NAMEDVALUE-set, id, name, value),
                state.s-SUPERSTATE-set)
        else
            update(val.take.s-Variable-identifier, value, state, id)
        endif
    endlet
```

The function assign modifies the variable with the given name in the state/id association to the given value.

```
assign (variablename:Variable-identifier, value:VALUE, state:STATE, id:STATEID): STATEOREXCEPTION \(=_{\text {def }}\)
    if isValueVariable(variablename) then
        if isSyntypeVariable(variablename) \(\wedge \neg\) rangeCheck(variablename.variableSort, value ) then
            raise(OutOfRange)
        else update(variablename, value, state, id)
        endif
    else
            // pid variable, sort of variable is an Interface-definition
            if variablename.variableSort \(=\) value.interface \(\vee\)
            isSuperType(variablename.variableSort, value.interface) then
            update(variablename, value, state, id)
            else
            update(variablename, nullPid, state, id)
        endif
    endif
```

The function caller returns the state id that caused this state id to exist.

```
caller(state: STATE, id: STATEID): STATEID =def
    take({ s.s-STATEID | s \in state.s-SUPERSTATE-set: s.s2-STATEID = id })
```

The function variableSort returns the sort for a given variable identifier.
variableSort(variableid: Variable-identifier): Data-type-definition $=_{\text {def }}$ variableid.idToNodeAS1.s-Sort-reference-identifier.idToNodeAS1

The predicate isValueVariable holds if the variablename refers to a variable of a value type.
isValueVariable(variableid: Variable-identifier): BOOLEAN $=_{\text {def }}$ variableid.variableSort $\in$ Value-data-type-definition
The predicate isSyntypeVariable holds if the variablename refers to a variable with a syntype.
isSyntypeVariable(variableid: Variable-identifier): BOOLEAN $=_{\text {def }}$ variableid.idToNodeAS1.s-Sort-reference-identifier $\in$ Syntype-identifier
interface(val: VALUE): Interface-definition $=_{\text {def }}$
if val.sort $\in$ Interface-definition then val.sort else undefined endif
The function sort gives the sort of a value, which for most domains (such as SDLBoolean or SDLSTRUCTURE that form part of the VALUE domain) is found from the Identifier element of the domain. The exception is the PID domain, which instead is either a NULLPID that has the value nullPid, and is a PidType value, or is a VALIDPID with an optional Interface-definition. In the case of a VALIDPID without an Interface-definition, the value is a PidType value; otherwise the data type definition is the Interface-definition.

```
sort(val: VALUE): Data-type-definition = def
if val \in NULLPID then PidType.idToNodeASI
elseif val \inVALIDPID then
    if val.s-Interface-definition = undefined then PidType.idToNodeAS1
    else val.s-Interface-definition
    endif
else val.s-Identifier.idToNodeAS1
endif
```


## F3.3.6 Specialization

The function dynamicType determines the identity of the dynamic type of a value.

```
dynamicType( \(v\) : VALUE): Identifier \(=\) def
if \(v=\) nullPid then raise(OutOfRange) else
    case \(v\) of
    \(\mid \operatorname{SDLBOOLEAN}(*, t) \quad=>t\)
    \(\mid \operatorname{SDLINTEGER}(*, t) \quad=>t\)
    \(\mid \operatorname{SDLCharaCter}(*, t) \quad=>t\)
    \(\mid \operatorname{SDLREAL}(*, *, t) \quad=>t\)
    \(\mid \operatorname{SDLSTRING}(*, t) \quad=>t\)
    \(\mid \operatorname{SDLLITERALS}(*, t) \quad=>t\)
    \(\mid \operatorname{SDLSTRUCTURE}(*, t) \quad=>t\)
    \(\mid \operatorname{PID}(*, t) \quad=>t\)
    endcase
endif
```


## F3.3.7 Operators and methods

The function dispatch determines the procedure to select given a set of actual parameters.

```
dispatch(procedure:PROCEDURE, values:VALUE*): Identifier =
    if procedure \in Static-operation-signature then
        procedure.s-Identifier
    else
        let c=allDynamicCandidates(procedure) in
        let cl = matchingCandidates(c, values) in
                        bestMatch(cl)
        endlet
    endif
```

The function allDynamicCandidates returns the set of all signatures with the same name as the given signature.

```
allDynamicCandidates(procedure:PROCEDURE): PROCEDURE-set = def
    { p|p\inOperation-signature:
        p.s-Operation-name = procedure.s-Operation-name }
```

The function matchingCandidates returns the set of all signatures that are compatible with the arguments.

```
matchingCandidates(procedures: PROCEDURE-set, values: VALUE*): PROCEDURE-set = def
```

```
{p|p\in procedures: isSignatureCompatible(p.s-Formal-argument-seq, dynamicTypes(values)) }
```

The function matchingCandidates returns the most specialized signature.

```
bestMatch(procedures:PROCEDURE-set): Identifier = = def
    take({ p.s-Identifier |p { procedures:
    \forallq\in procedures: isSignatureCompatible(p.s-Formal-argument-seq,
                q.s-Formal-argument-seq) })
```

The predicate isSignatureCompatible holds if p is compatible with q .

```
isSignatureCompatible(p:Formal-argument*, q:Formal-argument*): BooLEAN = def
    if p=empty then
            true
        else
            isSortCompatible(p.head.s-Argument, q.head.s-Argument) ^
            isSignatureCompatible(p.tail, q.tail)
        endif
isSortCompatible(p:Sort-reference-identifier, r: Sort-reference-identifier): BOOLEAN = def
    (p=r)\vee
    isDirectlySortCompatible(p,r)\vee
    (r.idToNodeASl \in Interface-definition ^
    (\exists q \in Sort-reference-identifier: (isSortCompatible(p,q)^isSortCompatible(q,r))))
isDirectlySortCompatible(y:Sort-reference-identifier, z: Sort-reference-identifier): BOOLEAN = def
    if isSuperSort (z,y) then
            if y.idToNodeASl \in Value-data-type-definition then
                    // true if y is <anchored sort> of the form this z
                    y.idToNodeAS1.s-Data-type-identifier = z
            else // y is a pid sort (because not a value dat type) - and z is super sort of y
                true
            endif
        else false
        endif
isSuperSort(z Sort-reference-identifier, y: Sort-reference-identifier): BOOLEAN = def
    isSuperType(z, y) // see clause F2.2.1.6.4.
dynamicTypes(values:VALUE*): Formal-argument* }\mp@subsup{=}{\mathrm{ def }}{
    <mk-Formal-argument(dynamicType(v))|v in values>
```


## F3.3.8 Syntypes

The predicate rangeCheck holds if the range check for a value of a syntype passes.

```
rangeCheck(syntype: Syntype-definition, value: VALUE): BOOLEAN = def
    \exists cond \in syntype.s-Range-condition.s-Condition-item-set:
        conditionItemCheck(cond, value, syntype.s-Parent-sort-identifier)
```

The predicate conditionItemCheck holds if the condition is true for the value of the given type. If the condition is a size constraint, rewriting the concrete grammar creates an anonymous operation identified by the Operation-identifier of the Size-constraint that embodies the ranges specified, so the Open-range or Closed-range items in the abstract grammar of Size-constraint are redundant. An alternative would be to construct an anonymous procedure here based on the Open-range or Closedrange items of Size-constraint, in which case the Operation-identifier of Size-constraint is redundant.

```
conditionItemCheck(cond: Condition-item, value: VALUE, type: Identifier): BOOLEAN \(=\) def
    if cond \(\in\) Open-range then
            semvalueBool(compute(cond.s-Open-range.s-Operation-identifier,
                < cond.s-Open-range.s-Constant-expression >))
    elseif cond \(\in\) Closed-range then
```

choose lessthaneq: lessthaneq $\in$ type.s-Static-operation-signature-set $\wedge$ lessthaneq.procName = "<=" semvalueBool(compute(lessthaneq, <cond.s-Closed-range.s-Constant-expression, value > )) $\wedge$ semvalueBool(compute(lessthaneq, < value, cond.s-Closed-range.s2-Constant-expression >)) endchoose
else //size constraint and cond $\in$ Size-constraint
semvalueBool(compute(cond.s-Size-constraint.s-Operation-identifier, < value >))
endif

## Appendix I to Annex F3

## List of abstract syntax grammar rules used

This list contains the Specification and Description Language abstract syntax grammar rules that are used in this annex (Annex F3). The complete list of abstract syntax grammar rules can be found in Annex A of Recommendation ITU-T Z.100, which also identifies the Recommendation ([ITU-T Z.101] or [ITU-T Z.102] or [ITU-T Z.104] or [ITU-T Z.107]) where the grammar rule is defined.

Action-return-node
Agent-definition
Agent-identifier
Agent-kind
Agent-type-definition
Agent-type-identifier
Any-expression
Argument
Assignment
Break-node
Call-node
Channel-definition
Channel-path
Closed-range
Composite-state-graph
Composite-state-type-definition
Composite-state-type-identifier
Compound-node
Condition-item
Conditional-expression
Connect-node
Connection-definition
Connector-name
Constant-expression
Continue-node
Continuous-expression
Continuous-signal
Create-request-node
Dash-nextstate
Data-type-definition
Data-type-identifier
Data-type-name
Decision-answer
Decision-node
Destination-gate
Entry-connection-definition
Entry-procedure-definition
Equality-expression
Exception-identifier
Exit-connection-definition
Exit-procedure-definition
Formal-argument
Free-action
Gate-definition
Graph-node
Identifier
In-parameter
In-signal-identifier
Initial-number

Inner-entry-point<br>Inner-exit-point<br>Input-node<br>Interface-definition<br>Join-node<br>Literal<br>Literal-name<br>Literal-natural<br>Literal-signature<br>Maximum-number<br>Name<br>Named-nextstate<br>Named-return-node<br>Named-start-node<br>Nextstate-parameters<br>Now-expression<br>Number-of-instances<br>Null-literal-signature<br>Offspring-expression<br>Open-range<br>Operation-application<br>Operation-identifier<br>Operation-name<br>Operation-signature<br>Originating-gate<br>Out-parameter<br>Out-signal-identifier<br>Outer-entry-point<br>Outer-exit-point<br>Output-node<br>Package-definition<br>Package-name<br>Package-qualifier<br>Parameter<br>Parent-expression<br>Parent-sort-identifier<br>Priority-name<br>Procedure-definition<br>Procedure-formal-parameter<br>Procedure-graph<br>Procedure-identifier<br>Procedure-start-node<br>Provided-expression<br>Qualifier<br>Range-check-expression<br>Range-condition<br>Reset-node<br>Result<br>Save-signalset<br>Self-expression<br>Sender-expression<br>Set-node<br>Signal-definition<br>Signal-identifier<br>Size-constraint<br>Sort-identifier<br>Sort-reference-identifier<br>Spontaneous-transition<br>State-aggregation-node<br>State-entry-point-name<br>State-exit-point-name<br>State-machine<br>State-name

State-node<br>State-partition<br>State-start-node<br>State-transition-graph<br>Static-operation-signature<br>Stop-node<br>Syntype-identifier<br>Syntype-definition<br>Terminator<br>Timer-active-expression<br>Timer-definition<br>Transition<br>Value-data-type-definition<br>Value-return-node<br>Value-returning-call-node<br>Variable-access<br>Variable-definition<br>Variable-identifier

## SERIES OF ITU-T RECOMMENDATIONS

Series A Organization of the work of ITU-T
Series D Tariff and accounting principles and international telecommunication/ICT economic and policy issues

Series E Overall network operation, telephone service, service operation and human factors
Series F Non-telephone telecommunication services
Series G Transmission systems and media, digital systems and networks
Series H Audiovisual and multimedia systems
Series I Integrated services digital network
Series J Cable networks and transmission of television, sound programme and other multimedia signals

Series K Protection against interference
Series L Environment and ICTs, climate change, e-waste, energy efficiency; construction, installation and protection of cables and other elements of outside plant

Series M Telecommunication management, including telecommunication network management and network maintenance

Series N Maintenance: international sound programme and television transmission circuits
Series O Specifications of measuring equipment
Series P Telephone transmission quality, telephone installations, local line networks
Series Q Switching and signalling, and associated measurements and tests
Series R Telegraph transmission
Series S Telegraph services terminal equipment
Series T Terminals for telematic services
Series U Telegraph switching
Series V Data communication over the telephone network
Series X Data networks, open system communications and security
Series Y Global information infrastructure, Internet protocol aspects, next-generation networks, Internet of Things and smart cities

Series Z Languages and general software aspects for telecommunication systems


[^0]:    * To access the Recommendation, type the URL http://handle.itu.int/ in the address field of your web browser, followed by the Recommendation's unique ID. For example, http://handle.itu.int/11.1002/1000/ 11830-en.

[^1]:    controlled stateNodeKind: STATENODE $\rightarrow$ STATENODEKIND
    controlled stateNodeRefinement: STATENODE $\rightarrow$ [STATENODEREFINEMENTKIND]

[^2]:    assign: Variable-identifier $\times$ VALUE $\times$ State $\times$ StateId $\rightarrow$ StateORExCEPTION

